

The New Area-Wide Model II:
An Updated Version of the ECB's Micro-Founded Model
for Forecasting and Policy Analysis with a Financial Sector

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What we do

- ▶ Depart from the estimated baseline version of the ECB's New Area-Wide Model (NAWM):
 - ▶ stylised financial frictions in the form of risk premium shocks
 - ▶ no *endogenous* financial intermediation frictions

What we do

- ▶ Depart from the estimated baseline version of the ECB's New Area-Wide Model (NAWM):
 - ▶ stylised financial frictions in the form of risk premium shocks
 - ▶ no *endogenous* financial intermediation frictions
- ▶ Extend the baseline NAWM with a rich financial intermediary sector:
 - ▶ analyze effects of non-standard measures, especially asset purchases, on the macroeconomy
 - ▶ study how shocks originating in the financial sector transmit to the real economy and contribute to business-cycle fluctuations
 - ▶ account for the prominent role of bank lending rates in the transmission of monetary policy operations

Outline

- 1 The model
- 2 Bayesian estimation
- 3 Inspecting the transmission mechanisms
- 4 Model comparison exercise
- 5 Conclusion

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The baseline version of the NAWM

- ▶ The baseline NAWM is a small-open-economy extension of the Smets-Wouters (2003, 2007) model, designed for forecasting and policy analysis at the ECB:
 - ▶ agents: households, (intermediate and final-good) firms, central bank and fiscal authority ▶ A
 - ▶ real and nominal frictions: habit formation, adjustment costs, sticky prices and wages, limited exchange-rate pass-through, ...
 - ▶ financial frictions: (exogenous) domestic and external risk premia ▶ F
 - ▶ Rest-of-the-World block (SVAR)
- ▶ Estimated on 18 macro time series employing Bayesian inference methods. ▶ D
- ▶ Details provided in Christoffel-Coenen-Warne (2008, 2011).

The financial extension of the NAWM: A bird's eye view

- ▶ Households face “loan-in-advance” constraint:
 - ▶ each household accumulates physical capital, the services of which it rents out to firms
 - ▶ capital investments by a household have to be financed by new bank loans (Carlstrom-et-al., 2014)
- ▶ Financial intermediaries (“banks”) engage in maturity transformation:
 - ▶ banks offer long-term loans to the private sector to finance investment projects and hold domestic and foreign long-term government bonds
 - ▶ banks fund these assets with short-term household deposits and with their equity/net worth (accumulated through retained earnings)

The financial extension of the NAWM: A bird's eye view

- ▶ Imperfect financial markets:
 - ▶ the option to abscond with a portion of their assets (“agency problem”) limits the leverage of banks (Gertler-Karadi, 2011 and 2013)
 - ▶ banks’ capital position influences the transmission of shocks (“financial accelerator” mechanism)
 - ▶ households’ holdings of domestic long-term government bonds are s.t. portfolio costs
 - ▶ foreign trade is intermediated by banks
- ▶ Delayed pass-through to lending rates:
 - ▶ long-term loans are originated by funding-constraint wholesale banks
 - ▶ monopolistically-competitive retail banks (Gerali-et-al., 2011) distribute loans and adjust loan rates sluggishly

The financial extension of the NAWM: A bird's eye view

- ▶ Exogenous financial disturbances:
 - ▶ survival rate of wholesale bankers
 - ▶ market power of retail bankers
- ▶ Central bank can purchase loans and government bonds from wholesale banks (against issuance of short-term excess reserves):
 - ▶ ease banks' leverage constraints ("stealth recapitalisation") and improve lending conditions ▶ CB
 - ▶ banks' holdings of foreign currency-denominated bonds account for exchange-rate channel of asset purchases

▶ Other extensions

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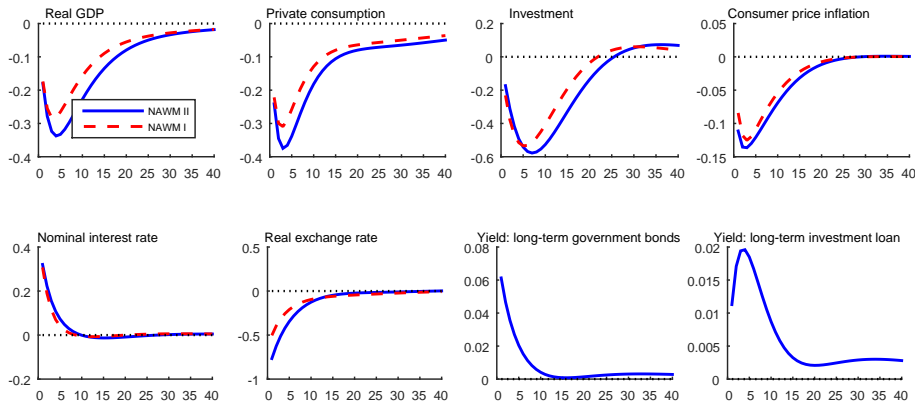
The data

- ▶ Macro data:
 - ▶ 18 macro time series of baseline NAWM
 - ▶ Source: Area-Wide Model database (Fagan et al., 2001)
- ▶ Financial data:
 - ▶ 10-year government bond yields for the euro area (AAA) and for the United States, and a composite euro area long-term lending rate
 - ▶ Source: ECB's Statistical Data Warehouse, Bundesbank, FRED
- ▶ Survey data:
 - ▶ long-term inflation expectations, and long-term growth expectations
 - ▶ Source: ECB's Survey of Professional Forecasters (SPF)
- ▶ Measure of the euro area output gap (based on the NMCM)
- ▶ Estimation sample extending from 1985 to 2014 [▶ Fig](#) [▶ Cal](#) [▶ Est](#)

Outline

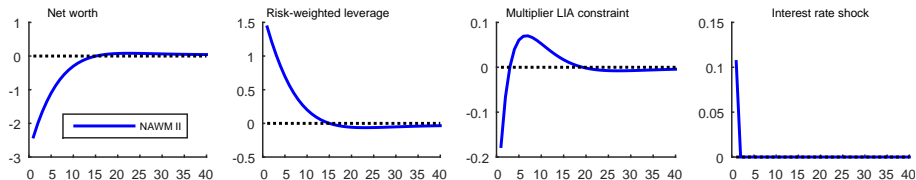
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Transmission of an interest rate shock



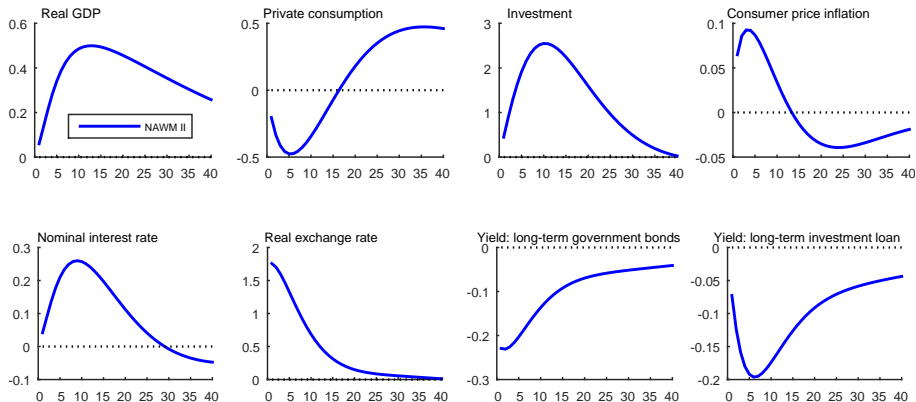
Note: This slide depicts the impulse responses of selected domestic variables to an interest rate shock equal to one standard deviation. All impulse responses are reported as percentage deviations from the model's non-stochastic balanced growth path, except for the impulse responses of the inflation and interest rates which are reported as annualised percentage-point deviations.

Transmission of an interest rate shock (cont'd)



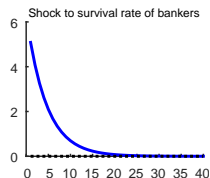
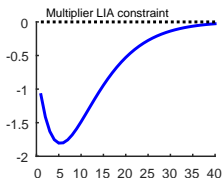
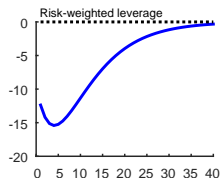
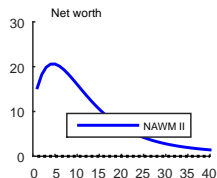
Note: See above.

Transmission of a shock to the survival rate θ



Note: This slide depicts the impulse responses of selected domestic variables to a shock to the wholesale banks' survival rate equal to one standard deviation. All impulse responses are reported as percentage deviations from the model's non-stochastic balanced growth path, except for the impulse responses of the inflation and interest rates which are reported as annualised percentage-point deviations.

Transmission of a shock to θ (cont'd)



Note: See above.

▶ Retail bank mark-down shock

Simulating the effects of asset purchases

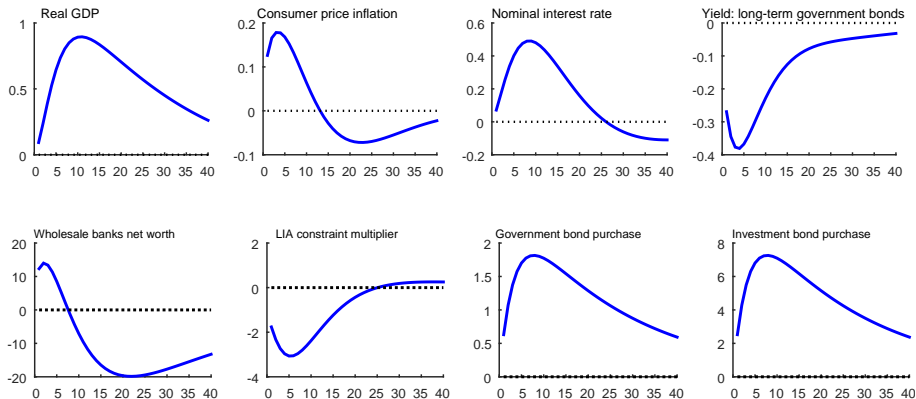
APP as announced in January 2015:

- ▶ 11% of GDP, 8-year maturity (9% in “ten-year equivalents”)
- ▶ 20% AAA government bonds, 80% “risky” assets
- ▶ hump-shaped, peaks in 2 years’ time, exits as bonds mature

Simulating the effects of asset purchases, cont.

▶ XR

▶ PEG

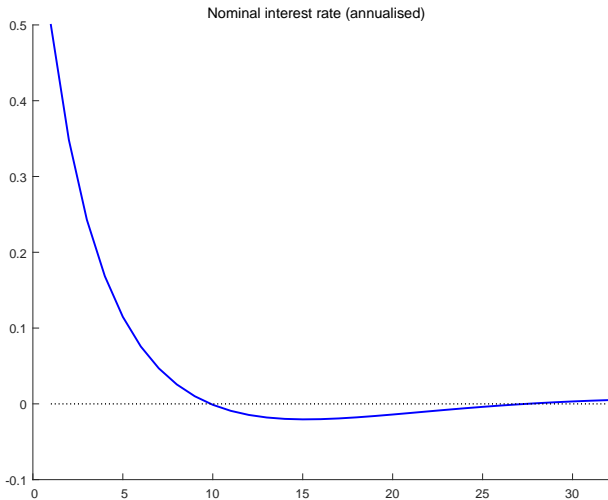


Note: This slide depicts the impulse responses of selected domestic variables to an APP shock for the baseline and for an alternative calibration. All impulse responses are reported as percentage deviations from the model's non-stochastic balanced growth path, except for the impulse responses of the inflation and interest rates which are reported as annualised percentage-point deviations.

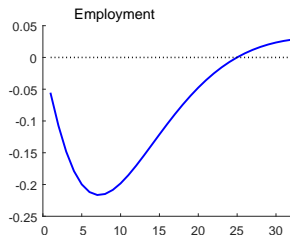
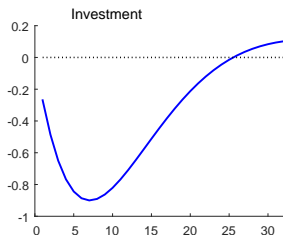
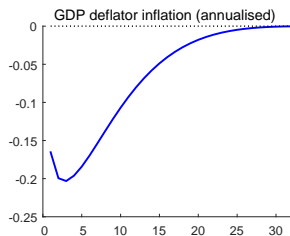
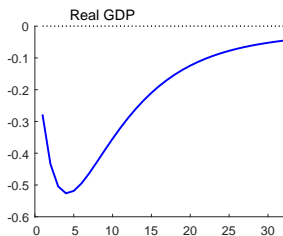
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50 basis points increase in the policy rate



50 basis points increase in the policy rate c'td



Note: This slide depicts the impulse responses of selected domestic variables to an interest rate increase of 50 basis points (annualised). All impulse responses are reported as percentage deviations from the model's non-stochastic balanced growth path, except for the impulse responses of the inflation and interest rates which are reported as annualised percentage-point deviations.

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Conclusion

- ▶ There exist a variety of frameworks for analysing the effects of the ECB's NSMs – reflecting their specific purpose and nature.
- ▶ The extension of the NAWM with a financial sector goes a long way towards providing a rich and detailed quantitative framework:
 - ▶ central bank asset purchases alleviate the funding constraints of banks and operate through domestic and external channels
 - ▶ emphasis on realistic bank-based financing with gradual lending-rate pass-through
- ▶ Preliminary findings regarding the macroeconomic impact of the ECB's asset purchases are broadly in line with alternative estimates.

Background slides

Linking “financial frictions” and the ECB’s NSMs

► Motivation

Financial frictions	Non-standard measures			
	(E)APP	(T)LTRO	OMT	SMP
Imperfect financial markets, funding constraint	X	(X)		X
Maturity transformation, nominal debt	X			X
Interbank frictions		X		
Multiple equilibria in sovereign financing			X	
Bank run equilibria		X	X	
Inability to commit to future interest rates	X	X		

- ▶ **Households:** consume, accumulate physical capital, supply differentiated labour services, set wages in monopolistically competitive markets, trade in domestic and foreign bonds.
- ▶ **Firms:** produce tradable intermediate and non-tradable final goods
 - ▶ domestic intermediate-good firms: use labour and capital services as inputs, produce tradable differentiated goods, set prices in *producer* currency in monopolistically competitive markets at home and abroad
 - ▶ foreign intermediate-good firms: sell differentiated goods in domestic markets, set prices in *local* currency in monopolistically competitive markets
 - ▶ final-good firms: combine domestic and foreign intermediate goods into three non-tradable goods: a private consumption good, a private investment good, a public consumption good

- ▶ **Central bank**: sets the short-term nominal interest rate by following a Taylor-type interest-rate rule.
- ▶ **Fiscal authority**: purchases public consumption goods, issues bonds, levies distortionary as well as lump-sum taxes.

- ▶ The NAWM features a relatively large number of frictions:
 - ▶ external habit formation in consumption
 - ▶ generalised adjustment cost in investment, imports and exports
 - ▶ fixed cost in intermediate-good production
 - ▶ monopolistic competition in intermediate-good and labour markets
 - ▶ sticky prices and wages à la Calvo, with dynamic indexation
 - ▶ domestic and external financial intermediation costs
 - ▶ non-state-contingent bonds
- ▶ The model contains a relatively large number of shocks (classified as demand, technology, markup and foreign shocks, plus a monetary policy shock).

- ▶ The NAWM uses data on 18 key macroeconomic variables:
 - real GDP
 - private consumption
 - government consumption
 - total investment
 - extra-euro area exports
 - extra-euro area imports
 - GDP deflator
 - consumption deflator
 - import deflator
 - employment
 - nominal wages
 - nominal interest rate (EURIBOR)
 - nominal effective exchange rate
 - competitors' export prices[†]
 - foreign demand[†]
 - foreign prices[†]
 - foreign nominal interest rate[†]
 - oil price[†]
- ▶ The variables with a dagger ('[†]') are modelled using a structural VAR, while government consumption is modelled as an AR process.

The financial extension in some detail: Market for loans

► B

- ▶ Demand for loans: loans are taken out by households
- ▶ Supply of loans: loans are originated by wholesale banks and distributed by retail banks
- ▶ Loan characteristics (at the retail level): nominal consoles with geometrically decaying coupons (as in Woodford, 2001):
 - ▶ loan value: $Q_{I,t} B_{I,t+1}$
 - ▶ loan rate (“yield to maturity”):

$$\mathcal{R}_{I,t} = \frac{1}{Q_{I,t}} + \varrho_I,$$

where $Q_{I,t}$ is the “discount price” of the loan $B_{I,t+1}$ and ϱ_I denotes the decay factor of the coupons

The financial extension in some detail: Demand for loans

► B

- ▶ Investments by household h require new bank loans (“loan-in-advance (LIA) constraint”, Carlstrom-Fuerst-Paustian, 2014):

$$P_{C,t} \tilde{p}_{I,t} I_{h,t} \leq Q_{I,t} (B_{I,t+1} - \varrho_I B_{I,t}),$$

where \tilde{p}_t^I is the relative price of the investment good obtained from the capital good producer

- ▶ Value of the loan for household h :

$$\beta \mathbf{E}_t \left[\frac{\Lambda_{h,t+1}}{\Lambda_{h,t}} \frac{P_{C,t}}{P_{C,t+1}} \frac{1 + \varrho_I Q_{I,t+1} (1 + \varsigma_{h,t+1})}{Q_{I,t} (1 + \varsigma_{h,t})} \right] = 1$$
$$\tilde{p}_{I,t} (1 + \varsigma_{h,t}) = Q_{h,t} \epsilon_t^I,$$

where $\varsigma_{h,t} \Lambda_{h,t} / P_{C,t}$ is the Lagrange multiplier associated with the household's LIA constraint and $Q_{h,t}$ represents Tobin's Q

- ▶ Funding-constrained **wholesale banks** (Gertler-Karadi, 2013):
 - ▶ originate long-term loans and hold domestic and foreign long-term government bonds, with expected excess returns s.t. no-arbitrage conditions
 - ▶ face a leverage constraint Φ_t reflecting the assumption that they can abscond with a portion Ψ of loans, and a portion $\omega_L \Psi$ ($\omega_{L,t}^* \Psi$) of domestic (foreign) government bonds
 - ▶ cannot raise equity, but only rebuild net worth NW_t through retained earnings
 - ▶ die with probability $1 - \theta_t$
 - ▶ new banks receive startup funds Θ
- ▶ Monopolistically competitive **retail banks** (Gerali-et-al., 2011): distribute loans and adjust loan rates sluggishly

- ▶ Wholesale banks' balance sheet:

$$\tilde{Q}_{I,t} B_{I,b,t+1}^p + Q_{L,t} B_{L,b,t+1}^p + S_t Q_{L,t}^* B_{L,b,t+1}^{*,p} = NW_{b,t} + D_{b,t+1}^h$$

- ▶ Evolution of net worth:

$$\begin{aligned} NW_{b,t+1} = & \tilde{R}_{I,t+1} \tilde{Q}_{I,t} B_{I,b,t+1}^p + R_{L,t+1} Q_{L,t} B_{L,b,t+1}^p \\ & + S_{t+1}/S_t R_{L,t+1}^* Q_{L,t}^* B_{L,b,t+1}^{*,p} - \epsilon_t^{RP} R_t D_{b,t+1}^h \end{aligned}$$

- ▶ Objective:

$$V_{b,t}(NW_{b,t}) = \max E_t \left[\sum_{k=1}^{\infty} (1 - \theta_{t+k}) \Pi_{i=1}^{k-1} \theta_{t+i} \Lambda_{t,t+k} \Pi_{C,t+k}^{-1} NW_{b,t+k} \right]$$

- ▶ Agency problem: banker can divert
 - ▶ the fraction Ψ of investment loans,
 - ▶ the fraction $\omega_{L,t}\Psi$ of domestic government bonds, and
 - ▶ the fraction $\omega_{L,t}^*\Psi$ of foreign government bonds, with $0 \leq \omega_{L,t}, \omega_{L,t}^* \leq 1$
- ▶ Lenders can recover the residual funds and shut the bank down
- ▶ Incentive constraint:

$$V_{b,t}(NW_{b,t}) \geq \Psi(\tilde{Q}_{I_t} B_{I,b,t+1}^p + \omega_{L,t} Q_{L,t} B_{L,b,t+1}^p + \omega_{L,t}^* S_t Q_{L,t}^* B_{L,b,t+1}^{*,p})$$

- ▶ The wholesale banks' balance sheets are s.t. a constraint on the “risk-weighted” leverage ratio Φ_t w.r.t. net worth NW_t :

$$\tilde{Q}_{I,t} B_{I,t+1}^p + \omega_L Q_{L,t} B_{L,t+1}^p + \omega_{L,t}^* S_t Q_{L,t}^* B_{L,t+1}^{*,p} = \Phi_t NW_t,$$

where $\tilde{Q}_{I,t}$, $Q_{L,t}$ and $Q_{L,t}^*$ are the “discount prices” of the privately (p) intermediated assets $B_{I,t+1}^p$, $B_{L,t+1}^p$ and $B_{L,t+1}^{*,p}$

- ▶ In equilibrium, the wholesale banks' leverage is given by:

$$\Phi_t = \frac{\mathbb{E}_t \left[\Lambda_{t,t+1} \Omega_{t+1} \Pi_{C,t+1}^{-1} \epsilon_t^{RP} R_t \right]}{\Psi - \mathbb{E}_t \left[\Lambda_{t,t+1} \Omega_{t+1} \Pi_{C,t+1}^{-1} \left(\tilde{R}_{I,t+1} - \epsilon_t^{RP} R_t \right) \right]},$$

where $\Lambda_{t,t+1} = \Lambda_{t+1}/\Lambda_t$, $\Pi_{C,t+1} = P_{C,t+1}/P_{C,t}$ and Ω_{t+1} is a discount factor modifier

Supply of loans: Wholesale banks ▶ B

- ▶ Low of motion for the wholesale banks' aggregate net worth:

$$\begin{aligned} NW_t = \theta_t & \left((\tilde{R}_{I,t} - \epsilon_{t-1}^{RP} R_{t-1}) \frac{\tilde{Q}_{I,t-1} B_{I,t}^p}{NW_{t-1}} \right. \\ & + (R_{L,t} - \epsilon_{t-1}^{RP} R_{t-1}) \frac{Q_{L,t-1} B_{L,t}^p}{NW_{t-1}} \\ & + \left(\frac{S_t \tilde{R}_{L,t}^*}{S_{t-1}} - \epsilon_{t-1}^{RP} R_{t-1} \right) \frac{S_t Q_{L,t-1}^* B_{L,t}^{*,p}}{NW_{t-1}} \\ & \left. + \epsilon_{t-1}^{RP} R_{t-1} \right) NW_{t-1} + \Theta, \end{aligned}$$

where $\tilde{R}_{I,t}$, $R_{L,t}$ and $R_{L,t}^*$ are the “expected returns” of the wholesale banks' assets in excess of the interest on household deposits $\epsilon_{t-1}^{RP} R_{t-1}$

- ▶ Arbitrage relation between loans and domestic government bonds:

$$\begin{aligned} \omega_L \mathbf{E}_t \left[\Lambda_{t,t+1} \Omega_{t+1} \Pi_{C,t+1}^{-1} (\tilde{R}_{I,t+1} - \epsilon_t^{RP} R_t) \right] \\ = \mathbf{E}_t \left[\Lambda_{t,t+1} \Omega_{t+1} \Pi_{C,t+1}^{-1} (R_{L,t+1} - \epsilon_t^{RP} R_t) \right] \end{aligned}$$

- ▶ Arbitrage relation between domestic and foreign government bonds:

$$\begin{aligned} \tilde{\omega}_{L,t}^* \mathbf{E}_t \left[\Lambda_{t,t+1} \Omega_{t+1} \Pi_{C,t+1}^{-1} \left(\frac{S_{t+1} R_{L,t+1}^*}{S_t} - \epsilon_t^{RP} R_t \right) \right] \\ = \mathbf{E}_t \left[\Lambda_{t,t+1} \Omega_{t+1} \Pi_{C,t+1}^{-1} (R_{L,t+1} - \epsilon_t^{RP} R_t) \right], \end{aligned}$$

where $\tilde{\omega}_{L,t}^* = \tilde{\omega}_L^* (1 - \Gamma_L^*(s_{L,t+1}^*; \epsilon_t^{RP*}))$ and $\tilde{\omega}_L^* = \omega_L / \omega_L^*$

Supply of loans: Retail banks ▶ B

- ▶ Retail banks obtain an amount $\tilde{Q}_{I,t} B_{I,t}$ of loans from the wholesale banks, differentiate them costlessly and distribute an amount $Q_{I,t} B_{I,t} \leq \tilde{Q}_{I,t} B_{I,t}$ of loans to the households.
- ▶ Retail banks face rigidities constraining their ability to re-set the loan price, like in Calvo (1983), resulting in sluggish loan rate adjustments:
 - ▶ loan price re-set (Calvo) parameter: ξ_I
 - ▶ “mark-down” shock: φ_t^I , with $\varphi^I \leq 1$
- ▶ Log-linearised equations for optimal loan price of retail bank r and for aggregate loan price index:

$$\begin{aligned}\hat{Q}_{I,r,t}^\circ &= (1 - \beta\xi_I)(\hat{\tilde{Q}}_{I,t} + \hat{\varphi}_t^I) + \beta\xi_I \hat{Q}_{I,r,t+1}^\circ \\ \hat{Q}_{I,t} &= \xi_I \hat{Q}_{I,t-1} + (1 - \xi_I) \hat{Q}_{I,r,t}^\circ\end{aligned}$$

The financial extension in some detail: Asset purchases ▶ B

- ▶ In the full model, also households are allowed to hold domestic government bonds s.t. portfolio adjustment costs:

$$\Gamma_L^h(B_{L,h,t}^p) = 1/2 \gamma_L^h \left(B_{L,h,t}^p - \bar{B}_{L,h}^p \right)^2 / \bar{B}_{L,h}^p$$

- ▶ The central bank can purchase loans and government bonds from wholesale banks s.t. aggregate supply:

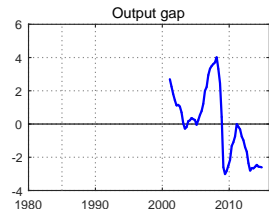
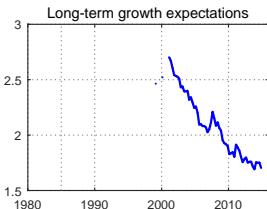
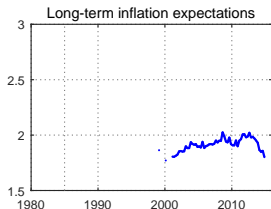
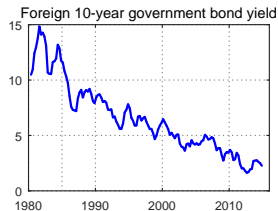
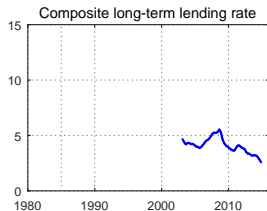
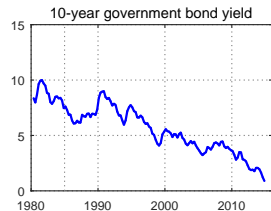
$$\begin{aligned} B_{I,t}^p + B_{I,t}^g &= B_{I,t} \\ B_{L,t}^p + B_{L,t}^g &= B_{L,t} \\ B_{L,t}^{*,p} + B_{L,t}^{*,g} &= B_{L,t}^*, \end{aligned}$$

where superscript p (g) denotes assets held privately (publicly)

- ▶ Asset purchases (against issuance of short-term excess reserves) ease wholesale banks' leverage constraint: they can extend more loans

- ▶ Non-zero import content of exports
- ▶ Kimball aggregator in deriving price Phillips curves (real rigidity)
- ▶ Partial indexation of wages to trend productivity in deriving wage Phillips curve
- ▶ Uncertainty about persistent shifts in trend productivity (signal extraction problem) linked to external measure of potential output
- ▶ Time-varying equilibrium real interest rate in monetary policy rule linked to perceived trend productivity growth
- ▶ Time-varying misperceptions on part of private agents about central bank's inflation objective

The financial, survey and output gap data



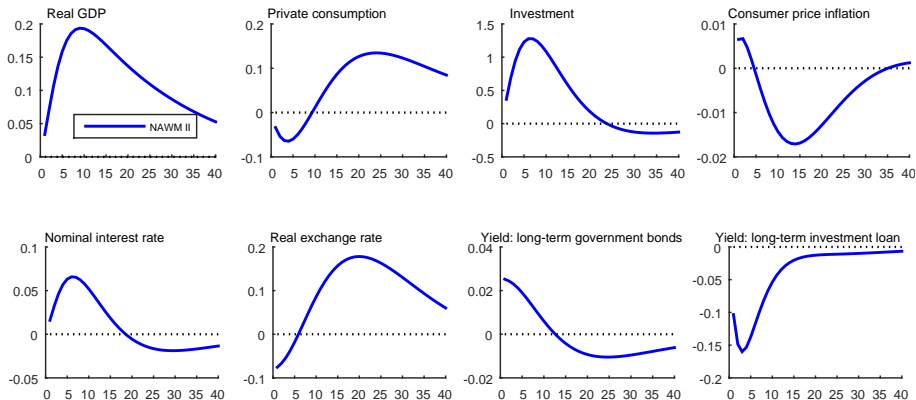
Note: The euro area 10-year government bond yield series (AAA) is available from 2004Q3 onwards, while the earlier observations concern the German 10-year government bond yield. The euro area long-term lending rate is available from 2003Q1 onwards and covers (new business) lending with an original maturity of over 1 year to households for house purchases and to non-financial corporations.

Parameter	Description	Value
A. Wholesale banks		
Φ	Leverage ratio	6.00
θ	Survival rate	0.95
B. Retail banks		
φ^I	Mark-down parameter	0.987
C. Duration of assets ($= 1/(4(1 - \varrho/R))$)		
ϱ_I	Decay parameter: loans	0.974
ϱ_L	Decay parameter: dom. gov. bonds	0.976
ϱ_L^*	Decay parameter: foreign gov. bonds	0.976
D. Spreads (in annualised percentage points)		
$R_I - R$	Retail loan rate over deposit rate	2.17

Parameter	Prior distribution	Posterior distribution	
		mode	std
A. Relative absconding rates for wholesale banks			
ω_L	gamma(0.72,0.05)	0.846	0.039
$\tilde{\omega}_L^*$	gamma(1.00,0.05)	0.967	0.042
B. Loan price re-set parameter for retail banks			
ξ_I	beta(0.75,0.0375)	0.740	0.019
C. Households' portfolio adjustment parameter			
γ_L^h	gamma(0.01,0.0025)	0.009	0.001
D. Autoregressive parameters of financial shock processes			
ρ_θ	beta(0.75,0.05)	0.801	0.044
ρ_{φ^I}	beta(0.75,0.05)	0.711	0.038

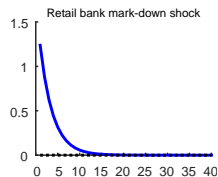
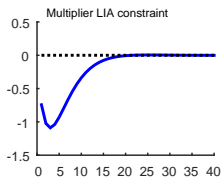
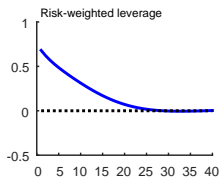
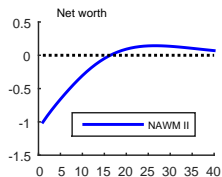
Transmission of a shock to the mark-down parameter φ^I

► B



Note: This slide depicts the impulse responses of selected domestic variables to to the retail banks' mark-down parameter equal to one standard deviation. All impulse responses are reported as percentage deviations from the model's non-stochastic balanced growth path, except for the impulse responses of the inflation and interest rates which are reported as annualised percentage-point deviations.

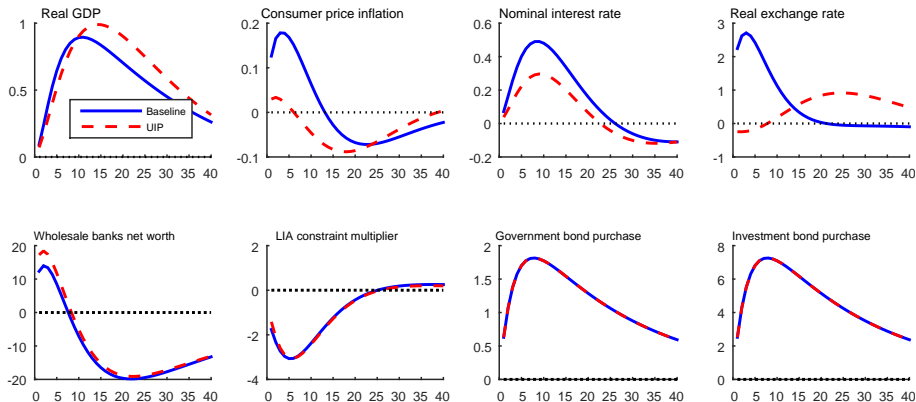
Transmission of a shock to φ^I (cont'd)



Note: See above.

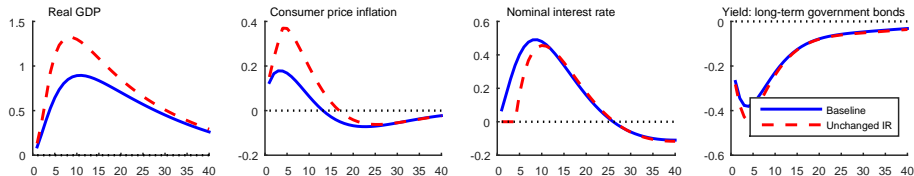
Impact of the exchange rate channel

► B



Note: This slide depicts the impulse responses of selected domestic variables to an APP shock for the baseline calibration and in a model version without the XR channel but with a standard UIP condition. All impulse responses are reported as percentage deviations from the model's non-stochastic balanced growth path, except for the impulse responses of the inflation and interest rates which are reported as annualised percentage-point deviations.

Effects with unchanged interest rate ▶ B



Note: This slide depicts the impulse responses of selected domestic variables to an APP shock for the baseline calibration with interest rates unchanged for 4 quarters. All impulse responses are reported as percentage deviations from the model's non-stochastic balanced growth path, except for the impulse responses of the inflation and interest rates which are reported as annualised percentage-point deviations.