

# The Economics of Platforms in a Walrasian Framework

Anil K. Jain\* and Robert M. Townsend†

Federal Reserve Board of Governors\* and Massachusetts Institute of Technology†

The findings and conclusions in this paper are solely the responsibility of the authors and should not be interpreted as reflecting the views of the Board of Governors of the Federal Reserve System, or the views of any other person associated with the Federal Reserve System.

## Motivation

- ▶ A successful platform needs to intermediate between buyers and sellers.
- ▶ We are interested in platforms where buyers and sellers care about the composition of the platform's users.
  - ▶ causing a potential 'externality' arising from one agent's platform choice on other agents' willingness to join the same platform.
- ▶ A credit card company must attract both consumers and merchants.
- ▶ Dark pools and exchanges must attract buyers and sellers.
- ▶ Internet service providers (ISPs) need to attract content producers and users.

## Example: M-Pesa

- ▶ Payment system for both consumers and merchants.
- ▶ 20 million M-Pesa users in Kenya.
- ▶ It is used to pay merchants and to transfer money to other users.
- ▶ Given that the a user's benefit to using M-Pesa is conditional on the number of other consumers and merchants:
  - ▶ How much should a consumer pay?
  - ▶ How much should a merchant pay?
  - ▶ How does the payment depend on M-Pesa's composition of users?

## Questions to answer

- ▶ In the context of multiple competing platforms is there a Walrasian equilibrium?
- ▶ Is the Walrasian equilibrium efficient?
- ▶ Is there a role for regulation due to a possible network externality?
- ▶ Are these “externalities” something which (only) regulation can deal with?
- ▶ How do changes in wealth affect prices and subsequently user's welfare?

## Questions to answer

- ▶ In the context of multiple competing platforms is there a Walrasian equilibrium?
- ▶ Is the Walrasian equilibrium efficient?
- ▶ Is there a role for regulation due to a possible network externality?
- ▶ Are these “externalities” something which (only) regulation can deal with?
- ▶ How do changes in wealth affect prices and subsequently user's welfare?

## Questions to answer

- ▶ In the context of multiple competing platforms is there a Walrasian equilibrium?
- ▶ Is the Walrasian equilibrium efficient?
- ▶ Is there a role for regulation due to a possible network externality?
- ▶ Are these “externalities” something which (only) regulation can deal with?
- ▶ How do changes in wealth affect prices and subsequently user's welfare?

## Questions to answer

- ▶ In the context of multiple competing platforms is there a Walrasian equilibrium?
- ▶ Is the Walrasian equilibrium efficient?
- ▶ Is there a role for regulation due to a possible network externality?
- ▶ Are these “externalities” something which (only) regulation can deal with?
- ▶ How do changes in wealth affect prices and subsequently user's welfare?

## Questions to answer

- ▶ In the context of multiple competing platforms is there a Walrasian equilibrium?
- ▶ Is the Walrasian equilibrium efficient?
- ▶ Is there a role for regulation due to a possible network externality?
- ▶ Are these “externalities” something which (only) regulation can deal with?
- ▶ How do changes in wealth affect prices and subsequently user's welfare?



## Solution

- ▶ Answer: Under certain assumptions, general equilibrium theory can answer these questions—in a manner suggested by Meade (1952) and Arrow (1969).
  - ▶ We can “internalize” the network externality through ex ante contracting.
  - ▶ Use “Firms as Clubs” (Prescott and Townsend (2000) and General Equilibrium theory.

# Roadmap

- ▶ Outline the model.
- ▶ Examples of the environment equilibrium.
- ▶ Comparative statics: Testing how the equilibrium changes with changes in costs, wealth, and distribution of user types.
- ▶ Outline model extensions.
- ▶ Conclusion.

## Set-up

- ▶ There are two agent types—buyers (A) and sellers (B).
- ▶ Buyers and sellers can trade only on a platform.
- ▶ Buyers and sellers care about the composition of the platform's users.
- ▶ Buyers and sellers each have some capital endowment ( $\kappa$ ).
- ▶ There is a single intermediary that connects agents to platforms.

## Agent's utility function

- ▶ An agent wants a higher **ratio** of agents of the other type, and **larger** platforms.
- ▶ A buyer's  $(A, i)$  utility function is:

$$U_{A,i}(N_A, N_B) = U_A(N_A, N_B) = \begin{cases} 0 & \text{if } N_A \text{ or } N_B = 0 \\ \left[ \left( \frac{N_B}{N_A} \right)^{\gamma_A} + N_B^{\epsilon_A} \right] & \text{else} \end{cases}$$

- ▶ Where  $\gamma_A, \gamma_B, \epsilon_A$  and  $\epsilon_B > 0$
- ▶ Symmetrically, the seller's  $(B, i)$  utility function is:

$$U_{B,i}(N_A, N_B) = U_B(N_A, N_B) = \begin{cases} 0 & \text{if } N_A \text{ or } N_B = 0 \\ \left[ \left( \frac{N_A}{N_B} \right)^{\gamma_B} + N_A^{\epsilon_B} \right] & \text{else} \end{cases}$$

## Agent's utility function

- ▶ An agent wants a higher **ratio** of agents of the other type, and **larger** platforms.
- ▶ A buyer's  $(A, i)$  utility function is:

$$U_{A,i}(N_A, N_B) = U_A(N_A, N_B) = \begin{cases} 0 & \text{if } N_A \text{ or } N_B = 0 \\ \left[ \left( \frac{N_B}{N_A} \right)^{\gamma_A} + N_B^{\epsilon_A} \right] & \text{else} \end{cases}$$

- ▶ Where  $\gamma_A, \gamma_B, \epsilon_A$  and  $\epsilon_B > 0$
- ▶ Symmetrically, the seller's  $(B, i)$  utility function is:

$$U_{B,i}(N_A, N_B) = U_B(N_A, N_B) = \begin{cases} 0 & \text{if } N_A \text{ or } N_B = 0 \\ \left[ \left( \frac{N_A}{N_B} \right)^{\gamma_B} + N_A^{\epsilon_B} \right] & \text{else} \end{cases}$$

## Cost of making a platform

- ▶ A platform is costly to manufacture, increasing in the number of users of each type, and increasing in the set of possible connections.

$$C(N_A, N_B) = \begin{cases} 0 & \text{if } N_A = 0 \text{ or } N_B = 0 \\ c_A N_A + c_B N_B + c N_A N_B + K & \text{else} \end{cases}$$

- ▶ Where  $c_A, c_B, K \geq 0$  and  $c > 0$ .
- ▶ Larger platforms are more than proportionally more expensive ( $c > 0$ )

## Cost of making a platform

- ▶ A platform is costly to manufacture, increasing in the number of users of each type, and increasing in the set of possible connections.

$$C(N_A, N_B) = \begin{cases} 0 & \text{if } N_A = 0 \text{ or } N_B = 0 \\ c_A N_A + c_B N_B + c N_A N_B + K & \text{else} \end{cases}$$

- ▶ Where  $c_A, c_B, K \geq 0$  and  $c > 0$ .
- ▶ Larger platforms are more than proportionally more expensive ( $c > 0$ )

## Agent's maximization problem

- ▶ Agent type ( $T$ ), subtype ( $i$ ) buys contracts  $b_T(N_A, N_B)$  to join a platform of size and composition  $(N_A, N_B)$ , subject to:
  - ▶ their wealth constraint
  - ▶ joining one platform.
- .
- ▶ Key tool to convexify commodity space: agents do not buy discrete numbers of contracts instead agent's buy probabilities to join a platform.



## Agent's maximization problem

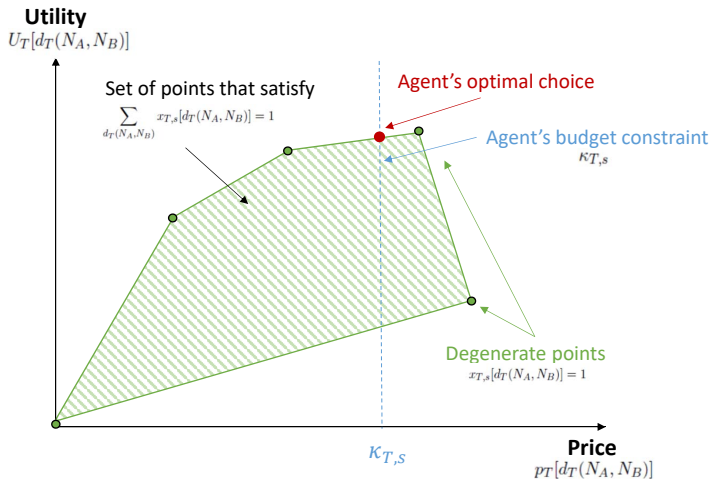
- ▶ Agent  $(T, i)$  takes prices  $p[b_T(N_A, N_B)]$  as given and solve the following maximization problem:

$$\max_{x_{T,i}} \sum_{N_A, N_B} x_{T,i}[b_T(N_A, N_B)] U_T[b_T(N_A, N_B)] \quad (1)$$

$$\text{s.t.} \quad \sum_{N_A, N_B} x_{T,i}[b_T(N_A, N_B)] p[b_T(N_A, N_B)] \leq \kappa_{T,i} \quad (2)$$

$$\sum_{N_A, N_B} x_{T,i}[b_T(N_A, N_B)] = 1 \quad (3)$$

# Agent's maximization problem—graphical illustration



## Intermediary's problem

- ▶ The intermediary maximizes the number of platforms  $y(N_A, N_B)$  to produce for the given prices ( $p[b_T(N_A, N_B)]$ ) for each position in the platform.
- ▶ The intermediary's profits are equal to the number of contracts it sells multiplied by the price of the contract minus the cost of the capital input.

## Intermediary's problem

- ▶ The intermediary's FOC w.r.t. to  $y(N_A, N_B)$  is:

$$C(N_A, N_B) \geq p[b_A(N_A, N_B)] * N_A + p[b_B(N_A, N_B)] * N_B \quad (4)$$

- ▶ **This condition requires the payments/memberships the platform receives must cover all of the platform's costs.**

## Market clearing

- ▶ The demand for each contract for each type must equal the supply of that contract.

$$\sum_i x_{T,i}[b_T(N_A, N_B)] = y_T(b_T(N_A, N_B)) \equiv N_A \times y(N_A, N_B) \quad \forall N_A, N_B, T \in \dots$$

## Market clearing

- ▶ The demand for each contract for each type must equal the supply of that contract.

$$\sum_i x_{T,i}[b_T(N_A, N_B)] = y_T(b_T(N_A, N_B)) \equiv N_A \times y(N_A, N_B) \quad \forall N_A, N_B, T \in \dots$$

## Competitive equilibrium

- ▶ A competitive equilibrium in this economy is  $(p, x, y) \in L \times X \times Y$  such that
  - ▶ For given prices, the allocation solves the consumer and platform maximization problems.
  - ▶ All markets clear: the demand for each contract equals the supply of each contract.
  - ▶ Active platforms are populated by numbers of buyers and sellers as anticipated (stipulated).

## Summary of results

- ▶ A competitive equilibrium is Pareto optimal.
- ▶ Any Pareto optimal allocation can be achieved with transfers between agents:
  - ▶ The first and second welfare theorems hold in our modified environment
- ▶ The endogenous pricing internalizes the effect of changing the composition of the platform—overcoming any network externality—as in Arrow (1969)



## Simple example—identical preferences and wealth

- ▶ Consider a platform with 2 subtypes of buyers, and 2 subtypes of sellers
- ▶ There is a measure 1 of each type, a measure 0.5 of each subtype
- ▶ Each agent is equally wealthy

Equilibrium platforms		
Platform Size	Number of Platforms Created	Cost of Production
$(N_A, N_B)$	$y(N_A, N_B)$	$C(N_A, N_B)$
(2,2)	0.5	8

Equilibrium user utility and platform choice						
Type ( $T, s$ )	Wealth ( $\kappa_{T,s}$ )	Platform Joined ( $N_A, N_B$ )	Price of Joining $p(d_T[N_A, N_B])$	Pr(joining) $x_{T,s}(d_T[N_A, N_B])$	Utility on Platform $U_T(N_A, N_B)$	
A,1	2	(2,2)	2	1	2.41	
A,2	2	(2,2)	2	1	2.41	
B,1	2	(2,2)	2	1	2.41	
B,2	2	(2,2)	2	1	2.41	

## The effect of a single richer subtype

- ▶ Let subtype  $(B, 2)$  be markedly richer than other types
- ▶  $(B, 2)$  will “sponsor” larger platforms—lower prices for Type  $(A)$

Platform Size ( $N_A, N_B$ )	Number of Platforms created	Cost of Production
(3, 2)	0.25	11
(1, 2)	0.25	5

Type ( $T, i$ )	Wealth	Platform joined ( $N_A, N_B$ )	Price of joining	Pr(joining)	Utility on Platform	Expected Utility
$A, 1$	1.37	(3, 2)	1.37	1	2.23	2.23
$A, 2$	1.64	(3, 2)	1.37	0.5	2.23	2.53
		(1, 2)	1.91	0.5	2.8	
$B, 1$	1.54	(1, 2)	1.54	1	1.7	1.7
$B, 2$	3.45	(3, 2)	3.45	1	2.96	2.96

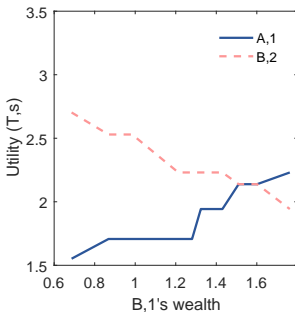
## The effect of a single richer subtype

- ▶ Let subtype  $(B, 2)$  be markedly richer than other types
- ▶  $(B, 2)$  will “sponsor” larger platforms—lower prices for Type  $(A)$

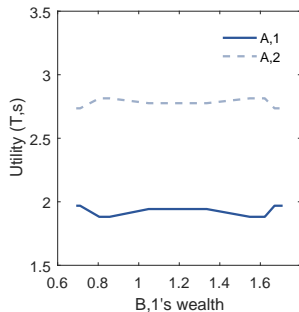
Platform Size ( $N_A, N_B$ )	Number of Platforms created	Cost of Production
(3, 2)	0.25	11
(1, 2)	0.25	5

Type ( $T, i$ )	Wealth	Platform joined ( $N_A, N_B$ )	Price of joining	Pr(joining)	Utility on Platform	Expected Utility
A, 1	1.37	(3, 2)	1.37	1	2.23	2.23
A, 2	1.64	(3, 2)	1.37	0.5	2.23	2.53
		(1, 2)	1.91	0.5	2.8	
B, 1	1.54	(1, 2)	1.54	1	1.7	1.7
B, 2	3.45	(3, 2)	3.45	1	2.96	2.96

How does the equilibrium change as we redistribute wealth? Redistributing wealth *across-* and *within-* agent type.

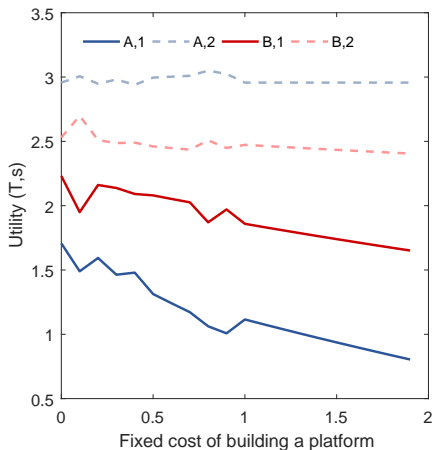


(A) **Across:** Transferring wealth from (A,2) to (B,1)

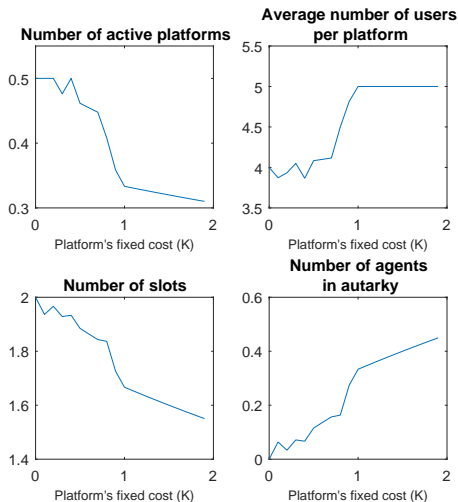


(B) **Within:** Transferring wealth from (B,2) to (B,1)

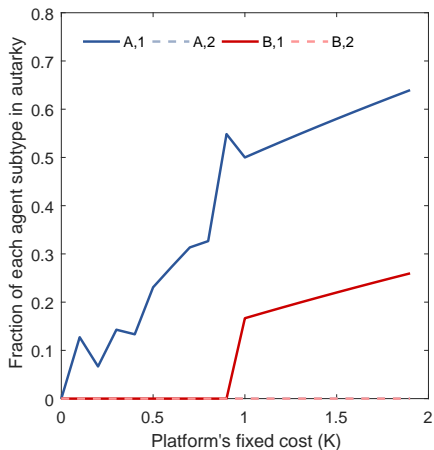
How does the equilibrium utility change as we increase the fixed cost of building a platform?



How does the equilibrium characteristics change as we increase the fixed cost of building a platform?



How does participation by subtype change as the fixed cost of building a platform rises?



## Extensions (in the paper)

- ▶ User heterogeneity
  - ▶ The base model only allows for heterogeneity within users by wealth.
  - ▶ The model is extended (in the paper) to allow different user preferences within type—for example, some agents really like being on larger platforms.
- ▶ Multihoming
  - ▶ The base model only allows agents to join one platform.
  - ▶ The model is extended to allow agents to join multiple platforms.



# Conclusion

- ▶ Even when agents' preferences are dependent on a platform's composition – the competitive equilibrium is efficient.
  - ▶ The endogenous pricing internalizes the benefits from changing a platform's composition.
- ▶ Using the GE framework we can examine how changes in wealth, preferences, affect the resulting equilibrium.
- ▶ A decrease in the cost of creating platforms may help the poorest agents the most.
- ▶ Our framework has limitations:
  - ▶ We assume no platform has any market power.
  - ▶ Our model is purely static – no consideration for entry or innovation in the space of platforms.