# Downward Nominal Wage Rigidity in Canada: Evidence against a 'Greasing Effect'

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### Downward Nominal Wage Rigidity

#### Motivation

- For a variety of reasons workers as well as firms are often reluctant to lower wages in response to poor labour-market conditions.
- As a result, DNWR *could* cause labour-market corrections occur disproportionately through the employment margins rather than through reduced wages.
- These downward nominal wage rigidities (DNWR) have been identified as a justification for positive inflation targets.

### Main Questions

#### Questions

- To what extend does DNWR explain the joint dynamics of unemployment and wage inflation in Canada?
- Do higher inflation targets cause a 'Greasing Effect' in the short run?

#### Answers

- Evidence of DNWR in Canada. DNWR helps explain the joint dynamics of unemployment and wage inflation during the Great Recession.
- Higher inflation targets <u>do not</u> shorten the overall recovery time nor attenuate the response of unemployment.

## Downward Nominal Wage Rigidity

#### DNWR in Canada

- Brouillete, D., Kostyshyna O. and N. Kyui, (2015a)
  - Evidence suggests that DNWR increased in Canada during the Great Recession.



Downward Nominal Wage Rigidity



## Model

### **Model Framework**

- DGE model with DNWR by Daly and Hobijn (2014).
- Each period a random fraction  $\lambda$  of workers will be unable to adjust wages downward (if required).
- The household is populated by members with a variety of costlessly differentiable labour types.
- Agents are forward looking and make optimal wage setting decisions in response to:
  - Aggregate shocks: Productivity and Preference shocks
  - Idiosyncratic shocks: Labour disutility shock
- Goods production is perfectly competitive

### Households

Households Lifetime Utility

$$\sum_{t=0}^{\infty} \beta^t e^{-\sum_{s=0}^{t-1} D_s} \left[ \ln C_t - \frac{\gamma}{\gamma+1} \int_0^1 Z_{it} L_{it}^{\frac{\gamma+1}{\gamma}} di \right], \ \gamma > 0$$

- *C<sub>t</sub>* household consumption
- Lit labour supplied by member i of the household
- $Z_{it}$  denotes the time dependent idiosyncratic disutility

• where 
$$ln(Z)$$
 is  $N\left(-\frac{\sigma^2}{2},\sigma\right)$  with  $E(Z) = 1$ .

•  $D_{\rm s}$  is a preference shock,  $\beta$  subjective discount factor,  $\gamma$  the Frisch elasticity of labour supply

Household's budget constraint

$$B_t + P_t C_t = (1 + i_{t-1})B_{t-1} + \int_0^1 W_{it} L_{it} di.$$

### Firms

Production

$$Y_t = A_t L_t.$$
  
 $A_t = (1 + a_t)A_{t-1}$ 

Production Technology

Aggregate Labour

$$L_t = \left[\int_0^1 L_{it}^{\frac{\eta-1}{\eta}} di\right]^{\frac{\eta}{\eta-1}}$$

Labour Demand Function

$$L_{it} = \left(\frac{W_t}{W_{it}}\right)^{\eta} L_t$$

Aggregate Wage Rate

$$W_t = \left[\int_0^1 \left(\frac{1}{W_{it}}\right)^{\eta-1} di\right]^{-\frac{1}{\eta-1}}$$

### Downward Wage Rigidity

With DNWR, a fraction of the household members  $\lambda$  are unable to adjust wages downward ( $w' \ge w$ ) when required

Household member i maximize

$$V_{t}(w) = (1 - \lambda) \int_{0}^{\infty} \max_{w_{it} \ge 0} \left( \Omega(Z_{it}, w_{it}, L_{t}) + \beta e^{-D_{t}} V_{t+1}(w') \right) dF(Z_{it})$$
$$+ \lambda \int_{0}^{\infty} \max_{w_{it} \ge w} \left( \Omega(Z_{it}, w_{it}, L_{t}) + \beta e^{-D_{t}} V_{t+1}(w') \right) dF(Z_{it}).$$

Where  $F(Z_{it})$  denotes the distribution of the idiosyncratic disutility shock  $Z_{it}$ 

$$\Omega(Z_{it}, w_{it}, L_t) = w_{it}^{1-\eta} - \frac{\gamma}{\gamma+1} Z_{it} w_{it}^{-\eta\frac{\gamma+1}{\gamma}} L_t^{\frac{\gamma+1}{\gamma}}$$

Detrended real wage in period t + 1 is

$$w' = w_{it}/((1+\pi_{t+1})(1+a_{t+1}))$$

### Downward Wage Rigidity

#### Labour supply

$$L_t = \left(\frac{\eta - 1}{\eta}\right)^{\frac{\gamma}{1 + \gamma}} \left(\frac{1}{Z_t^*}\right)^{\frac{\gamma}{1 + \gamma}}$$

Aggregate disutility

$$\begin{split} Z_t^* &= \left( (1-\lambda) \int_0^\infty \left(\frac{1}{Z_{it}}\right)^{\frac{\gamma(\eta-1)}{\eta+\gamma}} \left(\frac{w_t^f(Z_{it})}{w_t^*(Z_{it})}\right)^{\eta-1} dF(Z_{it}) \\ &+ \lambda \int_0^\infty \left(\frac{1}{Z_{it}}\right)^{\frac{\gamma(\eta-1)}{\eta+\gamma}} G_{t-1} \left(w_t^*(Z_{it})(1+\pi_t)(1+\mathfrak{d}_t)\right) \left(\frac{w_t^f(Z_{it})}{w_t^*(Z_{it})}\right)^{\eta-1} dF(Z_{it}) \\ &+ \lambda \int_0^\infty \left(\frac{1}{Z_{it}}\right)^{\frac{\gamma(\eta-1)}{\eta+\gamma}} \left[ \int_{w_t^*(Z_{it})}^\infty (1+\pi_t)g_{t-1} \left(w(1+\pi_t)(1+\mathfrak{d}_t)\right) \left(\frac{w_t^f(Z_{it})}{w_t^*(Z_{it})}\right)^{\eta-1} dw \right] dF(Z_{it}) \\ \end{split}$$

where  $G_t(w)$  is the distribution of real wages across workers

### Monetary Policy

#### **Taylor Rule**

$$i_t = rac{(1+ar{\pi})(1+ar{a})}{eta} \left(rac{y_t}{ar{y}}
ight)^{\phi^Y} \left(rac{1+\pi_t}{1+ar{\pi}}
ight)^{1+\phi^\pi} - 1$$

- $\bar{\pi}$  and  $\bar{a}$  are steady-state inflation and growth rates respectively.
- $\frac{y_t}{\bar{v}}$  is the output gap with  $\phi^Y$  its weight.
- $\frac{1+\pi_t}{1+\pi}$  is the inflation gap with  $1+\phi^{\pi}$  its weight.
- $r_t = (1 + i_t)/(1 + \pi_{t+1}) 1$

# Calibration

Parameters	Function	Value
η	Labour demand elasticity	1.33
$\gamma$	Frisch elasticity of labour supply	0.5
$\beta$	Discount factor	0.9921
$\bar{\pi}$	Target inflation	0.005
$\phi^Y$	Taylor rule parameter for the output gap	1
$\phi^{\pi}$	Taylor rule parameter for the inflation gap	0.3
ā	Technological growth rate	0.005
$\sigma$	Standard deviation of the idiosyn- cratic disutility shock to labour	0.294
$\epsilon^{D}$	Size of the demand shock	-0.0124
$\rho^D$	Persistence of the demand shock	0.95
$\lambda$	Calvo parameter for wages	(0.40, 0.70, 0.85, 0.99)

### Results: Roadmap

### Two Specific Questions:

- To what extend does DNWR explain the joint dynamics of unemployment and wage inflation following an economic downturn in Canada?
- Do higher inflation targets cause a 'Greasing Effect' in the short run?

#### DNWR over the Business Cycle

# Evolution of the SRAS and the AD Curve to a Negative Demand Shock



#### Impulse Response Functions



(a) Interest Rates (Annualized)



Increase in the Percentage (c) of Workforce Accepting a Nominal Wage Freeze





(b) Wage Inflation (Annualized)



(d) Unemployment Gap

 $\lambda = (0.40, 0.70, 0.85, 0.99)$ 

Response to a Negative Demand Shock

#### Short-Run Phillips Curves Varying Degrees of DNWR



### Response to a Negative Demand Shock

#### Wage Growth Distribution



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### DNWR over the Business Cycle

#### Wage Growth Distribution



#### **Impulse Response Functions**



#### **Negative Demand Shock**



Increase in the Percentage (c) of Workforce Accepting a Nominal Wage Freeze Martine Contract of the Contra

#### (b) Wage Inflation (Annualized)



(d) Unemployment Gap

 $\bar{\pi} = (1\%, 2\%, 5\%)$ 

## Conclusion

#### Main Questions

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#### Answer

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