

Endogenous Wage Indexation and Aggregate Shocks

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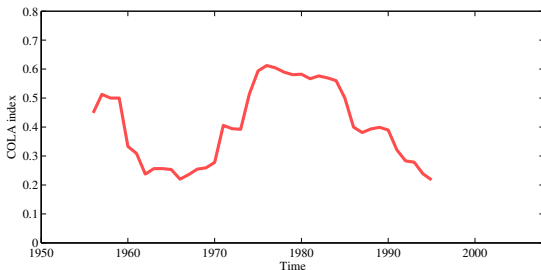
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Motivation

- ▶ Price and wage inflation are typically very persistent
- ▶ DSGEs assume prices and wages are **indexed to past inflation**
(To fix terms: **Aggregate indexation = past-inflation indexation**)
- ▶ Indexation is **hard-wired** as a fixed and policy invariant parameter
- ▶ But indexation practices are choices/agreements between agents
- ▶ Why should they remain permanently constant? (Lucas critique)
- ▶ Evidence suggests wage indexation has varied a lot

Motivation

- ▶ **Macro evidence for U.S.:** Hofmann, Peersman, and Straub (2012) find that U.S. wage dynamics are consistent with
 - ▶ high indexation for the *Great Inflation* (70s), and
 - ▶ low indexation for the *Great Moderation* (2000s)
- ▶ **Micro evidence for U.S.:** # contracts with cost-of-living adj. (COLA) clauses



- ▶ **Macro evidence for Europe:** Wage negotiations are starting to follow observed inflation rather than the ECB's inflation target.

Motivation

- ▶ High wage indexation renders inflation more persistence, making it more difficult to bring it back to target.
- ▶ Gray (1976) and Fischer (1977) offer a rationale for *socially optimal* changes in wage indexation
- ▶ To reduce output fluctuations, wage indexation should
 - ▶ decrease with supply-side shocks, and
 - ▶ increase with demand-side shocks.
- ▶ However, the Gray-Fischer hypothesis is problematic for two reasons:
 - ▶ Did demand shocks drive the 70s and supply shocks the 2000s?
 - ▶ The U.S. is driven by a decentralized wage setting (Calmfors and Driffil, 1988).

- ▶ Within a microfounded environment, we ask

Which macro factors influence workers' wage indexation choices?

- ▶ We proceed as follows:
 - ▶ In a stylised NK-DSGE model,
 - ▶ Utility-maximizing workers select a wage indexation rule:
past inflation or inflation target.
 - ▶ Workers respond to prevailing shocks, policy, and market structures.
 - ▶ We use the model's predictions to ask: **What caused wage indexation changes in the U.S.?**

1. Workers index wages to
 - ▶ **past inflation** in face of **perm. productivity and inflation-target shocks**
 - ▶ **target inflation** in face of **aggregate-demand shocks**
2. The decentralized wage indexation equilibrium carries an externality
 - ▶ Social planner choices are different than decentralised equilibrium
 - ▶ A worker does not internalise the effect of his choice on the aggregate
3. Model correctly predicts
 - ▶ high aggregate indexation for the *Great Inflation* and
 - ▶ low aggregate indexation for the *Great Moderation*
 - ▶ Changes in the volatility of **productivity shocks** drive results

Model building blocks

- ▶ New Keynesian model with sticky prices and wages (Erceg, Henderson, and Levin, 2000)
 - ▶ Linear technology on labor with no capital
 - ▶ Monetary policy: CB follows Taylor-type rule and sets inflation target
 - ▶ Shocks: Technology (perm.), Gov't spending (temp.), Target inflation
- ▶ Households have a unique labor type
 - ▶ Re-optimize labor contract infrequently
 - ▶ Step 1, HH choose *indexation rule given economic structure*
 - ▶ Step 2, HH choose *optimal wage given indexation rule*
 - ▶ In both steps, HH maximise expected utility

It is illustrative to analyse step 2 first, and then step 1

Households, step 2: wage-setting

- ▶ Household i 's objective is

$$\max_{c_{i,T}, b_{i,T}, W_{i,t}^k} E_t \left\{ \sum_{T=t}^{\infty} \beta^{T-t} \left(\log \left(c_{i,t} - \gamma^h c_{i,t-1} \right) - \psi \frac{(\ell_{i,t,T})^{1+\omega}}{1+\omega} \right) \right\}, \quad (1)$$

subject to

$$c_{i,T} + \frac{b_{i,T}}{R_T} \leq \frac{W_{i,t}^k}{P_T} \ell_{i,T} + \frac{b_{i,T-1}}{1+\pi_T} + \frac{Y_{i,T}}{P_T}, \quad (2)$$

$$\ell_{i,t,T}^k = \left(\frac{\delta_{t,T}^k W_{i,t}^k}{W_T} \right)^{-\theta_w} \ell_T \quad (3)$$

- ▶ HH sets new contract with probability $1 - \alpha_w$
- ▶ Available indexation rules are

$$\delta_{t-1,t}^{trend} = 1 + \pi_t^* \quad \text{and} \quad \delta_{t-1,t}^{past} = 1 + \pi_{t-1}$$

π_t^* is the central bank inflation target = trend inflation.

Households, step 2: costs from sticky wages

- ▶ If wages were flexible, usual *welfare maximizing* condition holds

Mg. rate of substitution between $c_{i,t}$ and $l_{i,t} \propto$ real wage

$$\frac{\psi \ell_t^\omega}{\lambda_t} = \frac{w_t}{\mu_w}.$$

- ▶ Since wages are sticky, this condition may not be satisfied
- ▶ Sticky wages imply welfare losses,
- ▶ but an indexation rule may close the gap between the desired and actual labor supply

Households, step 1: indexation-rule setting

- ▶ Workers select an indexation rule to maximise expected utility

$$\max_{\delta_i \in \{\delta^{trend}, \delta^{past}\}} E_t \left\{ \sum_{T=t}^{\infty} (\beta \alpha_w)^{T-t} \mathcal{U}(c_T(\xi_T, \Sigma_T), \ell_{i,T}(\delta_i, \xi_T, \Sigma_T)) \right\},$$

subject to the economy's structure, Σ_t

- ▶ $\Rightarrow c_t$ does not depend on δ_i^* (perfect risk sharing)
 - ▶ \Rightarrow Only expected labor disutility matters
- ▶ A worker chooses δ_i^* to minimize

$$\Omega_{i,t}(\delta_i, \xi_t) = E_t \left\{ \sum_{T=t}^{\infty} (\beta \alpha_w)^{T-t} \frac{\psi}{1+\omega} \ell_{i,T}^{1+\omega} \right\}$$

$\xi_t = \#$ workers indexing to past inflation, **taken as given by an individual worker**

Shocks & Policy

- ▶ Productivity shock:

$$y_{j,t} = A \exp(z_t) n_{j,t}, \text{ with } z_t = z_{t-1} + \varepsilon_{z,t},$$

- ▶ Government-spending shock (aggregate-demand shock):

$$g_t = g \exp(\varepsilon_{g,t}) y_t \text{ with } \varepsilon_{g,t} = \rho_g \varepsilon_{g,t} + \eta_{g,t},$$

- ▶ Monetary policy:

- ▶ Interest-rate rule:

$$R_t = [R_{t-1}]^{\rho_R} [R_t^*]^{1-\rho_R} \left[\frac{1 + \pi_t}{1 + \pi_t^*} \right]^{a_\pi(1-\rho_R)} [y_t]^{a_y(1-\rho_R)} \left[\frac{y_t}{y_{t-1}} \right]^{a_{\Delta y}},$$

where R_t^* is the long-term gross nominal rate

- ▶ Trend-inflation rule:

$$\pi_{t+1}^* = \rho_{\pi^*} \pi_t^* + \varepsilon_{\pi,t+1} \text{ with } \rho_{\pi^*} \in [0, 1].$$

Benchmark calibration

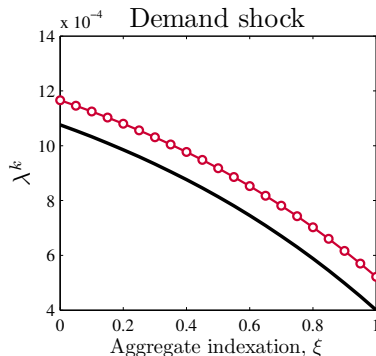
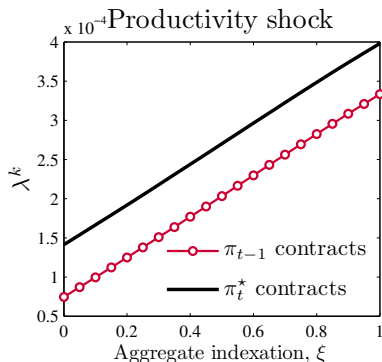
Table 1. Calibration based on HPS (2012)'s estimation

| | Great Moderation year 2000 |
|---|-------------------------------|
| γ^h Habit formation | .37 |
| γ^p Inflation inertia | .17 |
| α_p Calvo-price rigidity | .78 |
| α_w Calvo-wage rigidity | .54 |
| a_π Taylor Rule: inflation | 1.35 |
| a_y Taylor Rule: output gap | .1 |
| $a_{\Delta y}$ Taylor Rule: output gap growth | .39 |
| ρ_R Taylor Rule: smoothing | .78 |

Other parameters: $\beta = .99$, $\sigma = 1$, $\phi = 1$, $\omega = 2$, $\theta_w = \theta_p = 10$.

Aggregate indexation: welfare costs I

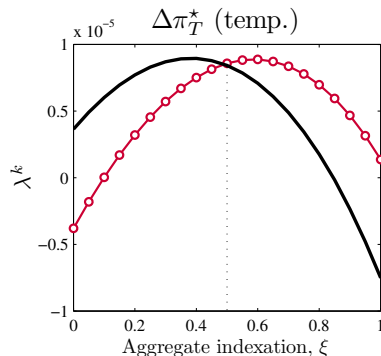
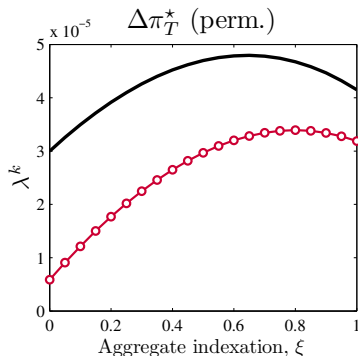
- Welfare costs are approx to the second order (leisure-equivalent λ_k)



- Workers pick *past* index. in the productivity shock regime
- Workers pick *trend* index. in the gov't spending regime
- The equilibria are globally stable

Aggregate indexation: welfare costs II

(black is trend and red is past)



- ▶ If the π^* -shocks are permanent, then workers pick *past* index.
- ▶ If the π^* -shocks are temporal, there's an interior solution
- ▶ Again, the equilibria are globally stable

Labor disutility at the steady state

- ▶ At the steady state, labor disutility is given by (let $\omega = 1$)

$$\Omega_{ss}^k \approx \frac{\psi}{1 - \beta\alpha_w} (R_{ss}^k + V_{ss}^k),$$

where

$$R_{ss}^k = \frac{1}{2} \left[\frac{\int_{i \in I_k} \left(\frac{W_i}{W} \right)^{-\theta_w} di}{\zeta^k} \times \ell_{ss} \right]^2, \text{ and } V_{ss}^k = \frac{1}{2} \text{var} \left(\ell_t^k \right)$$

where $\zeta^k = \zeta$ if $k = \textit{past}$ and $1 - \zeta$ if $k = \textit{trend}$

- ▶ R_{ss}^k depends on wage dispersion within a sector
- ▶ V_{ss}^k is a total measure of variance in hours worked
- ▶ We show that differences in R_{ss}^k are the main drivers of wage indexation decisions

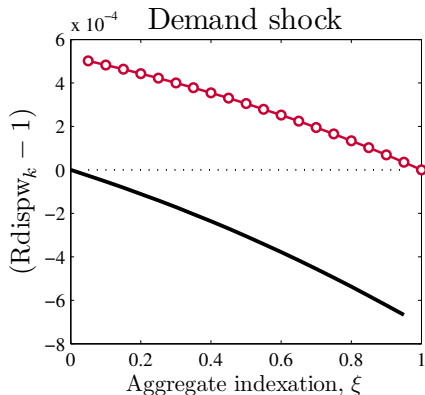
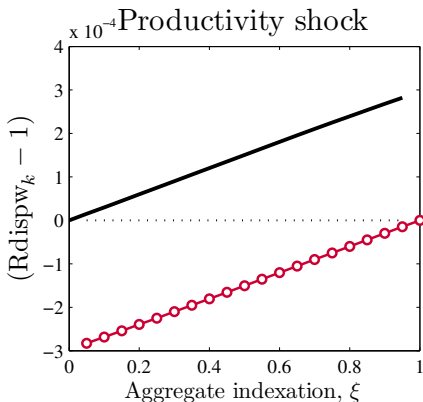
Labor contracts: Intuition

- ▶ How workers choose their indexation rule?
- ▶ Here's the intuition:
 - ▶ A larger wage dispersion means a larger variance in hours worked,
 - ▶ Workers dislike uncertainty on their labor and wages ($\omega > 0$),
 - ▶ So they choose a labor contract (δ^k, W^k) that minimizes that uncertainty.

Relative wage dispersion I

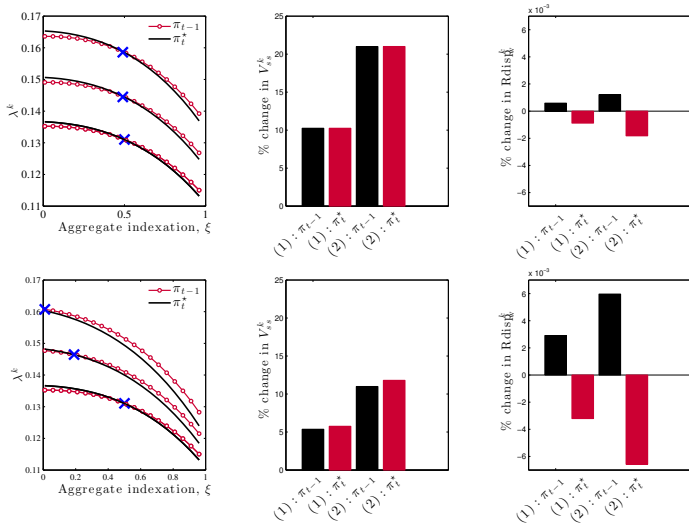
- ▶ In single-shock regimes, workers prefer contracts with lower relative wage dispersion

(black is trend and red is past)



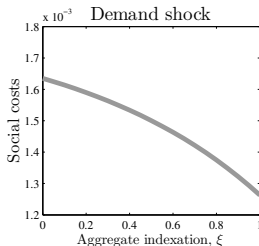
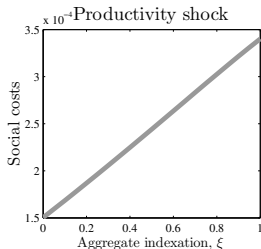
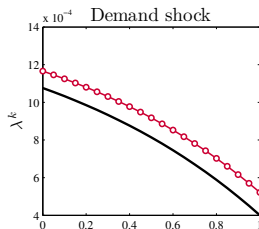
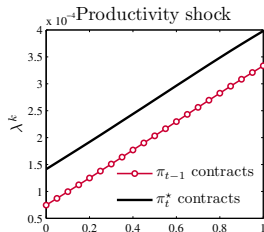
Relative wage dispersion II

- ▶ In multiple-shocks regimes, changes in relative wage dispersion drive changes in aggregate indexation



Social planner vs. Decentralized eq

- ▶ A worker disregards his own impact on the aggregate
- ▶ Coordination failure leads to a suboptimal equilibrium



Great Inflation calibration

Table 2. Calibration based on HPS (2012)'s estimation

| | Great Moderation 2000 (benchmark) | Great Inflation 1974 |
|---|--------------------------------------|-------------------------|
| γ^h Habit formation | .37 | .71 |
| γ^p Inflation inertia | .17 | .8 |
| α_p Calvo-price rigidity | .78 | .84 |
| α_w Calvo-wage rigidity | .54 | .64 |
| a_π Taylor Rule: inflation | 1.35 | 1.11 |
| a_y Taylor Rule: output gap | .10 | .11 |
| $a_{\Delta y}$ Taylor Rule: output gap growth | .39 | .5 |
| ρ_R Taylor Rule: smoothing | .78 | .69 |

Common parameters: $\beta = .99$, $\sigma = 1$, $\phi = 1$, $\omega = 2$, $\theta_w = \theta_p = 10$.

Predictions for U.S.

Table 3. Calibration of shocks

| | | Great Moderation 2000 (benchmark) | Great Inflation 1974 |
|---|--|--------------------------------------|-------------------------|
| σ_z | Std. dev. Tech. shock (HPS) | .31 | 1.02 |
| σ_g | Std. dev. Dem. shock (HPS) | 3.25 | 4.73 |
| σ_{π^*} | Std. dev. inflation target (HPS) | NaN | NaN |
| $\hat{\chi}$ | Estimated indexation (HPS) | .17 | .91 |
| Case 1: $\sigma_{\pi^*} = 0$ | | | |
| χ^* | Implied equilibrium indexation | 0 | .89 |
| χ^S | Implied social optimum | 1 | 0 |
| Case 2: $\sigma_{\pi^*} > 0$ | | | |
| σ_{π^*} | Std. dev. inflation target (CPS, 2010) | .049 | .081 |
| χ^* | Implied equilibrium indexation | .05 | .89 |
| χ^S | Implied social optimum | 1 | 0 |

Counterfactuals

Table 4. Counterfactual exercises

| | 2000: $\zeta^* = 0$, put 1974 value to: $\zeta^{counterfactual}$ | 1974: $\zeta^* = .89$, put 2000 value to: $\zeta^{counterfactual}$ |
|---|---|---|
| I - Shocks | | |
| σ_z Std. dev. Tech. shock | 1 | 0 |
| σ_g Std. dev. Dem. shock | 0 | 1 |
| σ_{π^*} Std. dev. inflation target | .6 | .89 |
| II - Policy parameters | | |
| a_{π} Taylor Rule: inflation | 0 | 1 |
| a_y Taylor Rule: output gap | .05 | .89 |
| $a_{\Delta y}$ Taylor Rule: output gap growth | 0 | 1 |
| ρ_R Taylor Rule: smoothing | 0 | .94 |

Remarks: Main driver is change in the volatility of the productivity shock, not monetary policy!

Extra: What can we say for SOEs?

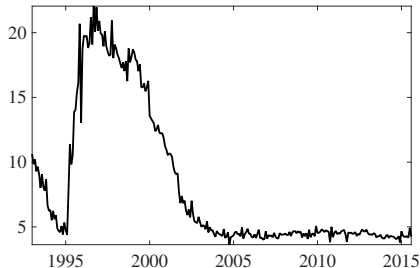
- ▶ Evidence suggest that wage indexation has also changed in Mexico
- ▶ Consider the following regression for Mexican employees' **contractual wage revisions**, Δw_t

$$\Delta w_t = c_t + \rho_t \Delta w_{t-1} + \beta_{lag,t} \sum_{i=0}^{12} \pi_{t-i} + \beta_{trend,t} \bar{\pi}_t + \gamma_t \Delta s_t + \varepsilon_t$$

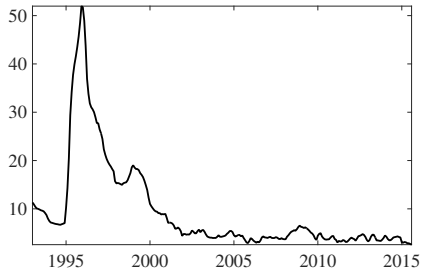
- ▶ where Δs_t is the percent change in the peso/dollar exchange rate, and c_t , ρ_t , $\beta_{lag,t}$, $\beta_{trend,t}$, and γ_t are time-varying coefficients

Extra: Mexico 1993-2015, monthly data

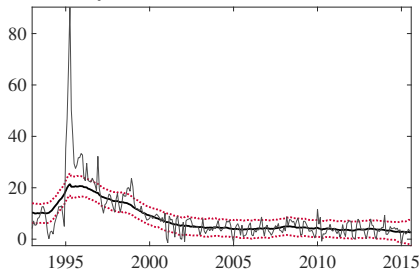
Nominal wage revisions



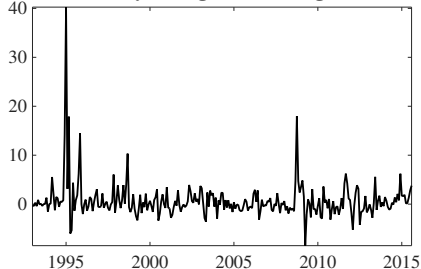
Cumulated annual inflation (lagged)



Monthly inflation (annualized) and trend

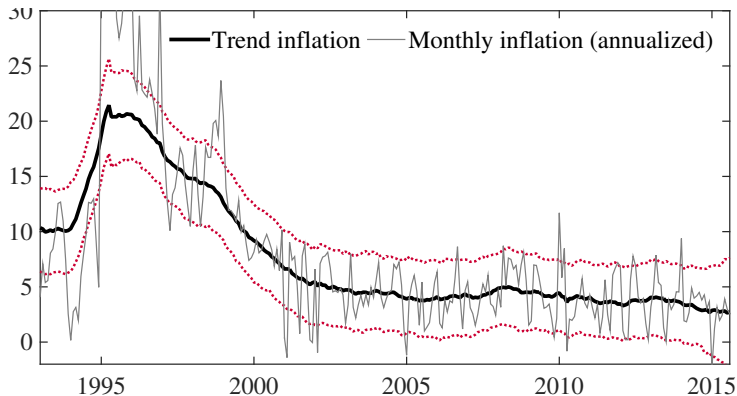


Monthly change in exchange rate



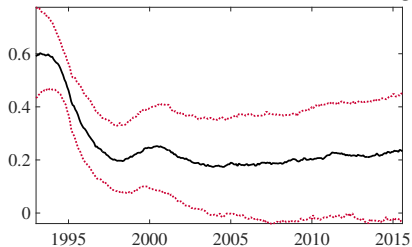
Extra: Predictions for Mexico

- ▶ According to the theory, wage indexation to past inflation should have been high in the 90s, and low in the 2000s

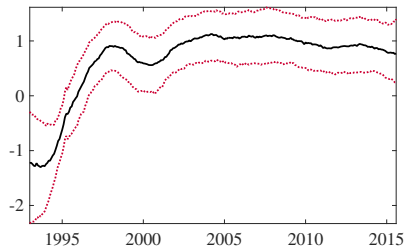


Extra: Predictions for Mexico

Long-run lagged-inflation coef. $((1-\rho_t)^{-1}\beta_{\text{lag},t})$



Long-run trend-inflation coef. $((1-\rho_t)^{-1}\beta_{\text{trend},t})$



- ▶ As expected, wage revisions followed more past inflation in the 90s, when trend inflation was drifting
- ▶ When trend inflation settled, wage revisions followed this variable

Conclusions

- ▶ We propose a microfounded approach to endogenize wage indexation in DSGE models
- ▶ We let workers select their own indexation rule
 - ▶ Expected changes in hour worked (aka, relative wage dispersion) is the most important driver in a worker's decision
 - ▶ However, this decentralized equilibrium suffers from an externality and is suboptimal
- ▶ The decentralized equilibrium offers a rationale to changes in U.S. wage indexation from the Great Inflation to the Great Moderation
- ▶ And it may offer predictions to SOEs too