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Macroprudential regulation and systemic capital requirements

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Macroprudential Regulation and Systemic Capital Requirements

Celine Gauthier Alfred Lehar and Moez Souissi

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Motivation - System-wide risk

 Current regulation is focussing on risk at individual institutions

 Consensus about a system-wide approach to regulation that would focus on system-wide risks



Motivation - System-wide risk

• A model to measure systemic risk

• Ways to internalise it



Contribution

 We propose a model to measure systemic risk (in the spirit of RAMSI at the BoE)

 We propose to reallocate capital according to individual contributions to systemic risk

 Fixed-point: capital requirement equals contribution to system risk



Contributions on the data side:

- We use extended data on exposures between the big six Canadian banks
- We use non public information on the largest loan exposures of banks
- Expanding the set of exposures between banks and considering the granularity of the loan portfolio have significant impact



Contribution

Main findings:

 Capital reallocation works: can decrease bank PDs as well as the probability of a crisis by around 25%

Works for all 6 capital reallocation mechanisms



Contribution

Main findings:

 Reallocated capital differs from current capital by up to 50%

 Reallocation is not trivially related to size or PD (at least in Canada)



Outline of the presentation

- 1. The related literature
- 2. A model of the banking system
- 3. Impact of contagion channels
- 4. Macroprudential capital requirements
- 5. Conclusion



1. The related literature

- Historical market data to exploit correlations and historical spillovers (Adrian and Brunnermeir [2008], Acharya et al. [2009])
- Network model and aggregate loss distribution conditional on stress-scenario (Aikman et al [2008], Elsinger et al [2006], Upper (2006))

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2. A model of the banking system

 The model used to generate the system loss distribution

 Integrate a credit risk model (Misina and Tessier [2006,2007]) to a network model of exposures between banks

• The network is a potential source of contagion



 Banks that fall short of regulatory requirements start selling assets to an illiquid market (Cifuentes, Shin and Ferrucci [2005])

- Spiral may occur because of mark-to-market accounting
- www.bankofcanada.ca The aggregate loss distribution includes both network and asset fire sale externalities



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2.1 The credit risk model

Two sources of uncertainty:

 Systematic factors which affects all loan portfolios simultaneously

 Idiosyncratic factors due to the composition of individual loan portfolios



2.2 The Network model

• Stylised balance-sheet (net worth)

$$p_i e_i + c_i + \sum_{j=1}^N \pi_{ji} d_j - d_i - L_i$$

• Clearing payment vector:

Min between total amount due and whatever is left after outside debt holders are paid (fixed point, Eisenberg and Noe [2001])



2.3 The asset fire sale (AFS)

• Minimum capital requirement constraint:

$$\frac{p_i e_i + c_i + \sum_j x_i \pi_{ji} - x_i - L}{w_i p_i (e_i - s_i)} \ge r^*$$

 An equilibrium of the model is a combination of interbank payments, individual sales of illiquid assets, and their prices.



2.4 The different sources of defaults

Fundamental default:

- Credit losses decreases capital sufficiently for a bank to be unable to honour its interbank obligations even when others do honour theirs.
 - Prices are not affected by AFS



AFS default:

- The bank is not in fundamental default...
- ...but cannot honour its interbank obligations at the equilibrium price of the illiquid assets...
- …even when all other banks meet their interbank obligations



2.4 The different sources of defaults

Contagious defaults:

• The bank is in default only because other banks are not able to keep their promises.

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3. Impact of contagion channels

| Bank | Fundamental PD | Contagious PD | AFS PD | Contagious PD (AFS) | Total PD (AFS) |
|------|----------------|---------------|--------|---------------------|----------------|
| | (%) | (%) | (%) | (%) | (%) |
| 1 | 0.00 | 0.00 | 2.96 | 3.47 | 6.43 |
| 2 | 0.15 | 0.00 | 9.09 | 0.94 | 10.19 |
| 3 | 0.00 | 0.00 | 2.99 | 6.33 | 9.31 |
| 4 | 0.01 | 0.00 | 6.50 | 3.93 | 10.45 |
| 5 | 0.00 | 0.00 | 1.61 | 6.09 | 7.70 |
| 6 | 0.19 | 0.01 | 4.53 | 6.93 | 11.65 |



• The probability of a financial crisis

| Number | Probability | | probability of involvement of bank | | | | | |
|----------|-------------|--------|------------------------------------|--------|--------|--------|--------|--|
| defaults | (in %) | 1 | 2 | 3 | 4 | 5 | 6 | |
| 1 | 3.53 | 4.64 | 30.86 | 6.97 | 15.49 | 0.75 | 41.28 | |
| 2 | 1.16 | 9.07 | 47.48 | 20.70 | 49.03 | 3.44 | 70.29 | |
| 3 | 0.84 | 14.60 | 57.19 | 45.28 | 83.50 | 12.40 | 87.03 | |
| 4 | 1.11 | 22.21 | 69.86 | 81.68 | 95.25 | 34.96 | 96.04 | |
| 5 | 2.66 | 32.17 | 88.55 | 97.95 | 99.15 | 82.69 | 99.48 | |
| 6 | 4.94 | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 | |



4. Macroprudential capital requirements

Component value-at-risk (beta):

 Allocates capital according to the relative marginal contributions of individual banks on the variance of the aggregate loss distribution



Incremental value-at-risk:

- Allocate capital according to the difference between the VaR of the aggregate loss distribution and the VaR of the aggregate loss without bank i.
- Measures the increase in risk by adding bank i to the system



4. Macroprudential capital requirements

Shapley values:

• Well known measure in game theory

 Allocate capital based on the average marginal value that the player's resources contribute to the total



CoVaR (Adrian and Brunnermeir):

 Allocate capital according to the difference in the VaR of bank i conditional on the whole banking system being at its VaR (CoVar) and the non-conditional VaR of bank i.



4. Macroprudential capital requirements

The reallocation mechanisms:

| Bank | Component | Incremental | Shapley va | $\Delta CoVaR$ | |
|------|-----------|-------------|---------------|----------------|--------|
| | VaR | VaR | Expected loss | VaR | |
| 1 | 95.33 | 104.56 | 105.18 | 105.25 | 96.45 |
| 2 | 103.95 | 101.91 | 102.52 | 102.34 | 103.57 |
| 3 | 96.17 | 92.95 | 92.62 | 92.54 | 96.69 |
| 4 | 110.44 | 114.07 | 113.11 | 113.47 | 95.94 |
| 5 | 91.74 | 89.23 | 89.20 | 89.14 | 91.92 |
| 6 | 106.66 | 104.26 | 104.31 | 104.38 | 149.62 |



The impact on individual default probability:

| Bank | Observed | Basel | Component | Incremental | Shapley value | | $\Delta CoVaR$ |
|---------|----------|-------|-----------|-------------|---------------|------|----------------|
| | capital | equal | VaR | VaR | Expected loss | VaR | |
| 1 | 6.43 | 9.05 | 6.60 | 3.91 | 3.75 | 3.73 | 7.53 |
| 2 | 10.19 | 9.97 | 7.68 | 8.15 | 7.91 | 7.97 | 8.93 |
| 3 | 9.31 | 8.91 | 8.34 | 8.82 | 8.87 | 8.91 | 10.57 |
| 4 | 10.45 | 9.04 | 6.72 | 5.77 | 5.91 | 5.85 | 11.97 |
| 5 | 7.70 | 7.73 | 7.55 | 7.76 | 7.73 | 7.74 | 9.47 |
| 6 | 11.65 | 10.53 | 8.28 | 8.49 | 8.44 | 8.43 | 2.42 |
| Average | 9.29 | 9.21 | 7.53 | 7.15 | 7.10 | 7.11 | 8.48 |



The impact on multiple defaults probabilities:

| Number | Observed | Basel | Component | Incremental | Shapley value | | $\Delta CoVaR$ |
|----------|----------|-------|-----------|-------------|---------------|------|----------------|
| defaults | capital | equal | VaR | VaR | Expected loss | VaR | |
| 1 | 3.53 | 3.55 | 3.01 | 3.43 | 3.39 | 3.41 | 3.01 |
| 2 | 1.16 | 1.05 | 0.85 | 1.11 | 1.09 | 1.10 | 1.20 |
| 3 | 0.84 | 0.60 | 0.51 | 0.75 | 0.73 | 0.75 | 1.25 |
| 4 | 1.11 | 0.70 | 0.67 | 1.08 | 1.06 | 1.08 | 2.47 |
| 5 | 2.66 | 1.70 | 1.71 | 2.49 | 2.58 | 2.57 | 4.06 |
| 6 | 4.94 | 6.09 | 4.62 | 3.04 | 2.95 | 2.93 | 1.93 |
| ≥ 5 | 7.60 | 7.78 | 6.33 | 5.53 | 5.53 | 5.50 | 5.98 |
| ≥ 4 | 8.70 | 8.48 | 7.00 | 6.60 | 6.59 | 6.59 | 8.46 |



5. Conclusion

 Macroprudential capital allocation mechanisms reduce individual default and the prob. of systemic crisis by as much as 25%

First step in measuring systemic risk and macroprudential capital requirement







2.2 The Network model

Stylised balance-sheet

$$p_i e_i + c_i + \sum_{j=1}^N \pi_{ji} d_j - d_i - L_i$$

Price of illiquid assets function of riskiness of BS

$$p_i = \min(1, p + (\overline{w} - w_i)\kappa)$$



Changing the elasticity of the demand curve

| Bank | AFS PD | Contagious PD (AFS) | Total PD |
|------|--------|---------------------------------|----------|
| | () | All data, P_{min} =0.97, in % | 6) |
| 1 | 33.58 | 24.84 | 58.42 |
| 2 | 57.64 | 3.92 | 61.74 |
| 3 | 29.05 | 34.23 | 63.29 |
| 4 | 55.06 | 8.63 | 63.71 |
| 5 | 17.17 | 44.67 | 61.84 |
| 6 | 26.88 | 36.86 | 63.94 |

| | Systemati | e and idiosyneratie | Systematic | | |
|----------------------|-----------------------------|--------------------------|------------|------------------|--|
| | | factors | | factors | |
| Panel A: Descriptive | statistics of | of aggregate loss distri | butions | | |
| | \$Billion %of Tier1 capital | | | %of Tier1capital | |
| Mean | -55.7 | 58.2 | -45.7 | 47.7 | |
| Standard Deviation | -11.4 | 11.9 | -7.9 | 8.3 | |
| Quantiles: | | | | | |
| 99% | -21.9 | 22.9 | -27.3 | 28.5 | |
| 10% | -77.3 | 80.8 | -35.5 | 37.1 | |
| 1% | -97.5 | 101.9 | -63.7 | 66.6 | |
| Panel B: Frequencies | s of bank d | efaults (%) | | | |
| Minimum | 0.004 | | 0.0 | | |
| Average | 0.06 | | 0.0 | | |
| Maximum | | 0.18 | | 0.0 | |



Advantages of scenario analysis:

 Compute the potential losses based on current positions rather than using past losses

Does not induce pro-cyclical risk-taking



2.1 The credit risk model

Severe recession scenario mapped into default rates for 7 sectors

| | Minimum | Average | Maximum | Historic Peaks |
|---------------|---------|---------|---------|----------------|
| Accommodation | 3.0 | 11.7 | 21.0 | 7.6 |
| Agriculture | 1.0 | 1.7 | 2.0 | 0.8 |
| Construction | 2.0 | 6.4 | 10.0 | 3.3 |
| Manufacturing | 5.0 | 12.2 | 20.0 | 8.3 |
| Retail | 0.0 | 4.3 | 8.0 | 5.3 |
| Wholesale | 2.0 | 7.0 | 12.0 | 4.6 |
| Mortgage | 0.0 | 0.6 | 1.0 | 0.6 |





| Bank | PD | Cond. probability of multiple defaults | | | | | |
|------|--------|--|------|------|-------|-------|-------|
| | (in %) | 1 | 2 | 3 | 4 | 5 | 6 |
| 1 | 6.43 | 2.55 | 1.64 | 1.91 | 3.82 | 13.28 | 76.80 |
| 2 | 10.19 | 10.70 | 5.41 | 4.72 | 7.60 | 23.08 | 48.50 |
| 3 | 9.31 | 2.64 | 2.58 | 4.09 | 9.71 | 27.93 | 53.05 |
| 4 | 10.45 | 5.24 | 5.45 | 6.72 | 10.10 | 25.21 | 47.30 |
| 5 | 7.69 | 0.35 | 0.52 | 1.35 | 5.03 | 28.54 | 64.21 |
| 6 | 11.65 | 12.51 | 7.00 | 6.28 | 9.13 | 22.68 | 42.41 |

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2.4 The different sources of defaults

Fundamental default

$$e_i + c_i + \sum_{j=1}^N \pi_{ji} d_j - L_i < d_i$$

• AFS default

$$e_i + c_i + \sum_{j=1}^N \pi_{ji} d_j - L_i > d_i$$
 and
 $p_i^* e_i + c_i + \sum_{j=1}^N \pi_{ji} d_j - L_i < d_i$



2.4 The different sources of defaults

Contagious defaults

$$p_i^* e_i + c_i + \sum_{j=1}^N \pi_{ji} d_j - L_i > d_i \qquad \text{but}$$
$$p_i^* e_i + c_i + \sum_{j=1}^N \pi_{ji} x_j^* - L_i < d_i$$