

# Blockchain Economics

Joseph Abadi & Markus Brunnermeier

(Preliminary and not for distribution)

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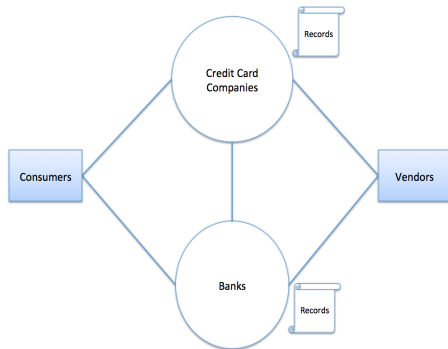
# Motivation

Ledgers are “written” and maintained by

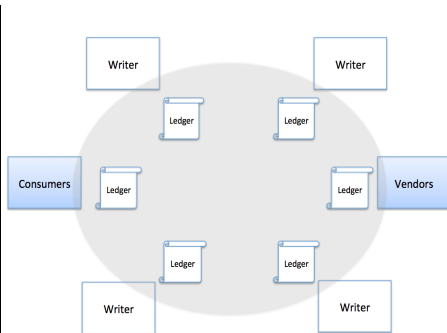
- **Centralized intermediaries** (traditional)
  - ▶ maintained by single, centralized agent
  - ▶ private
  - ▶ trusted because of franchise value
  
- **Blockchain technology** (new alternative)
  - ▶ maintained by many anonymous agents
  - ▶ publicly viewable
  - ▶ agreed-upon ledger
  - ▶ Large computational costs instead of franchise value

# When Centralized Intermediary, when Blockchain?

Main question: When is it *cheaper to secure* transactions via blockchain?

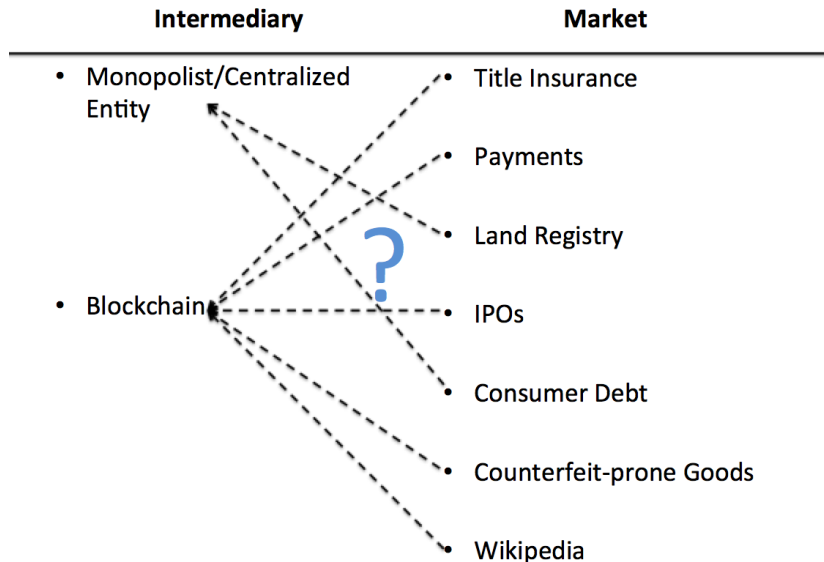


(a) Centralized record-keeping



(b) Decentralized record-keeping

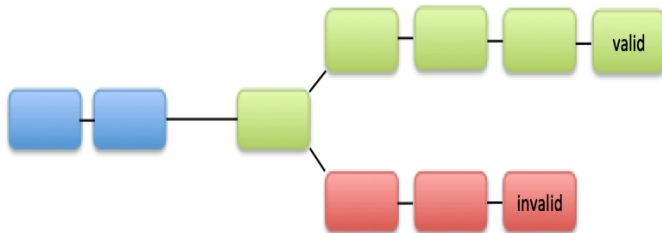
# When Centralized Intermediary, when Blockchain?



# What is a Blockchain?

- Blockchain is a **ledger** in which agents known as writers (or nodes) take turns writing on it.
  - ▶ Many ways to choose which writer records the state – discussed later.
- Ledger consists of a **tree of blocks**.
- Current **state** =
  - ▶ = longest “valid” chain.
  - ▶ = *entire chain* of transactions leading up to that block.
- **Validity** of a chain is determined by **public consensus**
  - ▶ Writers signal their acceptance of a block as valid by extending the chain corresponding to that block.
  - ▶ Writers earn rewards when their block is on the longest chain, so there are incentives for coordination.

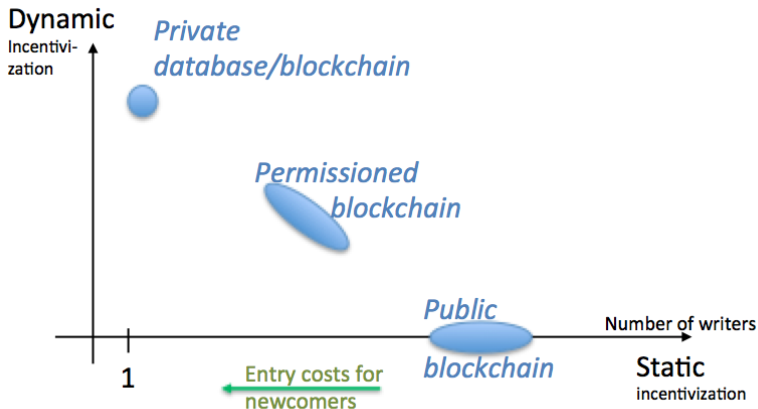
# What is a Blockchain? (cont.'d)



# Incentives Across the Spectrum



# Incentives Across the Spectrum





# Types of Blockchains

## Private Blockchain:

- *Written* by a centralized entity, but possibly *Readable* in real-time by the public or a regulator.
- Disciplined by readers of ledger (threat to leave blockchain)

## Permissioned Blockchain:

- *Write privileges* granted to consortium of entities  
*Read privileges* may be unrestricted.
- Writers are disciplined by those with read privileges **and other nodes**.

## Public Blockchain:

- Write and read privileges are unrestricted  $\Rightarrow$  Free entry!
- Writers are disciplined as in permissioned blockchains.
- Needs identity management: **proof-of-work**, proof-of-stake, etc.
  - ▶ Otherwise, Sybil attack:  
Create thousands of nodes to write the history you want.
  - ▶ real computational resource costs to add block  
(except if useful computations, like DNA decoding)
  - ▶ Compensation scheme  $\Leftarrow$  free entry condition

# When is Proof-of-Work Necessary?

- If readers/users refuse to trade on any ledger that's been attacked  
⇒ Private blockchain
- If writers refuse to build on any invalid block  
⇒ Permissioned blockchain
- Proof-of-Work:
  - 1 Readers/users can be “fooled” and trade on invalid ledgers.
  - 2 Writers are able to collude and steal from readers/users.

# Relation to Literature

- Rationale of PoW in many CS studies:  
PoW to defend against “double-spending” attacks
  - ▶ Writers obtain 51% of the network’s computing power and build long chains on which they didn’t spend certain coins.
- Most blockchain studies (CS and Econ):  
nobody can steal your assets or create new ones out of thin air.
- This paper:
  - ▶ mechanism to defend against arbitrary attacks
    - ★ Writers can write whatever they want (not just double-spending).
    - ★ Readers/users can freely choose (competing) ledger.
  - ▶ No need to assume fraction of “honest writers.”
  - ▶ No need to assume collusion is impossible ex-ante.

# Overview of Results

- Basic trade-offs (fee to incentivize writers)
  - ▶ Static: writer(s) “distort”  $\Rightarrow$  readers/users leave with higher prob.
  - ▶ Dynamic: franchise values
- **Security** of blockchain is guaranteed for two reasons:
  - ① *Joint attacks* by several writers are unprofitable because writers don't internalize the effects of their actions on others' profits.
  - ② *Collusion* in repeated setting is ruled out because of free entry
- **Efficiency** of blockchain  $>$  monopolistic intermediation (in static setting) when
  - ▶ The sensitivity of consensus to a writer's actions is small;
  - ▶ Franchise values are insensitive to deviations by the intermediary.
  - ▶  $\Rightarrow$  Optimal number of writers/monitors/miners
- **Ownership vs. Possession**
  - ▶ Blockchains don't guarantee secure transfer of possession, just ownership.
  - ▶ Blockchains with several writers are unable to discipline issuers of promises when they default.
  - ▶ Blockchains can't prevent monopolistic “enforcers” from selectively enforcing contracts.

# Roadmap

- ① What is a blockchain?
- ② Fee needed for “trustworthy” /incentivized
  - ▶ Blockchain with  $M$  miners/writers
  - ▶ Intermediary with 1 central record keeper
- ③ Ownership vs. possession (enforcement)

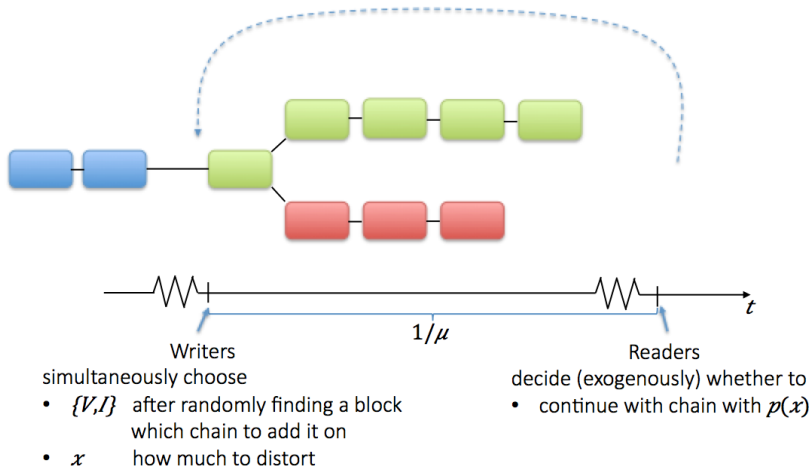
# Public Blockchain– Model Setup

- Agents:
  - ▶ Writers,  $M$ , who search for blocks
  - ▶ Free entry of writers  $\Rightarrow$  no dynamic play
  - ▶ Readers who “accept” blocks
- Time: continuous,  $t \in [0, \infty)$
- Blockchain:

Tree of blocks  $B^t = (B_1, \dots, B_n)$  with a partial order  $\prec_t$  satisfying the usual properties of a tree.

  - ▶ There is a minimal block and each block has a unique predecessor.
  - ▶ The tree can only be extended; blocks can't be erased or rearranged.
- Sequencing:
  - ▶ Writers' actions  $x$  (more later)
  - ▶ Readers choose chain of blocks
    - ★ At random points in time – Poisson arrival rate  $\mu$
    - ★ Readers' acceptance probability  $p(x)$ ,  
= function of writers' actions on a given chain
  - ▶ payoff's realize

# Summary



# Blockchains and Funding Limits

- **Lesson 1:**

Financial frictions are necessary for a blockchain to function!

- Writers exert costly computing power in order to “find” blocks. In each block, writers receive some transaction fees.
- Suppose writers have access to unlimited funding  $\Rightarrow$  single writer
  - ▶ If  $M$  writers each value their computers at  $Q$ , a single writer values  $M$  computers strictly more than  $MQ$ .
  - ▶ If a single writer owns all the computers, she extracts fees + monopolistic rents.
- *Assumption:*  
Each potential writer can only “afford” the same limited computing power.



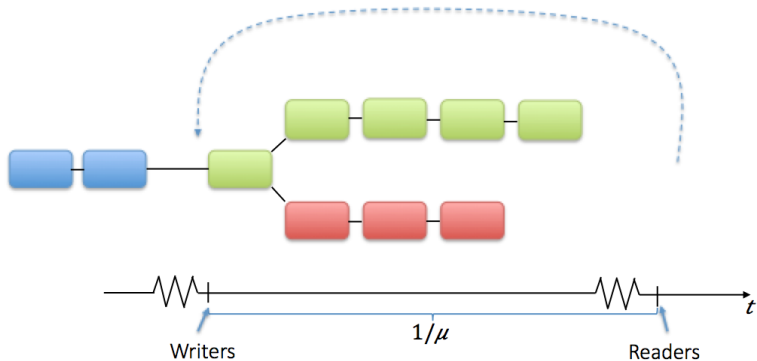
## Setup – Writers

- $k$  blocks that randomly arrive within window of random length  $1/\mu$
- Writers expend  $c$  units of computing resources in order to find blocks
  - ▶ arrive at rate  $\frac{\eta}{M}$  for an individual writer.
- Assume there are two chains of blocks:  
valid chain  $V$  and invalid chain  $I$ .
- Writing strategy:  $m_i \in \{V, I\}$
- Writer's action strategy:  $x_i \in [0, \bar{x}]$ 
  - ▶  $x$  = deviation from truth
- $n_V, n_I$  = number of blocks found on the valid and invalid chains,  
by a writer who plays action  $x$ .  
That writer's payoffs are
  - ▶  $\phi n_V$  if the valid chain is accepted
  - ▶  $(\phi + x)n_I$  if the invalid chain is accepted
- Free entry to become a writer:  $\frac{\eta\phi}{M} = c$

# Setup – Readers

- Readers choose whether to accept the valid or invalid chain.
- If valid chain is longer, they accept it automatically.
- If invalid chain is longer, they accept it w/ exogenous prob.  $1 - p(\hat{x})$ 
  - ▶  $\hat{x}$  = average action taken by writers
  - ▶  $p(\hat{x}) = 0$ , readers detect deviation immediately  
⇒ blockchain is automatically secure against any attack even with  $M = 1$ .
  - ▶ Recall at  $\hat{x} = \bar{x}$ ,  $p(\bar{x}) = 0$ .

# Summary



Writers  
simultaneously choose

- $\{V, I\}$  after randomly finding a block which chain to add it on
- $x$  how much to distort

Readers  
decide (exogenously) whether to

- continue with chain with  $p(x)$

# Equilibrium

## Lemma

In any equilibrium, all writers play on the same chain.

- Intuition: One writer can always mimic another writer's action and receive at least the same payoff.
- By playing on the same chain as another writer, the chance that the chain is accepted increases.
  - ▶  $\Rightarrow$  Higher payoffs for all writers on that chain
- Readers' preference for consensus (long chains) implies writers have an incentive to coordinate.

## Static Equilibrium Conditions

In an equilibrium in which all writers play on the invalid chain, a writer's optimization problem is

$$\max_x (\phi + x) E \left[ \left( 1 - p \left( \frac{k-n}{k} x^* + \frac{n}{k} x \right) \right) n \right]$$

The first-order condition in a symmetric equilibrium is

$$1 = \underbrace{\frac{p'(x^*)}{p(x^*)}}_{\text{hazard rate}} \frac{1}{\kappa(M)} (\phi + x^*)$$

where

$$\frac{1}{\kappa(M)} = \frac{1}{M} + \frac{M-1}{M} \frac{1}{E[k]}$$

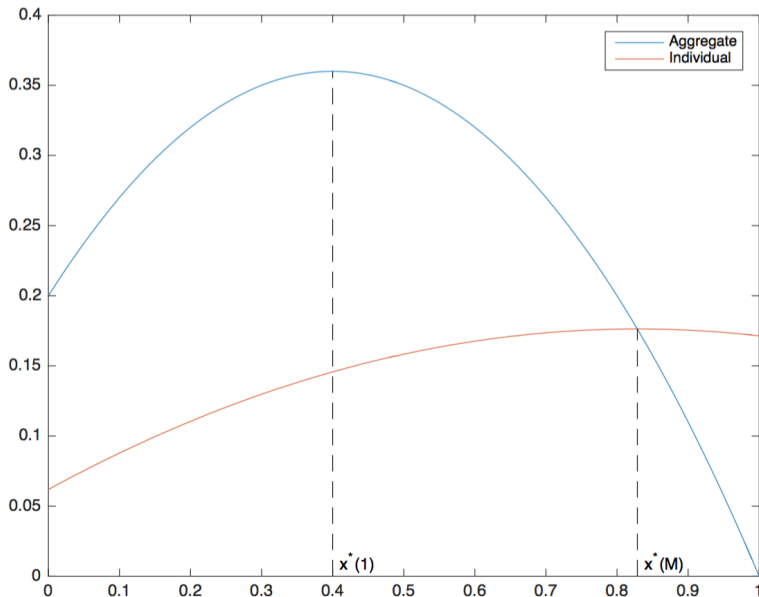
### Lemma

When expected number of blocks,  $E[k]$ , is sufficiently large, there is **no** equilibrium in which writers play on the **invalid chain** for large  $M$ .

# Why Are Attacks Unprofitable?

- 1 Each writer doesn't internalize the effect his action has on others' profits
- 2 Writers steal more than is optimal in aggregate;
- 3 The probability that readers reject the ledger increases;
- 4 Expected revenues on the invalid chain become lower than revenues on the valid chain;
- 5 Writers switch to the valid chain.

# Why Are Attacks Unprofitable? (cont.'d)



# Roadmap

- 1 What is a blockchain?
- 2 Model setup
- 3 Fee needed for “trustworthy” /incentivized
  - ▶ Blockchain with  $M$  miners/writers
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- 4 Ownership vs. possession (enforcement)



# Monopolistic Intermediary Benchmark

- no free entry  $\Rightarrow$  dynamic incentivization through franchise value
- Consider a monopolist who maintains a ledger and solves
  - ▶ Discount factor  $\delta$
  - ▶ Deviation  $x$  discovered with probability  $p(x)$
  - ▶ Intermediary forgiven with probability  $q$  on discovery

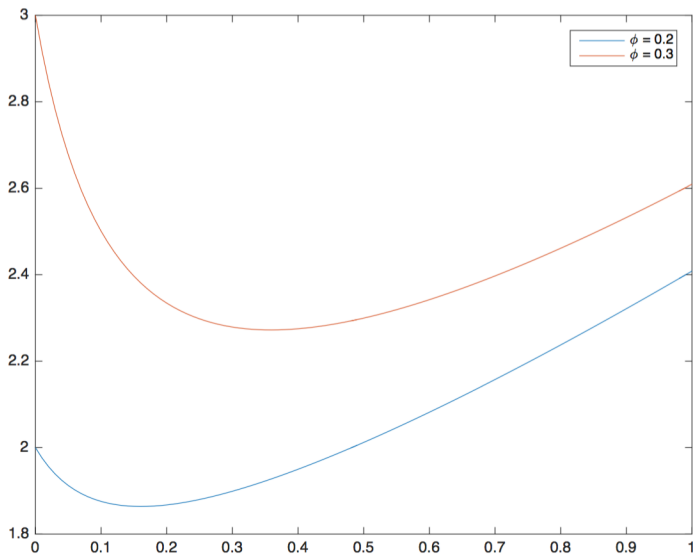
$$\max_x (\phi + x) + \delta(1 - p(x)(1 - q))(\phi + x) + \dots$$

$$\max_x \frac{\phi + x}{1 - \delta(1 - p(x)(1 - q))}$$

## Lemma

The intermediary chooses  $x = 0$  iff  $\phi \geq \frac{1-\delta}{\delta(1-q)}\bar{x} \equiv \underline{\phi}'$ .

# Monopolistic Intermediary Benchmark (cont.'d)



# Fee Comparison

- Can writers on a blockchain be incentivized to play  $x^* = 0$  for a **lower (aggregate) fee** than a monopolist?
- Let  $\bar{M} = \frac{\eta}{c} \phi^I$ . (How many miners can one afford instead of intermediary?)  
We want for some  $M \leq \bar{M}$ , deviation is not profitable, i.e.

$$(\phi(M) + x^*(M))(1 - p(x^*(M))) < \phi(M)$$

- *Example:* With  $p(x) = \pi x$ , this holds for some  $M \leq \bar{M}$  iff

$$\kappa(\bar{M}) < \frac{\delta}{1 - \delta}(1 - q)$$

# Fee Comparison - Optimal Number of Writers

- Approximate  $\kappa(\bar{M}) \approx E[k] = \frac{\eta}{\mu}$  (holds for large  $\bar{M}$ )

$$E[k] \approx \kappa(\bar{M}) < \frac{\delta}{1-\delta}(1-q)$$

⇒ independent of sensitivity  $\pi$ . (Recall  $p(x) = \pi x$ .)

- ⇒ **optimal number of writers:**

$$M^* = \frac{1}{\pi c T}$$

where  $T \equiv 1/\mu$  is the average length of a period.

- ▶ High  $\pi$  ⇒ Unprofitable theft for low  $M$
- ▶ High  $cT$  ⇒ Higher costs for the same  $M$

# Roadmap

- 1 What is a blockchain?
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- 3 Fee needed for stable
  - ▶ Blockchain with  $M$  miners/writers
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- 4 Ownership vs. possession (enforcement)
  - ▶ Blockchain with a monopolistic enforcer (government)
  - ▶ Blockchain with defaultable promises

# Blockchain: Ownership vs. Possession

- Several blockchain proposals involve using blockchains as ownership databases for all kinds of assets– not just cryptocurrencies.
  - ▶ E.g. WSJ: "How Blockchain Can End Poverty"
- So far: ignored distinction between **ownership** and **possession**.
  - ▶ *Ownership* is traded in the secondary market
  - ▶ *Possession* is conferred by the previous possessor and enforced by some entity
- **Currency** is the outlier: no fundamental value.
- Blockchain is good for determining ownership but not possession.
  - ▶ No security against an enforcer who selectively enforces contracts.
  - ▶ Provides security when issuers want to coordinate with intermediaries.
  - ▶ No discipline for issuers who want to default.

# Blockchain and Enforcement

- There is an enforcer and  $M$  writers.
- The enforcer does not like enforcing contracts and chooses how many to enforce.
- Writers choose how much to cooperate with the enforcer and receive bribes for doing so.
  - ▶ E.g. writers could erase ownership records for land the government wants to seize.
  - ▶ More bribes  $\Rightarrow$  greater probability of detection
- Main result: The equilibrium is independent of the number of miners.
  - ▶ More miners  $\nrightarrow$  more security!
  - ▶ The enforcer can control the extent of deviations by choosing how much to bribe.
  - ▶ The enforcer makes sure writers never steal too much and get detected.

# Intermediation with Defaultable Promises

- $M$  writers
- Continuum of issuers
  - ▶ Each wants to default on promise on ledger
  - ▶ Try to bribe writers to cooperate with default
    - ★ Example:  
Company bribes an exchange to lie, says shares it issues are authentic
- Two cases for issuers:
  - ▶ Issuers want to *coordinate* default with writers  
⇒ Same problem as before
  - ▶ Default is *dominant*: can issuers be disciplined?
- Writers may choose to deny service to issuers ⇒ zero payoff
  - ▶ No denial of service in a static setting  
⇒ Dynamic setting is needed



# Discussion

- Our examples follow from two main results:
  - ① **Security:**  
Selfish incentives to steal make joint ledger distortion unprofitable.
  - ② **No Collusion:**  
Free entry  $\Rightarrow$  No off-equilibrium punishments/rewards.
- In contrast to CS literature
  - ▶ No need to assume fraction of “honest writers.”
  - ▶ No need to assume collusion is impossible ex-ante.
    - ★ This emerges naturally from the free entry condition.
    - ★ Ex-ante impossible collusion  $\Rightarrow$  No PoW.

# When anonymous PoW blockchain

- Markets where reputations are insensitive to deviations
  - ▶ E.g., TBTF
- Markets where issuers want to coordinate deviations with intermediaries
  - ▶ E.g. Title insurance, counterfeiting, IPOs
- **Not** with monopolistic enforcers.
  - ▶ E.g. Land registries
- **Not** when issuers need to be disciplined.
  - ▶ E.g. Consumer debt markets

# Conclusions

