Australian exchange rates, long bond yields and inflationary expectations

Alison Tarditi

Introduction

Australia, like many countries, has undergone extensive market deregulation and internationalisation. More than two decades have elapsed since the initial relaxation of domestic interest rate controls and just over one decade since the float of the Australian dollar. Interest rates and exchange rates now constitute two of the most important channels through which macroeconomic policy can affect the broader economy. Over the longer run, their influence extends to the efficient allocation of capital and resources. The need for policymakers to better understand the forces that determine the behaviour of these two variables motivates this research. In particular, it is now widely recognised that expectations play a critical role in these mechanisms, affecting both the timing and speed by which interest and exchange rates transmit shocks through to real activity and prices. While theoretical discussions of the role of interest and exchange rates often incorporate forward-looking expectations, it has been difficult to model this type of behaviour within an empirical framework. This paper makes that attempt by developing behavioural models of the Australian real exchange rate and the long bond yield which explicitly incorporate some forward-looking behaviour.

Section 1 begins with a review of existing macroeconomic models of the Australian economy. These large-scale models offer the convenience of an internally consistent link between the financial sector variables and the real economy and typically embody forward-looking expectations. But their exchange rate and long bond yield equations reflect orthodox theoretical relationships; they are not estimated equations. This section concludes that, for the purposes of practical policymaking, a more complete analysis of the determinants of financial prices is required. The remaining sections of the paper proceed to develop single equation, behavioural models.

Section 2 builds on the wealth of earlier applied econometric studies of the Australian real exchange rate. This previous literature identifies roles for the terms of trade, net foreign liabilities and long-term interest differentials in determining exchange rate movements. Direct roles for macroeconomic policy and forward-looking expectations have, to date, been ignored. Herein, these omissions are redressed. The explanatory performance of the real exchange rate equation developed in this paper is found to be superior to earlier specifications.

In contrast, very little work has been undertaken in Australia on modelling the behaviour of long bond yields. Section 3 attempts to address this gap. Firstly, a model of the Australian ex ante real long bond yield, deflated with the customary backward-looking measure of inflationary expectations is specified. This draws heavily on Orr, Edey and Kennedy (1995) who identify a comprehensive list of the fundamental determinants of real long-term yields across a 17 country panel data set, including Australia. This time-series model suffers several inadequacies and raises the question of how best to transform nominal bond yields into real magnitudes. Inflation expectations are largely unobservable and the paper spends some time exploring a suitable methodology for their measurement.

In practice, inflationary expectations can be heavily conditioned on a country's historical inflation performance. In Australia, successful inflation reduction policies in the early 1990s appear to have been accompanied by falls in existing measured inflationary expectations series. Section 3.2 discusses the inadequacies of these existing measures and estimates an alternative, forward-looking inflationary expectations series. For this purpose, a Markov switching technique is used. This methodology endogenises shifts in the series and produces estimates of the probabilities associated with remaining in particular (high or low) inflationary regimes. A model of the long-bond yield,
deflated with this unconventional forward-looking series, performs quite well. The final section concludes.

1. The macroeconomic model approach

The two most widely quoted macroeconomic models of the Australian economy are the models developed by the private consulting firm, Econtech (the "Murphy" model)\(^1\) and the model developed by the Australian Commonwealth Treasury (the "TRYM" model)\(^2\). These macro models embody similar philosophies, sharing many common features of design and specification. They have similar theoretical underpinnings, with Keynesian properties in the short run (prices are sticky and output is demand determined) and neoclassical properties in the long run. Equations describing the exchange rate and the long-term bond yield are elements of the financial sectors of these models and reflect orthodox theoretical considerations; they are not estimated behavioural equations. This section briefly discusses these equations and their implied responses to shocks. For illustrative purposes, this exposition pertains to the Murphy model.

The process of expectation formation is central to the performance of the macro model equations. Financial-sector expectations are assumed to be completely forward looking. In the long run, the equilibrium inflation rate is secured by assuming that the authorities target an exogenously determined money growth path. Quarterly inflationary expectations are then calculated from a weighted average of current inflation and the model's one-quarter-ahead predicted long-term equilibrium inflation rate. The equilibrium inflation rate is that rate which is consistent with the difference between money supply (nominal income) and real output growth in period \(t+40\), as derived from the steady-state version of the macro model.

1.1 Exchange rate determination

Each of the macro models employs a concept of the equilibrium real exchange rate. This is defined as that rate which achieves macroeconomic (that is, simultaneous internal and external) balance; it is calculated by a calibration of the steady-state version of the model prior to any dynamic simulation. Following any shock, adjustment back to the equilibrium rate is assumed to be complete within 40 quarters. After tying down the long-run real exchange rate, current and future changes in the real exchange rate are determined by an uncovered interest parity condition – if foreign long (10-year) interest rates are above domestic rates, the current value of the exchange rate must be below its equilibrium value.

More specifically, in the long run (\(t+40\) quarters), the interest differential collapses (either to zero or, alternatively, to some constant risk premium). Agents are assumed to be forward looking and to understand the fundamental structure of the economy and so form model-consistent (rational) estimates of the equilibrium real exchange rate. As mentioned above, this rate realises macroeconomic balance and is akin to the concept of the so-called fundamental equilibrium exchange rate (FEER), popularised by Williamson in the early 1980s.

---

1 Developed by Mr. Chris Murphy; the current disaggregated Murphy model consists of 538 equations.

2 TRYM was developed between 1990 and 1993 and consists of 23 estimated equations, 3 financial market identities, 2 default response functions for monetary and fiscal policy and about 100 identities linking these key variables (Downes (1995)). Other macroeconomic models of the Australian economy include the Monash (see ORANI) model, developed by the Centre of Policy Studies and Impact Project, Monash University, Melbourne; MSG2 and G-Cubed Models developed by Prof. Warwick McKibbin, of the Australian National University Canberra. The financial sector treatment in these models is comparable.
Internal balance is interpreted, in the standard way, as achieving the underlying level of potential output which is consistent with the NAIRU. External balance is more difficult to define and In't Veld (1991), in calculating equilibrium exchange rates for each of the G3 countries, found that his results were very sensitive to changes in this definition. The concept is intended to describe an equilibrium position in the current account; in the Australian macro models this is achieved with a stable ratio of foreign liabilities to GDP (typically stabilised at around 45 per cent, a little higher than the current level)\(^3\). As with any intertemporal analysis, the path to external balance depends on current assessments of the future values of variables. The part of the macroeconomic model that is critical in this exercise is the trade sector which consists of equations expressing the dependence of output and the balance of payments on demand and competitiveness (the real exchange rate). For example, the present discounted value of future terms-of-trade shocks impacts upon the current exchange rate to the extent that it moves the equilibrium exchange rate, in period \(t+40\), to offset income effects on the current account and restore external balance.

The equilibrium exchange rate reflects the specification of interactions within the individual macroeconomic model. Bayoumi et al. (1994) conducted sensitivity analysis on the macroeconomic models of several industrial economies. They found that the estimated range in the calculated equilibrium exchange rates varied between 10 and 30 per cent. This degree of imprecision implies that interpretation of such an equilibrium rate is perhaps better restricted to the identification of relatively large exchange rate misalignments. Furthermore, the calculation of equilibrium real exchange rates as a basis for policy depends on an analysis of whether there are predictable shifts in the real exchange rate and the extent to which different sources of these shifts can be disentangled (for example, structural changes from long-lag dynamics). This is an exercise more appropriately undertaken in the behavioural framework outlined in Section 2.

1.2 Interest rate determination

Consistent with traditional textbook models, but ignoring the practical operation of monetary policy, the short-term interest rate in these macro models is endogenous. The authorities are assumed to target an exogenously determined growth path for money. A simple error-correcting money demand equation describes the link between the financial and real sectors of the macroeconomic model. The long-run component of this estimated money demand equation is inverted to produce a monetary policy rule. In this way, the current level of the short-run nominal interest rate is determined by medium-term changes in nominal demand relative to the money supply. By its nature, the policy rule is arbitrary and a highly simplified representation of the policy formation process\(^4\); the primary function of these mechanisms is to ensure that the economy moves towards a stable growth path in the very long run. The Fisher effect is assumed complete and this delivers the real interest rate.

At the other end of the yield curve, determination of the long bond yield is analogous to the macro model's treatment of the exchange rate. Over the long run, international arbitrage ensures that (subject to a constant risk premium) domestic and foreign long-term real interest rates are equalised. In this way, aggregate demand and supply are equilibrated by adjustments in the real...
exchange rate. Movements in the Australian bond yield away from the foreign rate (equilibrium) are then determined by a term structure calculation.

1.3 Response to shocks

To better illustrate the relevant properties of the macroeconomic models, responses to a domestic monetary policy shock and a terms-of-trade shock are illustrated (Figures 1 and 2).

Figure 1
Money supply shock
Permanent 1% reduction

---

5 The specification of the term structure calculation is model-dependent. In the Murphy model, the yield on a 10-year security is set equal to the expected return from holding a continuous sequence of one-quarter securities over the next 10 years. The expected returns from holding one-quarter securities are model-consistent (Murphy (1988)).

6 These results are obtained from simulations of the Murphy model. Given our understanding of the structure of TRYM, they are broadly representative of the financial sector properties of both macroeconomic models.
Firstly, a permanent 1 percentage point reduction in the exogenous money supply is effected; this can be thought of as a standard textbook monetary policy tightening. Unfortunately, as described earlier, the macro models are not set up to deal with an explicit interest rate shock. Such a simulation would involve successive manipulation of the money supply, producing "bumpy" response functions.

In the manner of forward-looking monetary models, the asset price variables "jump" instantaneously in reaction to any shock, typically exhibiting a damped oscillation back to their long-run paths. A permanent 1 percentage point contraction of the money supply raises real short-term interest rates by 0.63 of a percentage point (panel 1, Figure 1). This delivers a temporary fall-off in demand and a 1 percentage point reduction in the price level. The price fall is anticipated and agents immediately reduce their inflationary expectations by 0.14 of a percentage point.

7 This long-run adjustment behaviour is largely due to the lagged adjustment processes specified to describe the demand side of the models.
The nominal 10-year bond yield jumps up by 0.08 per cent in the initial quarter of the shock; through the uncovered interest parity (UIP) condition, the nominal exchange rate must depreciate by 0.08 of a percentage point per annum for the next 10 years in order to equalise domestic and foreign returns. This requires an immediate appreciation of the exchange rate. Consistent with the imposed theoretical condition of long-run money neutrality, the 1 per cent decrease in the money supply has no effect on real variables in the long run, but leaves the nominal exchange rate appreciated by 1 percentage point.

Alternatively, consider a sustained terms-of-trade shock, here effected through a permanent increase in the foreign price of exports (Figure 2).

This shock raises domestic income; given that not all of this income is spent on imports, the current account balance improves. The macro model's equilibrium exchange rate must appreciate to generate a smaller trade surplus in the long run and thereby restore external balance. As well, a proportion of the higher domestic income is spent on non-tradable goods; this places upward pressure on prices and interest rates, appreciating the exchange rate via the UIP condition. In total, the real exchange rate eventually appreciates by around 0.4 of a percentage point.

1.4 Assessment

The textbook-style impulse responses obtained from the macroeconomic models are useful baseline cases, but policymakers need to think more critically about the determinants of exchange rate and long bond yield behaviour. A number of points in particular are worth highlighting:

- Within the macroeconomic model framework, the exchange rate and long bond yield display an instantaneous "jump" response to all types of shocks. This is usually followed by a damped oscillation to (partly) unwind the initial impulse. Experience suggests that such impulse responses do not accurately capture real world dynamics.

- Inflationary expectations are also characterised as a "jump" variable; their instantaneous response to shocks occurs before any adjustment in actual inflation. This feature of the macro model approach does not line up closely with actual experience. In many cases, a change in inflationary expectations has not occurred until after actual inflation has changed.

- Macro models are designed to analyse shocks to the money supply. By contrast, policy simulations are more naturally examined in terms of changes in the short-term interest rate.

- The size of the estimated exchange rate responses to terms-of-trade shocks cannot comfortably accommodate the long-standing observed correlation between movements in the terms of trade and the Australian dollar (first documented by Blundell-Wignall and Thomas (1987)).

- The assumption of UIP, embodying risk-neutrality (or a constant risk premium), perfect capital mobility, efficiency in the foreign exchange market, and negligible transactions costs has no empirical support (Smith & Gruen (1989) for Australia; Goodhart (1988) and Hodrick (1987) for international evidence). Quite apart from the validity of the UIP assumption, which turns on the issue of unbiasedness, predictions of future exchange rates based on UIP tend to be highly inaccurate.

Therefore, the remainder of this paper proceeds to develop simpler, single-equation behavioural models of the exchange rate and long bond yield. This approach allows a richer characterisation of the distinctive behaviour of these variables in Australia.
2. A behavioural model of the Australian real exchange rate

2.1 What determines the Australian real exchange rate?

Previous empirical work (the most recent and comprehensive of which is Blundell-Wignall et al. (1993), hereafter BW) has identified three statistically significant determinants of the Australian real exchange rate:

- the terms of trade;
- net foreign liabilities (proxied by the cumulative current account deficit);
- real long-term interest differentials.

Each of these is addressed in turn. Firstly, while all three "fundamentals" have been reported as statistically significant determinants of the real TWI exchange rate over the period since the floating of the Australian dollar, only the terms of trade has consistently retained its explanatory power over a longer sample period (1973:2-1992:3). This latter result is consistent with the cross-country study of Amano and Van Norden (1995) which documents a robust relationship between the real domestic price of oil and real effective exchange rates in Germany, Japan and the USA. They interpret the real oil price as capturing exogenous terms-of-trade shocks and find these shocks to be the most important factor determining real exchange rates over the long run.

The relationship between the terms of trade and the Australian real exchange rate is striking, as shown in Figure 3. Depreciations of the real TWI occurring in 1974-1976; 1984-1986; and 1991-1993 were all associated with falls in the terms of trade (denoted by the pale grey bars in Figure 3). Similarly, the real TWI appreciated over 1987-1989 and 1994 when the terms of trade improved (highlighted by the darker grey bars).

Figure 3
Real TWI and terms of trade
Index 1989/90=100

---

8 This is the terms of trade for goods and services. It seems reasonable to take the terms of trade as exogenous because Australia's share of world trade is small and it exports relatively few differentiated products. Dwyer et al. (1994) presents empirical evidence for Australia.
An exception can be identified in the early 1980s. This period coincides with a resources investment boom, promoted by the second OPEC oil-price shock and provides a good example of the role that expectations can play in determining movements in the exchange rate. The resources boom generated optimistic expectations about future improvements in the terms of trade and thereby, future income; the TWI appreciated despite little change in the prevailing terms of trade. Given that the anticipated improvements never eventuated, a correction in expectations contributed to the magnitude of the real TWI depreciation over 1985 and the first half of 1986.

Secondly, Australia experienced a rapid and sustained rise in net foreign liabilities over the 1980s (Figure 4)⁹. Increasing net foreign liabilities, as a share of wealth, require larger balance of trade surpluses to restore equilibrium. Similar to the macro model mechanism of maintaining external balance, this may require a depreciation of the real exchange rate to attract resources into the tradables sector (of course, if the real return on investment is high, the higher trade surpluses may be achieved without a real depreciation).

![Figure 4](image)

**Australia's net foreign liabilities**

As a percentage of GDP

Thirdly, the vast majority of the literature finds that the long-term real interest differential has the most success in obtaining significant and correctly signed estimates in exchange rate equations (Gruen and Wilkinson (1991) and BW for Australia; Isard (1988) and Shafer and Loopesko (1983) for international evidence). Long-term interest differentials are often justified on the grounds that shocks to the real exchange rate can persist for long periods and this slow reversion towards equilibrium is simply more appropriately matched by a correspondingly long-term interest rate¹⁰.

---

⁹ Empirical work generally uses the cumulated current account deficit as a proxy for net foreign liabilities because it abstracts from valuation effects.

¹⁰ Isard (1983) supports the use of long (10 year) interest rate differentials on the grounds that they are convenient to interpret. As in the Australian macro models, he assumes that the expected real exchange rate in 10 years time is the equilibrium exchange rate; in this way, the long (10 year) real interest differential (corrected for any risk premium) can be interpreted as denoting the annual rate of real depreciation/appreciation of the dollar expected by the market over the next 10 years.
This seems curious given that the exchange rate is considered to be an important channel for transmitting changes in the policy-determined short-term interest rate to the economy. De Kock and Deleire (1994) estimate that, post-1982 in the United States, the exchange rate accounts for roughly one-third of monetary policy transmission to output, compared to a near-negligible contribution earlier. Perhaps it is the case that previous Australian studies did not have the benefit of a sufficiently long sample period, after the floating of the Australian dollar, over which to estimate their exchange rate models. At any rate, this seems to beg further investigation.

The real long-term interest differential in existing models could simply be replaced by a real short-term interest differential. As customarily measured - using 12 months ended inflation rates - real short-term interest rate differentials would reflect the prevailing stance of domestic, relative to foreign, monetary policy; but they would fail to capture any market anticipation of the future paths of short-term interest rates, inflation and growth.

![Figure 5: Episodes of policy change](image)

It is difficult to capture these forward-looking aspects in behavioural models. This seems unsatisfactory in models of the exchange rate since financial market behaviour is generally characterised by forward-looking expectations. Therefore, the novel approach taken here is to use a
measure of the relative slopes of the domestic and foreign yield curves. Estrella and Mishkin (1995) and Mishkin (1994) provide evidence that the slope of the yield curve contains information about the current and expected future stance of monetary policy\(^\text{11}\). Inflationary expectations, and therefore expectations of the future path of short-term interest rates, are reflected in long bond yields. Although well-understood by policymakers, it is worthwhile digressing to illustrate this operational point further.

Figure 5 depicts two episodes of monetary policy action in Australia. Between April and December 1987 (top panel) and from December 1990 to March 1992 (bottom panel), the operational instrument of monetary policy in Australia - the nominal cash rate - was reduced by around 5 percentage points. In the first episode, in 1987, the long bond yield remained relatively unchanged (falling by a small 0.48 of a percentage point). By comparison, over the early 1990s episode, the long bond yield fell by almost 4 percentage points. At this time, some progress on inflation was already widely apparent in Australia and so market expectations for future inflation may well have moderated with the reduction in the cash rate. To the extent that this explains the fall in the long end of the yield curve, agents were not expecting short-term rates to have to rise very much in the future. Relative to the example in 1987, the slope of the yield curve remained fairly flat. By this measure, the stance of monetary policy was relatively tighter than over the 8 months to December 1987, despite equivalent movements in the nominal cash rate.

Also of interest to policymakers is the role of fiscal policy in determining exchange rate behaviour. Rarely mentioned in earlier work on the Australian exchange rate, the impact of fiscal policy can occur through two separate channels and is theoretically ambiguous:

- Firstly, the simplest *Mundell-Fleming* model predicts that expansionary fiscal policy causes an appreciation of the exchange rate. The intuition for this result is that increased government spending raises demand for domestic output which, in turn, induces a currency appreciation (alternatively, increased demand exerts upward pressure on interest rates which induces capital inflow and a stronger currency). The appreciated currency reduces the value of foreign demand, which restores the original level of output.

- Secondly, fiscal policy can impact upon the exchange rate through a risk premium. Fiscal expansion may be penalised by investors who perceive an increased probability of default or expect higher inflation in the future because they believe that the incentive exists for the Government to "inflate" its debt away; in order to hold Australian dollar assets, they demand a risk premium on domestic interest rates. Furthermore, it is often argued that higher government budget deficits are associated with negative sentiment on the exchange rate because they imply lower national savings and thus greater net foreign liabilities in the longer run. In this way, it is argued that the exchange rate depreciates. To the extent that the negative sentiment arises because of the overall size of net foreign liabilities, rather than their public/private composition, this effect may be partly captured, over the long run, by a cumulated current account variable.

Both the monetary and fiscal policy variables discussed above seem likely to be important, in addition to the variables identified in earlier work, for explaining movements in the Australian real exchange rate. To ascertain the empirical validity of this proposition, the BW equation, being the most recent in this literature, is tested for and appears to suffer from omitted variable bias.

---

\(^{11}\) See also Cook and Hahn (1990) for a survey of the more recent literature and some support for the idea that parts of the yield curve are useful in forecasting interest rates; Lowe (1992) provides evidence for Australia.
Table 1 summarises the results from application of the "rainbow test", a member of the Ramsey (1969) RESET family of tests for the omission of unknown variables (Utts (1982)\textsuperscript{12}). The test is conducted over several post-float sample periods, when the exchange rate became a channel of transmission for monetary policy; the null hypothesis of no omitted variables is consistently rejected. The omitted variable(s) will be captured in the error process and as a consequence, the estimated coefficients in the BW equation will be both biased and inconsistent.

### Table 1

<table>
<thead>
<tr>
<th>BW equation</th>
<th>RESET Rainbow test</th>
<th>Significance level</th>
</tr>
</thead>
<tbody>
<tr>
<td>1984:1–1992:3 (BW original estimation period)</td>
<td>3.11**</td>
<td>F(18.10) 0.035</td>
</tr>
<tr>
<td>1984:1–1995:2 (Update of BW estimation period)</td>
<td>2.61**</td>
<td>F(24.16) 0.026</td>
</tr>
<tr>
<td>1985:1–1995:2 (This paper's estimation period)</td>
<td>2.02*</td>
<td>F(22.14) 0.089</td>
</tr>
</tbody>
</table>

\*\*, \* Denote the null hypothesis of no omitted variables rejected at the 5% and 10% significance level respectively.

In an effort to address this bias, several modifications to the BW specification are made. Specifically, the terms of trade and cumulated current account deficit are retained. A yield gap differential \( YGAP \) replaces the long-term interest differential and takes the form:

\[
YGAP = \left( i_s - i_L \right) - \left( i_s - i_L^* \right) \]

(1)

where:

\( i_s - i_L \) : measures the slope of the domestic yield curve as the difference between the domestic nominal cash rate \( i_s \) and the domestic nominal long (10-year) bond yield \( i_L \);

\( i_s - i_L^* \) : measures the slope of the foreign yield curve using equivalent foreign interest rates (see Appendix A for details on the construction of world interest rates and Table B.2 in Appendix B for statistical confirmation of the implied restrictions in (1)).

In addition, a role for fiscal policy is accommodated by including a measure of the change in the Commonwealth Government budget balance, expressed as a proportion of GDP (hereafter, the fiscal variable). While it would be preferable to use a cyclically-adjusted measure of the fiscal position, this was not available for Australia\textsuperscript{13}.

---

\textsuperscript{12} The "rainbow test" compares estimates of the variance of the regression disturbance obtained from estimation over the full post-float sample and a truncated sub-sample; if the null hypothesis is true, both variance estimates are unbiased. The test statistic is an F-statistic, adjusted for the appropriate degrees of freedom. See Kmenta (1990, pp.454-455) for a full description of the test. It should be noted that the consequences of omitting relevant explanatory variables are the same as those of using an incorrect functional form.

\textsuperscript{13} Typically, the government budget tends to be in surplus when the economy is growing strongly and vice versa. The fiscal variable was tested against domestic and foreign growth variables and measures of the output gap to eliminate the possibility that it was just proxying the economic cycle. The fiscal variable retained its explanatory power over both the shorter post-float period (1985:1–1995:2) and the longer, historical sample period (1973:4–1995:2).
2.2 The empirical results

Following the convention for time series methodology, the order of integration of the real exchange rate and its proposed explanatory variables is established (see Table B.3 in Appendix B for detailed statistics). To this end, the Augmented Dickey-Fuller (Dickey and Fuller (1981); Said and Dickey (1984)) and Elliot, Rothenberg and Stock (1992) (DF-GLS) tests of a unit root null, together with the Kwiatkowski, Phillips, Schmidt and Shin (1992) (KPSS) test of a stationary (trend stationary) null, are employed\(^ {14}\). Confirming the results of Bleaney (1993) and Gruen and Kortian (1996), these tests imply mean reversion of the Australian real exchange rate to a slowly declining trend\(^ {15}\). Similar evidence of stationarity exists for other countries (see, for example, Phylaktis and Kassimatis (1994); Liu and He (1991); Huizinga (1987)\(^ {16}\)). The integration tests also provide evidence that the terms of trade and other explanatory variables are I(0) processes.

Nevertheless, the analytical convenience of the unrestricted error correction framework is exploited to specify a behavioural model of the real Australian TWI exchange rate\(^ {17}\). The model is specified with 4 lags of each explanatory variable in the dynamics; sequential F-tests are used to derive the following parsimonious representation:

\[
\Delta rer_t = \alpha + \beta rer_{t-1} + \delta tot_{t-1} + \phi cad_{t-1} + \gamma YGAP_t + \sum_{i=0}^{1} \phi_i \left[ \Delta Def/GDP_{t-i} \right] + \theta tot_t + \varepsilon_t \tag{2}
\]

where:
- \(rer\) : log Australian real TWI exchange rate;
- \(tot\) : log terms of trade;
- \(cad\) : log cumulated current account deficit, expressed as a proportion of GDP (defined such that a current account deficit is a positive number);
- \(YGAP\) : relative slopes of domestic and foreign yield curves as described in (1) above;
- \((\Delta Def/GDP)\) : fiscal variable, defined as the log change in the Commonwealth Government deficit and expressed as a proportion of GDP (defined such that a budget deficit is a positive number);
- \(\varepsilon\) : white noise error term;
- \(\Delta\) : first difference operator.

\(^{14}\) The null hypothesis of a unit root in the ADF and DF-GLS tests may result in a type II error; series may appear to contain a unit root because the data are insufficient to provide strong evidence for rejection of that null. This is why the KPSS test, with a null of stationarity, is also applied (see Appendix B for a brief description of this test).

\(^{15}\) From the perspective of modelling, the essential difference between the trend-stationary and integrated model specifications is the nature of the process driving the stochastic component, and whether the series is trended.

\(^{16}\) Phylaktis and Kassimatis (1994), in examining real exchange rates in eight Pacific Basin countries (calculated using the unofficial black market exchange rates), find evidence for mean reversion which suggests a half-life of four quarters. Using amended variance ratio tests, Liu and He (1991) offer evidence that mean reversion is quicker in the developing Asian countries relative to industrialised countries. Huizinga (1987) employs spectral methods to analyse real exchange rates for ten major currencies vis-à-vis the US dollar. Various real bilateral rates against the US dollar and the pound sterling were found to be mean-reverting, but against the Japanese yen, the exchange rates were indistinguishable from random walks.

\(^{17}\) In this way, the analysis recognises that in finite samples, any trend stationary process is nearly observationally equivalent to a unit root process where shocks are substantially reversed - that is, where the errors have a moving-average component with a root near minus one (or a fat-tailed distribution for the error process). And, irrespective of the order of integration of the variables, this modelling technique remains valid.
Given the time-series properties of the data, this specification is used to distinguish different types of influences on the real exchange rate and, in this way, retains one characteristic of the macroeconomic models described in Section 1 - namely, the general framework wherein the real exchange rate - affected by speculative and cyclical factors - eventually tends towards a path determined by underlying structural factors. The macroeconomic fundamentals, identified in Section 2.1 above, set the parameters within which the exchange rate should move in the short to medium term and provide a pertinent framework from which to assess the appropriateness of policy settings.

Table 2
Real exchange rate model
Dependent variable: change in log real TWI

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>β: Speed of adjustment(^1)</td>
<td>-0.51*** (0.12)</td>
<td>-0.25*** (0.07)</td>
</tr>
<tr>
<td>δ: Terms of trade(_{t-1})</td>
<td>0.46*** (0.14)</td>
<td>0.22*** (0.07)</td>
</tr>
<tr>
<td>ϕ: Cumulated current account(_{t-1})</td>
<td>-0.01 (0.05)</td>
<td>-0.04** (0.02)</td>
</tr>
<tr>
<td>γ: Yield curve differential(_{t-1})</td>
<td>1.10*** (0.35)</td>
<td>0.08 (0.21)</td>
</tr>
<tr>
<td>(\sum \varphi_i; \sum_{i=0}^{1}) Fiscal(_{t-i})</td>
<td>-4.87*** (7.15)</td>
<td>-1.36*** (5.43)</td>
</tr>
<tr>
<td>θ: Δ Terms of trade(_t)</td>
<td>1.41*** (0.19)</td>
<td>0.89*** (0.16)</td>
</tr>
<tr>
<td>α: Constant</td>
<td>0.16 (0.31)</td>
<td>0.09 (0.25)</td>
</tr>
<tr>
<td>R(^2)</td>
<td>0.74</td>
<td>0.35</td>
</tr>
<tr>
<td>DW</td>
<td>1.53</td>
<td>1.88</td>
</tr>
<tr>
<td>ARCH(4) test</td>
<td>1.33 [0.86]</td>
<td>3.26 [0.52]</td>
</tr>
<tr>
<td>AR(4) test</td>
<td>5.48 [0.24]</td>
<td>5.19 [0.27]</td>
</tr>
<tr>
<td>Jarque–Bera normality test</td>
<td>2.28 [0.32]</td>
<td>2.40 [0.30]</td>
</tr>
<tr>
<td>Rainbow test</td>
<td>1.08 [0.45]</td>
<td>0.84 [0.72]</td>
</tr>
</tbody>
</table>

\(^1\) This speed of adjustment implies a half life of 1 quarter; this is not unreasonable given that the real exchange rate is trend stationary.

* ** *** denote significance at the 10, 5 and 1% level respectively.

Standard errors are in round brackets, probability values are in square brackets, and the F test statistic for the joint significance of the fiscal variable is in parentheses, {).
The model is estimated over two sample periods; three decades of data encompass two broad exchange rate regimes in which the dynamics of the real exchange rate are unlikely to be identical. With this in mind, results for the real TWI over the post-float period (1985:1-1995:2) and a longer, historical sample (1973:4-1995:2) are reported in Table 2.

Two points are worth noting immediately:

The model is estimated over two sample periods; three decades of data encompass two broad exchange rate regimes in which the dynamics of the real exchange rate are unlikely to be identical. With this in mind, results for the real TWI over the post-float period (1985:1-1995:2) and a longer, historical sample (1973:4-1995:2) are reported in Table 2.

- As expected, it is only after the floating of the Australian dollar that the exchange rate has played a role in channelling changes in real interest rates through to the broader economy.

- On the other hand, the cumulated current account deficit is only significant in explaining the real exchange rate over the fuller, historical sample period; this accords with its longer-run structural nature. Over this period, the level of Australia's net foreign liabilities is estimated to have exerted some downward pressure on the real exchange rate, but this has been of a relatively small order of magnitude; a 1 percentage point increase in net foreign liabilities to GDP, ceteris paribus, eventually leads to around 1/6 of a percentage point depreciation in the real exchange rate.

The remainder of this section concentrates on interpreting the results obtained from estimation of this model over the post-float period. Simple impulse response diagrams show the estimated impact of a change in each of the explanatory variables, ceteris paribus, on the real exchange rate.

As in Section 1.3, consider first a temporary monetary policy shock.

This is executed through a one percentage point (negative) steepening of the Australian yield curve relative to the foreign yield curve, maintained for 8 quarters. In response, the real exchange rate is estimated to appreciate by 2.2 percentage points; 76 per cent of the adjustment is complete after 2 quarters (Figure 6a). This gradual adjustment of the real exchange rate to a monetary policy shock is quite different to the "jump" response elicited in the macro model.

Secondly, similar to the results obtained by earlier work, a sustained one percentage point increase in the terms of trade eventually delivers a 0.9 per cent appreciation of the real Australian exchange rate (Figure 6b). This estimated response is almost double that returned by simulation of the macro model exchange rate equation in Section 1.3. While there is some uncertainty about the operation of the short-run dynamics, a literal interpretation of the behavioural model suggests that the real exchange rate could appreciate by as much as 1.4 per cent in an initial response to this shock.

---

18 The foreign exchange market is given one year after the floating of the Australian dollar in 1983:4 to overcome initial turbulence and establish its new regime; thus, estimation over the shorter sample period begins in 1985:1. If the entire period since the float is included in the estimation period (i.e. 1984:1) then a direct role for monetary policy is no longer significant at the 10 per cent level.

19 The foreign exchange market is given one year after the floating of the Australian dollar in 1983:4 to overcome initial turbulence and establish its new regime; thus, estimation over the shorter sample period begins in 1985:1. If the entire period since the float is included in the estimation period (i.e. 1984:1) then a direct role for monetary policy is no longer significant at the 10 per cent level.

20 It is worth noting that the relative yield gap variable outperforms (statistically) the alternative short-term real interest differential over this sample period (see Table B.4 in Appendix B for details).

21 This is the opposite of the BW result that the cumulated current account deficit is only significant over the shorter, post-float sample period and even then, that it is outperformed by a simple trend (see Table B.1 in Appendix B).
Figure 6

Real TWI exchange rate: impulse response

6a: Temporary 1% monetary policy shock – 1% steepening of domestic yield curve for 8 quarters

6b: Sustained 1% terms of trade shock

6c: Permanent 1% fiscal policy tightening – affected over 4 subsequent quarters
The magnitude of the estimated real exchange rate response to terms-of-trade shocks is something of a puzzle. Gruen and Kortian (1996) contend that this observed historical response results from inefficiency in the foreign exchange market. They demonstrate the existence of large and variable predictable excess returns to holding Australian assets over horizons of a year or more. This is interpreted as evidence of a relative scarcity of forward-looking foreign exchange market participants with an investment horizon of this length.

If this myopic behaviour does indeed prevails, participants in the foreign exchange market may not be adequately distinguishing between temporary, soon-to-be-reversed, shocks and longer, more sustained, shifts in the terms of trade. This would result in Australia's real exchange rate moving more tightly with the terms of trade than is consistent with perfectly forward-looking investor behaviour. While the smaller responses to temporary terms-of-trade shocks generated by the macro models is theoretically appealing, the presence of excess returns in the foreign exchange market undermines the predictions of UIP; this condition is the central relationship determining exchange rate outcomes in the macro models.

Figure 7
The real exchange rate model: dynamic simulation and out-of-sample forecast
Finally, over the full sample period (1973:4-1995:2), the average absolute value of annual changes in fiscal policy has been in the order of 1 per cent of GDP. The largest fiscal contraction occurred in the year to June 1988 and represented almost 1.7 per cent of GDP; the largest fiscal expansion occurred in the year to June 1992, representing 2.9 per cent of GDP. Movements of this magnitude are infrequent.

Given this historical profile, the fiscal policy shock illustrated in Figure 6c is a permanent contraction of the Commonwealth Government budget deficit by 1 percentage point of GDP. The shock is engineered through four quarters of 0.25 percentage point reductions in the ratio of the deficit to GDP. As discussed in Section 2.1 above, the theoretical effect of a fiscal policy change on the real exchange rate is indeterminate. But, consistent with the prediction from a standard Mundell-Fleming model, a permanent 1 percentage point fiscal contraction is here estimated to instantly depreciate the real exchange rate by around 2 percentage points, other things being constant.

To give some idea of the model's fit, Figure 7 compares the actual behaviour of the real Australian TWI exchange rate over the post-float period, with its predicted values from this model.
The top panel of Figure 7 plots the fitted values from the model when it is estimated using the post-float data set, 1985:1-1995:2. In sample, the model fits very well.

The bottom panel of Figure 7 presents the model's out-of-sample forecasts. These are obtained by re-estimating equation (2) using data to the December quarter of 1989 (or half the sample period). Subsequently, actual values of the exogenous variables are used to obtain one-step-ahead forecasts of the real exchange rate out to the end of the sample, 1995:2. Out-of-sample, the equation captures most of the actual movements in the real exchange rate and picks the major turning points in the early 1990s and again around the end of 1993.

It is also instructive to ascertain the model's interpretation of historical movements in the real exchange rate. To this end, using all the data over the post-float sample period (1985:1-1995:2), the model is simulated dynamically. Sub-periods of pronounced exchange rate movement are then identified. Over each of these periods, the change in the simulated value of the real exchange rate is calculated and decomposed into the contribution attributable to movements in the terms of trade and each of the policy variables (Figure 8).

The rapid depreciation of the real TWI to mid-1986 is overwhelmingly attributable to the falling terms of trade. Over the first half of this sub-period, despite a relatively steeper yield curve in Australia, the effect on the real exchange rate from the declining terms of trade dominated. While it is clear that relative monetary policy movements affect the real exchange rate, their contribution is often overwhelmed by other (temporary) factors.

A rising terms of trade was responsible for 65 per cent of the predicted appreciation of the real TWI over the remainder of the 1980s. The yield differential made some smaller contribution at the beginning of this period. Fiscal policy had little effect.

Between 1990 and end-1991, the real exchange rate was relatively stable, with downward pressure from the terms of trade largely offset by expansionary fiscal policy. Possibly reflecting expectations of domestic inflationary pressure, the yield differential as well as fiscal policy made some contribution to the depreciation of the dollar over 1992-1993. Most recently, the terms of trade have, once again, appeared to dominate.

The overwhelming importance of temporary terms-of-trade shocks for Australia's real exchange rate is a documentable historical fact. Nevertheless, this result appears at odds with standard economic theory and, as discussed above, the assumption of market efficiency.

3. A behavioural model of the Australian long-term interest rate

In contrast to the volume of literature on determinants of the exchange rate, work on modelling the behaviour of the Australian long bond yield is scarce. This paper takes Orr et al. (1995) as a starting point for its research; these authors provide a succinct yet comprehensive discussion of the determinants of real long-term bond yields for a panel of seventeen OECD countries, including Australia. By using the "fundamental" variables identified by Orr et al., this section develops a time-series equation for the Australian ex ante real long bond yield. Ex ante real rates are difficult to measure because inflation expectations are largely unobservable. In this regard, the paper takes two alternative approaches.

Firstly, expectations are assumed to be adaptive (backward-looking) so that the nominal long bond yield is deflated, in the customary way, using actual past inflation rates. The parsimonious specification of this model seems dependent on an inflation risk premium variable which has little appeal within this time-series representation.

---

22 These contributions do not sum to 100 per cent because the contribution from the dynamic specification of the model is not included.
An alternative approach is posited in Section 3.2. *Forward-looking* expectations are generated by estimation of a model that endogenises shifts between a high and a low inflation regime. This methodology seems particularly apt for Australia, where successful inflation reduction policies in the early 1990s have been accompanied by a discrete shift in existing survey measures of inflationary expectations. A single equation, time-series model for the real long bond yield deflated with this unconventional forward-looking inflationary expectations series, is well-behaved.

### 3.1 The real bond yield fundamentals in brief

I begin with the principle determinants of real long bond yields. Orr et al. list these determinants as the domestic rate of return on capital, the world real long bond yield, and various risk premia. They note that these risk premia are likely to depend on:

- the perceived degree of each country's monetary policy commitment to price stability. Recognising that the expectations of market participants may follow some adaptive process, they use the existing level of inflationary expectations, conditioned on some longer-run historical performance (the average rate of inflation over the preceding 10 years). In this way, movements in bond yields relative to changes in current inflationary expectations will depend on the weight that investors attribute to Australia's relatively poorer historical inflation performance;
- the expected sustainability of government fiscal and net external debt positions. Orr et al. measure these by the ratios of government budget positions and cumulated current account deficits, respectively, to GDP;
- some undiversifiable domestic portfolio risk associated with holding bonds

Following the time-series methodology outlined in Section 2, the real long bond yield, (r), deflated, first of all, with (annualised) quarterly underlying inflation rates, is determined by an unrestricted error correction model. Tests of the order of integration of each variable are presented in Table C.1 in Appendix C. Four lags of each of the differenced "fundamental" variables, together with domestic growth, were included in the initial dynamic specification of the model; F-tests were then used to derive the parsimonious final model:

\[
\Delta r_t = \alpha \Delta r_{t-1} + \beta \{ \pi_{10} - E_t(\pi) \} + \gamma_0 \text{RetCap}_{t-1} + \sigma \Delta r_{t-2} + \phi \Delta \text{RetCap}_{t-1} \\
+ \lambda_0 \Delta E_t \left[ \pi_{PF_t} \right] + \lambda_2 \Delta E_t \left[ \pi_{PF_{t-1}} \right] + \theta \Delta GDef_t + \sum_{i=0} g_{t-i} + e_t
\]

where:

- \( r_t \) : real Australian 10-year bond yield deflated with annualised quarterly underlying inflation rates;
- \( \{ \pi_{10} - E_t(\pi) \} \) : inflation differential variable;
- \( \text{RetCap} \) : return on capital;
- \( GDef \) : Commonwealth Government Budget deficit, expressed as a proportion of GDP (a deficit is denoted as a positive number);
- \( g \) : domestic GDP growth;

---

23 It may also be the case that some degree of liquidity risk exists for Australia, due to a relatively shallow bond market.

24 Annualised quarterly inflation rates are used to avoid the introduction of autocorrelation.
\[ \Delta \] difference operator;
\[ \varepsilon_t \] white noise error term.

The estimation results are presented in Table 3 (see Table C.2 in Appendix C for the full dynamics). Despite the richness of the Orr et al. cross-sectional specification, only the return on capital and the inflation credibility risk premium were found to be significant fundamental determinants of the Australian real bond yield in this time-series model.

<table>
<thead>
<tr>
<th>Explanatory variable</th>
<th>Coefficient</th>
</tr>
</thead>
<tbody>
<tr>
<td>Speed of adjustment parameter</td>
<td>-0.513***</td>
</tr>
<tr>
<td></td>
<td>(0.10)</td>
</tr>
<tr>
<td>Return on capital</td>
<td>0.164***</td>
</tr>
<tr>
<td></td>
<td>(0.04)</td>
</tr>
<tr>
<td>Inflation term: ( (\pi_t - E_{t}(\pi)) )</td>
<td>0.256***</td>
</tr>
<tr>
<td></td>
<td>(0.08)</td>
</tr>
</tbody>
</table>

\[ \bar{R}^2 \] .......................... 0.60
\[ DW \] ................................ 1.76
ARCH test \[ \chi^2 \] .......................... 0.882
\[ \chi^2 \] ................................ 3.28
Jarque–Bera normality test \[ \chi^2 \] .............. 0.96

\* \* \* \* \* denote significance at the 10, 5 and 1\% level respectively. Standard errors are in parentheses, probability values are in square brackets.

A one percentage point rise in the domestic return on capital in this model implies an eventual increase in the real long bond yield of about 1/3 of a percentage point; this compares to around 1/4 of a percentage point in the Orr et al. estimation. While the inflation differential variable has some appeal for estimation with panel data, its appropriateness within this time-series framework is difficult to justify. This is because, by construction, the real bond yield will often be relatively high in periods when the current (expected) rate of inflation is low; this will also be true of the inflation variable. That is, the existence of some mean reversion in inflation would generate this positive, significant coefficient.

The fit of the model is represented in the top panel of Figure 9. Out-of-sample forecasts are obtained by estimating the model to December 1991; actual values of the exogenous variables are then used to forecast the real long bond yield forward through time. The results are presented in the lower panel of Figure 9. The model predicts the fall in the real long bond yield over the early 1990s and its trough in 1993. However, it fails to anticipate the extent of the rise in the real bond yield over the course of 1994, suggesting, perhaps, that the world-wide bond market sell-off was not completely consistent with fundamentals. Despite the fact that a similar pattern was documented in most OECD
countries over 1994, the panel estimation in Orr et al. also fails to predict bond yield behaviour over this period.

Figure 9
Real long bond yield model: simulation and out-of-sample forecast

Given the reservations with the model's (likely spurious) dependence on the inflation differential term, \((\pi_{i0} - E_i(\pi))\), it may be the case that the dependent variable, measured as it is, with backward-looking inflationary expectations, is not an adequate measure of the ex ante real long bond yield. The remainder of this section explores an alternative real long bond yield model that assumes inflation expectations to be forward looking.

3.2 Measuring inflationary expectations

The gap between nominal and indexed 10-year bond yields is often used to estimate financial market expectations of the average rate of inflation over the next 10 years. However, in Australia's case, the indexed bond market has only very recently become liquid; historically, indexed
bonds were held in concentrated parcels and were not actively traded in a secondary market at all until 1993. An alternative measure of inflationary expectations is available from the Westpac Bank and the Melbourne Institute. A random selection of 1,200 adults aged 18 and above, sampled Australia-wide, are asked to respond to a question about how much they expect prices to rise over the next twelve months; their responses are weighted to reflect population distribution. The disadvantage of this survey series is that it asks about inflationary expectations over the next 12 months - not over the next 10 years. Perhaps more importantly, the expectations of consumers might differ from those of financial market participants (Figure 10).

**Figure 10**

Survey measure of inflationary expectations and the nominal 10-year bond rate

\[
\begin{align*}
\text{Survey expectations (RHS)} & \\
\text{10 year bond rate (LHS)} & \\
\end{align*}
\]

This paper proposes a different approach to measuring expectations which exploits the Markov switching technique and endogenises shifts in the inflation process through time\textsuperscript{25}. In brief, this methodology allows the process of inflation to be characterised by two different regimes, the first identified by relatively high inflation; the second, by relatively low inflation. Switches between these states are based on a probabilistic process\textsuperscript{26}. Maximum likelihood estimation of the two-state model returns a probability that inflation is in one or other of these regimes. This is used to construct a probability-weighted \(n\)-period-ahead inflationary expectations series which is, by its nature, forward-looking. Thus constructed, this series is found to be superior to its survey alternative in a model of the nominal bond yield (Section 2.3).

More specifically, inflation is specified to depend on its own past values and forward-looking measures of the output gap (itself measured by a Hodrick-Prescott filter on GDP(A)). Three forecasting methods are tried:

---

\textsuperscript{25} Initial work with Markov switching models was done by Hamilton (1989, 1990) with applications to business cycles. Recent work by Evans and Wachtel (1993) and Laxton, Rickets and Rose (1994) (and Simon and Tarditi (1995, mimeo) for Australia) has applied the technique to inflation with a view to examining the issue of central bank credibility. The Gauss programme used for estimation of the Markov switching model is an adaptation of that used by Hamilton (1989) and Goodwin (1993) and I thank Thomas Goodwin for generously providing me with the computer code.

\textsuperscript{26} A Markov process is one where the (fixed) probability of being in a particular state is only dependent upon what the state was last period.
First, agents are assumed to have perfect foresight so that they know the output gap existing in the period over which their inflationary forecast is relevant. In this case, the probability-weighted inflationary expectations series is a function of lagged inflation and the actual future output gap (and is denoted $E_{PF_i}(\pi_{t+n})$ for perfect foresight Markov measure):

$$E_{PF_i}(\pi_{t+n}) = f\{\pi_{t-i}, GAP_t+i\}; i = 0,1,2,...,n-1$$

In this way, inflationary expectations over the next year ($n=4$ quarters) would be $E_{PF_i}(\pi_{t+4})$; over the next 10 years, $E_{PF_i}(\pi_{t+40})$.

Alternatively, the assumption of perfect foresight can be relaxed so that inflationary expectations are a function of lagged inflation and a mean-reverting output gap (and this measure is denoted $E_{MR_i}(\pi_{t+n})$ for mean-reverting Markov measure):

$$E_{MR_i}(\pi_{t+n}) = g\{\pi_{t-i}, GAP_t+i\}; i = 0,1,2,...,n-1$$

where:

$$GAP_{t+i} = GAP_{t-1}\left(1 - \frac{i+1}{n}\right)$$

In this way, $n=4$ quarters is roughly consistent with a 4 to 5 year business cycle; at any point in time, $t$, the output gap is not known (although $GAP_t$ is known), but is expected to close within 5 quarters.

Finally, since similar analysis in the literature has commonly been univariate, the output gap is excluded altogether (this worsens the fit of the model but leaves the general dynamics relatively unchanged).

Quarterly data from the past 35 years (1959:4-1995:2) are used to estimate the model parameters with maximum likelihood techniques. For convenience, only the results from estimation of the first specification, $E_{PF_i}(\pi_{t+n})$, which assumes perfect foresight of the output gap, are presented below. State 0 identifies the 1970s and 1980s as episodes of relatively high inflation in Australia and the estimated model describes underlying inflation as a persistent (but not integrated) process around a mean of 8.7 per cent. State 1 identifies the 1960s and 1990s as low inflation regimes where shocks are less persistent and inflation reverts to a mean of 3.3 per cent.

**State 0: High inflation regime**

- $\pi_t^0 = 0.40 + 0.8\pi_{t-1} + 0.09GAP_{t-1} + \varepsilon_t^0$
  
  - Mean: 0.40
  - Coefficient: 0.8
  - Coefficient: 0.09
  - Coefficient: 1
  - Coefficient: 0.03

- $\varepsilon_t^0 = z \cdot 1.04\sqrt{\sigma_t}$

- $p(s_t = 0|s_{t-1} = 0) = 0.989$

- $z \sim N(0,1)$

**State 1: Low inflation regime**

- $\pi_t^1 = 0.54 + 0.34\pi_{t-1} + 0.11GAP_{t-1} + \varepsilon_t^1$

- Mean: 0.54
- Coefficient: 0.34
- Coefficient: 0.11
- Coefficient: 1
- Coefficient: 0.03

- $\varepsilon_t^1 = z \cdot \sqrt{\sigma_t}$

- $p(s_t = 1|s_{t-1} = 1) = 0.980$

- $\sigma_t^2 = 0.14 + 0.47\varepsilon_{t-1}^2$

- Coefficient: 0.14
- Coefficient: 0.47
- Coefficient: 0.03
- Coefficient: 0.20
Figure 11 illustrates the probability of being in the high inflation state, 0, at each point in time. It is this series which is used to appropriately weight one-step-ahead forecasts from the inflation models of state 0 and state 1 to construct what will be referred to as the "Markov inflationary expectations series". This approach has two advantages. It explicitly incorporates the forward-looking behaviour customarily associated with financial market participants and assumed in the macro model approach. Furthermore, this method can deliver a longer-horizon measure of inflationary expectations, n periods ahead, as per (4) or (5). These n-step-ahead estimates embody more realistic, behavioural processes than the simple log linear interpolated values used in the macro models. Expectations 2 years ahead, as well as 1 year ahead, are calculated.

![Figure 11](image)

It is clear from Figure 12 that the behaviour of the Markov expectations series is quite distinct from that of the consumer survey measure. For exposition, only the Markov 1-year-ahead inflationary expectations, generated by agents with perfect foresight of the output gap, $E_{PF}(\pi_{t+4})$, are illustrated in Figure 12. The alternative, mean-reverting output gap specification and the 2-year-ahead forecasts of Markov expectations exhibit similar patterns and timing.

3.3 Empirical results for the long bond yield equation with forward-looking inflationary expectations

The relevance of the various Markov forward-looking expectations series, in contrast to the survey measure of consumer expectations, is examined for explaining movements in the nominal bond yield. This is achieved by estimating an unrestricted ECM of the form:

$$i_t = \alpha \hat{E}_1(\pi_{t+40}) + \gamma Z + \theta \Delta X + \epsilon_t$$

(6)
where:

\[ i_t \quad : \quad \text{nominal 10-year bond yield;} \]

\[ \hat{E}_t(\pi_{t+40}) \quad : \quad \text{estimated average rate of inflation expected over the next 10 years proxied either by one of the Markov measures of inflation expectations or the consumer survey measure;} \]

\[ Z \quad : \quad \text{vector of explanatory variables for the real 10-year bond yield as described by Orr et al. (1995) and discussed in Section 3.1 above;} \]

\[ X \quad : \quad \text{vector of dynamics;} \]

\[ \varepsilon_t \quad : \quad \text{white noise error term.} \]

Four lags of each of the differenced explanatory variables were initially included in the dynamic specification of the model; F-tests were then used to derive the parsimonious final model. Table 4 summarises the results from estimation of (6) using the competing measures of \( \hat{E}_t(\pi_{t+40}) \).

Figure 12

Alternative measures of inflationary expectations

The Markov one-year-ahead inflationary expectations measure, calculated using the assumption of perfect foresight for the output gap, \( E_{PF}(\pi_{t+1}) \), was found to have the greatest explanatory power for movements in the nominal long bond yield (model #1); it clearly outperforms the survey measure (model #3). The alternative Markov measure, based on an assumption of mean-reversion in the output gap, rather than perfect foresight, but with an equivalent 1-year forecast horizon, \( E_{MR}(\pi_{t+1}) \), also performed better than the survey measure; however, in this equation, model #2, the real long foreign bond yield became insignificant. Two-year-ahead Markov expectations in models #3 and #4 were slightly less significant; the foreign long bond yield was insignificant in these equations as well.
Table 4  
Australian nominal long bond yield equation  
Dependent variable: $\Delta r$  

<table>
<thead>
<tr>
<th>Model #</th>
<th>Measure of $E_t(\pi_{t+n})$</th>
<th>$\beta$ (t-stat)</th>
<th>Speed of adjustment $\gamma_0$ (t-stat)</th>
<th>$\gamma_1$ (t-stat)</th>
<th>$R^2$</th>
<th>(p-value)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$E_{PF}(\pi_{t+4})$</td>
<td>0.204 (4.80)</td>
<td>-0.241 (4.36)</td>
<td>0.079 (2.68)</td>
<td>0.13 (1.90)</td>
<td>0.332</td>
</tr>
<tr>
<td>2</td>
<td>$E_{MR}(\pi_{t+4})$</td>
<td>0.223 (4.10)</td>
<td>-0.226 (4.38)</td>
<td>0.083 (2.97)</td>
<td>-</td>
<td>0.284</td>
</tr>
<tr>
<td>3</td>
<td>Survey</td>
<td>0.262 (3.09)</td>
<td>-0.299 (3.47)</td>
<td>0.083 (2.31)</td>
<td>-</td>
<td>0.271</td>
</tr>
<tr>
<td>4</td>
<td>$E_{PF}(\pi_{t+8})$</td>
<td>0.091 (2.05)</td>
<td>-0.065 (2.95)</td>
<td>-</td>
<td>-</td>
<td>0.216</td>
</tr>
<tr>
<td>5</td>
<td>$E_{MR}(\pi_{t+4})$</td>
<td>0.245 (3.21)</td>
<td>-0.210 (3.61)</td>
<td>0.066 (2.33)</td>
<td>-</td>
<td>0.214</td>
</tr>
</tbody>
</table>

The remainder of this section concentrates on the results obtained from model #1's specification (see Table C.3 in Appendix C for the full estimated dynamics):

$$
\Delta_i = \alpha_i t_{i-1} + \beta \left[ E_{PF}(\pi_{t+4}) \right]_{i-1} + \gamma_0 \text{RetCap}_{t-1} + \gamma_1 r^*_{t-1} + \sum_{j=0}^{2} \sigma_j \Delta_i t_{i-1} + \phi \left[ E_{PF}(\pi_{t+4}) \right]_{i-1} + \psi g_{t-3} + \epsilon_i
$$

where:

- $i_t$ : nominal Australian 10-year bond yield;
- $E_{PF}(\pi_{t+4})$ : Markov model estimates of inflationary expectations as defined in (4) above or consumer survey measure;
- $\text{RetCap}$ : return on capital;
- $r^*$ : US real 10-year bond rate;
- $g$ : domestic GDP growth;
- $\Delta$ : difference operator;
- $\epsilon_i$ : white noise error term.

Full-sample predictions from this very simple nominal long bond yield equation fit the actual data very well (Figure 13). As in Section 3.1, out-of-sample forecasts were obtained by estimating the model to December 1991; actual values of the exogenous variables were then used to forecast the nominal long bond yield forward in time. The model anticipates the turning point in bond
yields in late 1993 as well as their subsequent pick-up over 1994, presumably because it contains the foreign bond yield \( r^* \); the other models did not.

The null hypothesis in the final column of Table 4 tests whether the Fisher Hypothesis holds, such that movements in inflationary expectations are matched one-for-one by movements in the nominal interest rate. This restriction is necessary for valid reparameterisation of model #1 (equation (7)) as a real bond yield equation; the null hypothesis could not be rejected. Trivially, additional restrictions are also accepted such that this model, re-estimated as a real bond yield equation, delivers the same parameter estimates on the \( Z \) variables.

In this way, while equation (3) in Section 3.1, presented a model of the real 10-year bond yield, deflated with backward-looking expectations, equation (7) provides an alternative model which derives real yields by using a forward-looking Markov measure of expectations and has the following main features:
the Australian nominal long bond yield reacts to a change in inflationary expectations with a lag (bottom panel of Figure 14). In contrast, a permanent 1 percentage point rise in the US real long bond rate, *ceteris paribus*, causes the Australian real long bond yield to react instantaneously; by the second quarter after the shock, the domestic long bond yield would be around 0.54 of a percentage point higher (panel 2, Figure 14; this is larger than the 0.30 of a percentage point implied by the Orr et al. cross-section estimates for Australia).

consistent with the result obtained from estimation of equation (3), a permanent 1 percentage point improvement in the return on Australian capital raises the domestic real yield by around 1/3 of a percentage point; this response occurs more slowly than that estimated for a change in the US real rate (panel 1, Figure 14).

Further research could investigate the possibility of including elements of both forward- and backward-looking expectations within a model of Australian bond yields.

Figure 14

Bond yield responses to permanent 1% shocks to:
Conclusion

There is no single, simple conclusion to be drawn from this research but rather, a series of points can be made.

Interest rates and exchange rates now form part of the transmission mechanism by which policy changes feed through to the broader economy. Expectations play a critical role in this mechanism, affecting both the timing and speed of transmission. Theoretical discussions of interest rate and exchange rate markets typically characterise expectations as forward looking. However, it has been difficult to model this type of behaviour within an empirical framework.

One approach has been to rely on the relevant components of full-scale, intertemporal macroeconomic models. These models embody theoretically consistent long-run properties and rational forward-looking expectations. In Australia, such exchange rate and bond yield equations are not estimated; they reflect orthodox theoretical considerations including uncovered interest parity and the term structure hypothesis. But the textbook-style results produced by these macro-models have limited relevance for practical policymaking.

Alternatively, single equation, behavioural models can be used to document the observed historical relationships in the data. These have typically assumed that expectations are formed adaptively, that is, are backward looking. The research in this paper concentrates on introducing a forward-looking element into behavioural models of the Australian real exchange rate and long bond yield.

Given that expectations play a central role in determining the responses to various shocks, the macroeconomic and behavioural model approaches are probably best distinguished by a comparison of impulse response functions. In particular, these two methodologies provide different characterisations of the behaviour of the real exchange rate. In the macro model framework, monetary policy shocks elicit an instantaneous change in the real exchange rate which is subsequently and gradually unwound. In contrast, the behavioural model does not return this instantaneous "jump" response. Instead, the real exchange rate only gradually transmits a change in monetary policy through to the broader economy so that the full impact of the policy change through this channel is felt with a lag. Despite very different adjustment paths, both models produce final responses of a similar order of magnitude.

On the other hand, about half of a sustained terms-of-trade shock is finally passed through to the real exchange rate in the macro models; this occurs through an initial jump in the exchange rate, followed by gradual adjustment towards the long run. While this result is theoretically appealing, it does not describe the actual behaviour of the Australian real exchange rate. The behavioural model estimates that the real exchange rate moves much more closely with terms-of-trade shocks, regardless of whether the shocks are temporary or sustained over very long periods. Some overshooting is estimated to occur immediately. This result is puzzling but it is consistent with the idea that agents in the foreign exchange market have only a relatively short horizon. The inherent difficulty of incorporating inefficient mechanisms into the macro model framework may be one source of the disparity between the macro model results and those recorded by the behavioural models.

Incorporating forward-looking behaviour into a bond yield equation is less straightforward. In this paper, it is achieved by explicitly modelling the formation of inflation expectations. Expectations are generated from a series of assessments about the probability of shifting between a high and a low inflation regime. This is particularly apt in Australia, since a discrete shift in inflationary expectations occurred in the early 1990s. The superior performance of the shorter horizon expectations suggests that some myopia may exist in this market as well. Further work in this area might consider whether there are roles for both forward and backward-looking elements within the model.
Appendix A: Data sources

The data for Section 2 of the paper were collected for the period from September 1973 to June 1995. The data for Section 3 were collected for the period from December 1979 to June 1995. All indexes are based to 1989/90 = 100. This Appendix lists each of the variables used in the paper together with their method of construction and original data source(s).

Real exchange rate
Index.
Reserve Bank of Australia.

Terms of trade
Index; seasonally adjusted; goods and services measure.
The terms of trade was spliced to the goods and services trend measure at September 1974.
Australian Bureau of Statistics, Catalogue 5302.0, Table 9.

Nominal gross domestic product (GDP)
Millions of A$; seasonally adjusted; income measure.
Australian Bureau of Statistics, Catalogue 5206.0.

Real gross domestic product
Average measure.
The growth variable is the quarterly growth of real GDP.
Australian Bureau of Statistics, Catalogue 5206.0.

Cumulated current account
Current account balance; millions of A$; seasonally adjusted.
The cumulated current account for each quarter is calculated as the cumulative sum of quarterly current account balances from September 1959 and taken as a proportion of annualised GDP:

\[ \sum_{t=1}^{4} \text{current account}_t / (GDP \times 4) \]
Australian Bureau of Statistics, Catalogue 5302.0, Table 3.

Net foreign liabilities
Net international investment position at end of period; millions of A$; not seasonally adjusted.
Annual data for the period June 1974 - June 1985, quarterly data afterwards; expressed as a proportion of annual GDP.
June 1974-June 1978: Reserve Bank of Australia Occasional Paper No. 8;
June 1979-June 1995: Australian Bureau of statistics Catalogue 5306.0, Table 1.

Fiscal
Commonwealth government budget balance.
The fiscal variable for the four quarters of each fiscal year is measured as the change in the annual Commonwealth government budget balance as a proportion of GDP, calculated on a quarterly basis.
Cash rate
Reserve Bank of Australia Bulletin, Table F1 and internal sources.

90-day bank bill
Reserve Bank of Australia Bulletin, Table F1 and internal sources.

10-year bond rate
Reserve Bank of Australia Bulletin, Table F2 and internal sources.

GDP in US dollars
Annual GDP for the United States, Canada and the United Kingdom, measured in millions of US dollars, are applied as weights in the construction of world variables. The UK measure of GDP is quarterly and is converted into an annual measure.

World short interest rates
The world short interest rate is calculated as the weighted arithmetic average of short interest rates (3-month Treasury bills) from the United States, Canada and the United Kingdom. Each country's GDP, measured in US dollars, are used as weights.

World long interest rates
The world long interest rate is calculated as the weighted arithmetic average of long interest rates for the above countries, with GDP in US dollars used as weights.

Real interest rates
Real interest rates for the exchange rate section are calculated by deflating the interest rate by a corresponding measure of four-quarter-ended inflation ie. \((1 + r_t / 1 + \pi_t) - 1\). For the bond yield equation, US long bond yields are deflated by quarter-ended inflation.

Australia: Treasury underlying price index. Commonwealth Treasury.
Canada: Underlying price index; Datastream code: cnd20833.
Consumption deflator. Datastream code: cnipdcone.
The underlying price index is spliced to the consumption deflator at March 1986.

United Kingdom: Underlying price index. Datastream code: ukrpiy..f.
Consumption deflator. Datastream code: ukipdcone.
The underlying price index is spliced to the consumption deflator at March 1987.

Yield differential
The yield differential is calculated as the difference between the Australian and world yield curves. The yield curve for Australia is measured as the difference between the cash rate and the 10-year bond rate. The world yield curve is measured as the difference between short and long nominal world interest rates.
Inflation
Treasury underlying rate.
Commonwealth Treasury.

Return on capital
The return on capital is measured as corporate GOS divided by gross capital stock.
Australian Bureau of Statistics catalogue 5206.0 and 5221.0.

Inflation expectations
Constructed from a Markov switching model using underlying inflation and an output gap. The output gap is calculated as the percentage deviation of nominal GDP(A) from a Hodrick-Prescott trend.

Survey
The survey variable is the Westpac/Melbourne Institute survey of consumer inflation expectations over the next four quarters.
Appendix B: The behavioural model of the Australian real exchange rate: integration tests and diagnostics

Table B.1
Testing the Blundell-Wignall et al. (1993) equation: cumulative current account deficit (CCAD) or trend?

<table>
<thead>
<tr>
<th>Model</th>
<th>1985:1-1995:2</th>
<th>Estimate coefficient¹</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>CCAD</td>
</tr>
<tr>
<td>Original specification - CCAD</td>
<td>-0.281</td>
<td>(-2.60*)</td>
</tr>
<tr>
<td>Adding a trend term</td>
<td>0.626</td>
<td>(1.49)</td>
</tr>
<tr>
<td>Replacing CCAD with a trend term</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

¹ Estimates are taken from the Bewley Transformation of an unrestricted error correction model; figures in parentheses denote t-statistics; * denotes significance at the 10% level.

Table B.2
Yield gap variable: testing the null of the validity of the implied restrictions

\[ YGAP = \gamma \left\{ (i_s - i_L) - (i_s - i_L)^* \right\} \]

<table>
<thead>
<tr>
<th>Sample period</th>
<th>Test-statistic</th>
<th>Significance level</th>
</tr>
</thead>
<tbody>
<tr>
<td>1985:1-1995:2</td>
<td>1.06</td>
<td>F(3,31)</td>
</tr>
<tr>
<td>1973:4-1995:2</td>
<td>0.77</td>
<td>F(3,76)</td>
</tr>
</tbody>
</table>

The DF-GLS test (Elliot et al. (1992)) is a modified version of the Augmented Dickey-Fuller (ADF) t-test, having the advantages that it exhibits superior power properties and suffers from only small size distortions in finite samples. The testing procedure involves demeaning or detrending the series using Generalised Least Squares and then running the ADF test regression using that series. The constant and time trend terms are omitted from the test regression. The t-statistic on (p-1) is then used to test for significance against the appropriate critical value. The demeaned case (DF-GLSH) is comparable to including a constant term in the ADF test; the critical values are taken from Fuller (1976) and the no-constant variant of the MacKinnon (1991) table. The detrended case (DF-GLS) is comparable to including a constant and a time trend in the ADF test; the critical values have been tabulated by Elliot et al. (1992).
Table B.3a

<table>
<thead>
<tr>
<th></th>
<th>$H_0$ : Non-stationarity</th>
<th>$H_0$ : Stationarity</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\Phi_3$</td>
<td>$\tau_t$</td>
</tr>
<tr>
<td>Real exchange rate</td>
<td>5.48*</td>
<td>-3.31*</td>
</tr>
<tr>
<td>Terms of trade</td>
<td>10.6***</td>
<td>-4.07***</td>
</tr>
<tr>
<td>Prices</td>
<td>8.33**</td>
<td>-2.32</td>
</tr>
<tr>
<td>Current account</td>
<td>7.44**</td>
<td>-3.86*</td>
</tr>
<tr>
<td>Debt</td>
<td>1.76</td>
<td>-1.87</td>
</tr>
<tr>
<td>Government deficit</td>
<td>6.97**</td>
<td>-3.71*</td>
</tr>
<tr>
<td>Yield gap</td>
<td>5.00</td>
<td>-3.15*</td>
</tr>
<tr>
<td>Yield gap*</td>
<td>5.01</td>
<td>-3.16*</td>
</tr>
</tbody>
</table>

Table B.3b

<table>
<thead>
<tr>
<th></th>
<th>$H_0$ : Non-stationarity</th>
<th>$H_0$ : Stationarity</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\Phi_3$</td>
<td>$\tau_t$</td>
</tr>
<tr>
<td>Real exchange rate</td>
<td>3.03</td>
<td>-2.36</td>
</tr>
<tr>
<td>Terms of trade</td>
<td>8.96**</td>
<td>-4.17***</td>
</tr>
<tr>
<td>Prices</td>
<td>6.67*</td>
<td>-1.99</td>
</tr>
<tr>
<td>Current account</td>
<td>6.13*</td>
<td>-3.43*</td>
</tr>
<tr>
<td>Debt</td>
<td>11.35***</td>
<td>-4.74***</td>
</tr>
<tr>
<td>Government deficit</td>
<td>6.61**</td>
<td>-3.31*</td>
</tr>
<tr>
<td>Yield gap</td>
<td>6.78**</td>
<td>-3.63**</td>
</tr>
<tr>
<td>Yield gap*</td>
<td>2.78</td>
<td>-2.29</td>
</tr>
</tbody>
</table>

*, ** and *** denote significance at the 10, 5 and 1% levels respectively. $\Phi_3$ refers to the likelihood ratio test of $(\alpha,\beta,\rho) = (\alpha,0,1)$ in $Y_t = \alpha + \beta t + \rho Y_{t-1} + \epsilon_t$. The critical values are from Dickey and Fuller (1981). $\tau$ refers to the Augmented Dickey Fuller (ADF) "t-tests"; $\tau_t$ includes a constant and trend and $\tau_p$ includes a constant only. The critical values are from Fuller (1976). DF-GLS $\tau$ and DF-GLS $\mu$ are a modified trend and constant versions, respectively, of the ADF tests proposed by Elliot, Rothenberg and Stock (1992). KPSS is a test proposed by Kwiatkowski, Phillips, Schmidt and Shin (1992) which tests the null hypothesis of stationarity. A truncation lag of 8 is used for the calculation of the estimate of the error variance.
The KPSS (1992) test is applied in the following way. All series can be written as the sum of a trend ($\xi_t$), a random walk ($r_t$), and a stationary component ($\varepsilon_t$) such that:

$$y_t = \xi_t + r_t + \varepsilon_t$$

where:  \[ r_t = r_{t-1} + u_t \]

If the series is stationary (that is, there is no random walk component), the variance of $u_t$ will be zero. The test statistic for the null hypothesis of no unit root is an LM statistic which is a function of the estimated residuals and an estimate of the long run error variance. These residuals are either the demeaned series ($n_m$) or the demeaned and detrended series ($n_t$). The critical values for these tests are detailed in Kwiatkowski, Phillips, Schmidt and Shin (1992), page 166.

These tests provide evidence over the full sample period (1973:4-1995:2) that the real exchange rate, terms of trade, interest differentials, yield gaps, current account deficit, government budget balance, and relative productivity differentials are I(0), with the first two series exhibiting this stationarity around a trend. These conclusions are also supported over the shorter sample period (1984:1-1995:2).

### Table B.4

**A comparison of the statistical significance of competing measures of interest rates in the real exchange rate equation**


<table>
<thead>
<tr>
<th>Interest differential term</th>
<th>Estimated coefficient</th>
<th>t-statistic (p-value)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\left{(i_t-i_s)-(i_t-i_s)\right}$</td>
<td>2.48</td>
<td>3.05 (0.00)</td>
</tr>
<tr>
<td>$r_t-r_s$</td>
<td>2.98</td>
<td>2.45 (0.02)</td>
</tr>
<tr>
<td>$(r_t-r_s)$ as per the BW equation</td>
<td>0.16</td>
<td>0.11 (0.91)</td>
</tr>
<tr>
<td>$(r_t-r_s)^2$</td>
<td>3.64</td>
<td>2.39 (0.02)</td>
</tr>
</tbody>
</table>

1 The real TWI exchange rate model is specified as a function of the terms of trade, the cumulated current account deficit, an interest differential term, and a fiscal policy variable.

2 The real long interest differential is here tested in the B-W specification which expresses the real TWI as a function of the terms of trade, the cumulated current account deficit as a proportion of GDP, and this real long interest rate differential.
Figure B.1
Real exchange rate model: equation (2)
Diagnostics

[CUSUM plot]

[CUSUM Squared plot]
Figure B.2
Parameter stability tests

%  

1 Standard deviation

%  

-2 86/87 88/89 90/91 92/93 94/95 -2

-1 

0 

1 

2 

3 

-1 86/87 88/89 90/91 92/93 94/95 -1
Appendix C: The behavioural model of Australian long bond yields: integration tests and diagnostics

Table C.1
Integration tests: 1979:4–1995:2

<table>
<thead>
<tr>
<th></th>
<th>$H_0$ : Non-stationarity</th>
<th>$H_0$ : Stationarity</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\Phi_1$</td>
<td>$\tau_\tau$</td>
</tr>
<tr>
<td>Real 10-year bond</td>
<td>10.51***</td>
<td>-4.37***</td>
</tr>
<tr>
<td>Real US 10-year bond</td>
<td>4.38</td>
<td>-2.94</td>
</tr>
<tr>
<td>Return on capital</td>
<td>6.29**</td>
<td>-3.53**</td>
</tr>
<tr>
<td>Cash rate</td>
<td>2.47</td>
<td>-1.96</td>
</tr>
<tr>
<td>Government deficit</td>
<td>5.14</td>
<td>-3.18*</td>
</tr>
<tr>
<td>Undiversifiable risk</td>
<td>1.36</td>
<td>-1.60</td>
</tr>
<tr>
<td>Current account</td>
<td>3.54</td>
<td>-2.21</td>
</tr>
<tr>
<td>Inflation expectations</td>
<td>12.03***</td>
<td>-4.89***</td>
</tr>
<tr>
<td>Delta Inflation</td>
<td>58.8***</td>
<td>-10.80***</td>
</tr>
</tbody>
</table>

*, ** and *** denote significance at the 10, 5 and 1% levels respectively. $\Phi_1$ refers to the likelihood ratio test of $(\alpha, \beta, \rho) = (\alpha,0,1)$ in $Y_t = \alpha + \beta Y_{t-1} + \rho Y_t + \epsilon_t$. The critical values are from Dickey and Fuller (1981). $\tau$ refers to the Augmented Dickey Fuller (ADF) "t-tests"; $\tau_\tau$ includes a constant and trend and $\tau_\mu$ includes a constant only. The critical values are from Fuller (1976). DF-GLS$\tau$ and DF-GLS$\mu$ are a modified trend and constant versions, respectively, of the ADF tests proposed by Elliot, Rothenberg and Stock (1992). KPSS is a test proposed by Kwiatkowski, Phillips, Schmidt and Shin (1992) which tests the null hypothesis of stationarity. A truncation lag of 8 is used for the calculation of the estimate of the error variance.

All three tests support the stationarity of the Australian real 10-year bond rate around a constant or a trend. On the other hand, evidence for the US real long bond rate is mixed; the ADF and DF-GLS tests fail to reject the null of a unit root, but the KPSS tests fail to reject the null hypothesis that the real US long bond rate is stationary around either a mean or a trend. The return on domestic capital and inflationary expectations are both clearly stationary; the ratio of the Commonwealth government budget balance to GDP is mean stationary; the evidence for the undiversifiable risk term, "beta", is mixed.
### Table C.2

**Real long bond equation (3)**  
*Dependent variable: change in real bond*  

<table>
<thead>
<tr>
<th>Explanatory variable</th>
<th>Coefficient</th>
</tr>
</thead>
<tbody>
<tr>
<td>Speed of adjustment parameter</td>
<td>-0.513*** (0.10)</td>
</tr>
<tr>
<td>Return on capital</td>
<td>0.164*** (0.04)</td>
</tr>
<tr>
<td>Inflation term : ((\bar{\pi}_t - E_t(\pi)))</td>
<td>0.256*** (0.08)</td>
</tr>
<tr>
<td>(\Delta \text{ Real bond}_{t-2})</td>
<td>0.369*** (0.12)</td>
</tr>
<tr>
<td>(\Delta \text{ Return on capital}_{t-1})</td>
<td>0.431* (0.23)</td>
</tr>
<tr>
<td>(\Delta E(\pi)_{t-1})</td>
<td>-1.22*** (0.22)</td>
</tr>
<tr>
<td>(\Delta E(\pi)_{t-2})</td>
<td>0.93*** (0.29)</td>
</tr>
<tr>
<td>(\Delta \text{ Government deficit}_{t})</td>
<td>0.89* (0.52)</td>
</tr>
<tr>
<td>Growth_{t}</td>
<td>0.40* (0.21)</td>
</tr>
<tr>
<td>Growth_{t-1}</td>
<td>-0.39* (0.20)</td>
</tr>
</tbody>
</table>

| |  
| --- | --- |
| \(\bar{R}^2\) | 0.60 |
| DW | 1.76 |
| ARCH test | \(\chi^2_1\) 0.882 (0.347) |
| AR (4) test | \(\chi^2_2\) 3.28 (0.512) |
| Jarque-Bera normality test | \(\chi^2_1\) 0.96 (0.618) |

*, ** and *** denote significance at the 10, 5 and 1% level respectively.  
Standard errors are in parentheses; probability values are in square brackets.
Figure C.1
Real long bond equation (3)

Figure C.2
Nominal bond equation (7)
Table C.3  
Nominal bond equation (7)  
Specification #1  
Dependent variable: change in nominal bond  

<table>
<thead>
<tr>
<th>Explanatory variable</th>
<th>Coefficient</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nominal bond, (j)</td>
<td>-0.241***</td>
</tr>
<tr>
<td>Capital return, (j)</td>
<td>0.079***</td>
</tr>
<tr>
<td>US real, (j)</td>
<td>0.127*</td>
</tr>
<tr>
<td>({E_{PP}(\pi_{t+1})}), (j)</td>
<td>0.204***</td>
</tr>
<tr>
<td>(\Delta) US real, (j)</td>
<td>0.268*</td>
</tr>
<tr>
<td>(\Delta) Expectations, (j)</td>
<td>0.375***</td>
</tr>
<tr>
<td>(\Delta) GDP, (j)</td>
<td>-0.304***</td>
</tr>
</tbody>
</table>

\(R^2\) 0.332  
DW 2.07  
ARCH test  
AR (4) test  
Jarque-Bera normality test  

* *, ** and *** denote significance at the 10, 5 and 1% level respectively. 

Standard errors are in brackets, probability values are in square brackets and the F-test for the joint significance of the US real rate dynamics are in parentheses {}.

The small negative coefficient on the third lag of growth in the dynamics of equation (7) corresponds with the (roughly) 3-year cycle in bond yields in Australia.
References


Bleaney, M., 1993, "The Australian Real Exchange Rate, Terms of Trade and Primary Commodity Prices 1901-91", *CREDIT Research Paper* No.93/6, University of Nottingham.


Comments on paper by A. Tarditi by Robert McCauley (BIS)

This paper offers a contrast between its careful empirical results and local macroeconomic models that, as far as the financial sectors are concerned, sacrifice reality to theoretical appeal. This comment attempts to advance the interpretation of the results of the exchange rate analysis and pose a pair of questions regarding the interest rate analysis.

1. Exchange rate

The analysis of the real exchange rate very nicely underscores the importance of the terms of trade, the stance of monetary and fiscal policy and the accumulating net liability position.

The terms of trade effect in this analysis and in previous analyses seems too strong, and this is one puzzle of Australia's exchange rate. Another puzzle is why does the Australian dollar tend to strengthen when the US dollar appreciates and to fall when the US dollar depreciates. These two puzzles may have common roots in the portfolio behaviour of foreign investors but quite different behavioural grounds. The strong reaction of the Australian dollar to the terms of trade reflects the scarcity value of Australian assets as commodity bets. With Australia, you get industrial country risk and developing country exposure to commodities. Foreign investors buy Australian stocks, currency and even bonds when they are worried about commodity prices. Given the adverse effect of commodity prices on corporate profits and bond prices in the rest of the industrial country portfolio, Australian assets offer some insurance.

Market participants report that the Australian dollar's resonance with the dollar-mark exchange rate arises because Continental and Japanese investors tend to treat the Australian dollar, in common with its Canadian and New Zealand cousins, as a supercharged dollar. Thus, if buying the US dollar looks good, buying the Aussie dollar looks even better. Here the motive is quite different: reaching for yield means accepting risk, not avoiding it.

A question that arises not just in connection with the Australian paper but also in other papers is the theoretical underpinning of net international liabilities or assets. Does this variable measure the growing exposure of global portfolios to Australian dollar assets in a Branson portfolio balance model of exchange rates on the assumption that the current account deficit is financed entirely in Australian dollars? Or does this variable measure a country's international indebtedness, or solvency, where all the debt might be in, say, US dollars? The theoretical underpinning should be thought out so that a proper measure is selected.

2. Long-term interest rate

The paper analyses the real bond yield and finds it related only to the real return on capital and the difference between current and average inflation. The author is quite sensibly unsatisfied with an approach that divides the current yield by current inflation to generate the dependent variable only to enter current inflation as a regressor. She moves on to modelling the nominal bond yield, and that strikes me as a good place to start as well as to end. In such a framework, one can test whether one can cast the model as a real yield equation.

The habit of entering the real return to capital as a determinant of the real rate strikes me as both obscure and sneaky. Obscure because it is not clear how much it is a cyclic variable and how much it is picking up differences across cycles in profitability. Sneaky because high real interest rates, caused by high fiscal deficits in the conventional wisdom, may have constrained managers to show better profits. In other words, might not the real side show the effects of financial markets rather than vice-versa?
The author's experiments with a Markov model for inflation regimes are quite promising. The Markov model seems well justified by the survey expectations that show 10 percent inflation until the end of the 1980s and then drop to 5 percent in the 1990s in one step. But the claim that the Markov-derived expectations are different from and better than "inherently backward-looking survey expectations" should be explicitly demonstrated. Are the estimated mean inflation rates of 8.7 percent and 3.3 percent significantly different from 10 and 5 percent, respectively? Given the correlation of survey and Markov expectations, do the Markov expectations dominate the survey expectations if they are run head-to-head?

The author makes a pitch for so-called behavioural models over the imposition of model-consistent, perfect-foresight expectations. It is sign of danger that such a pitch is felt to be necessary. Policy could only suffer were economists at central banks to yield to their aesthetic inclination to neatness and coherence in model building and thereby miss observed regularities that cannot be derived from some economically correct model of house-trained agents.