

The Role of Industrial Composition in Driving the Frequency of Price Change

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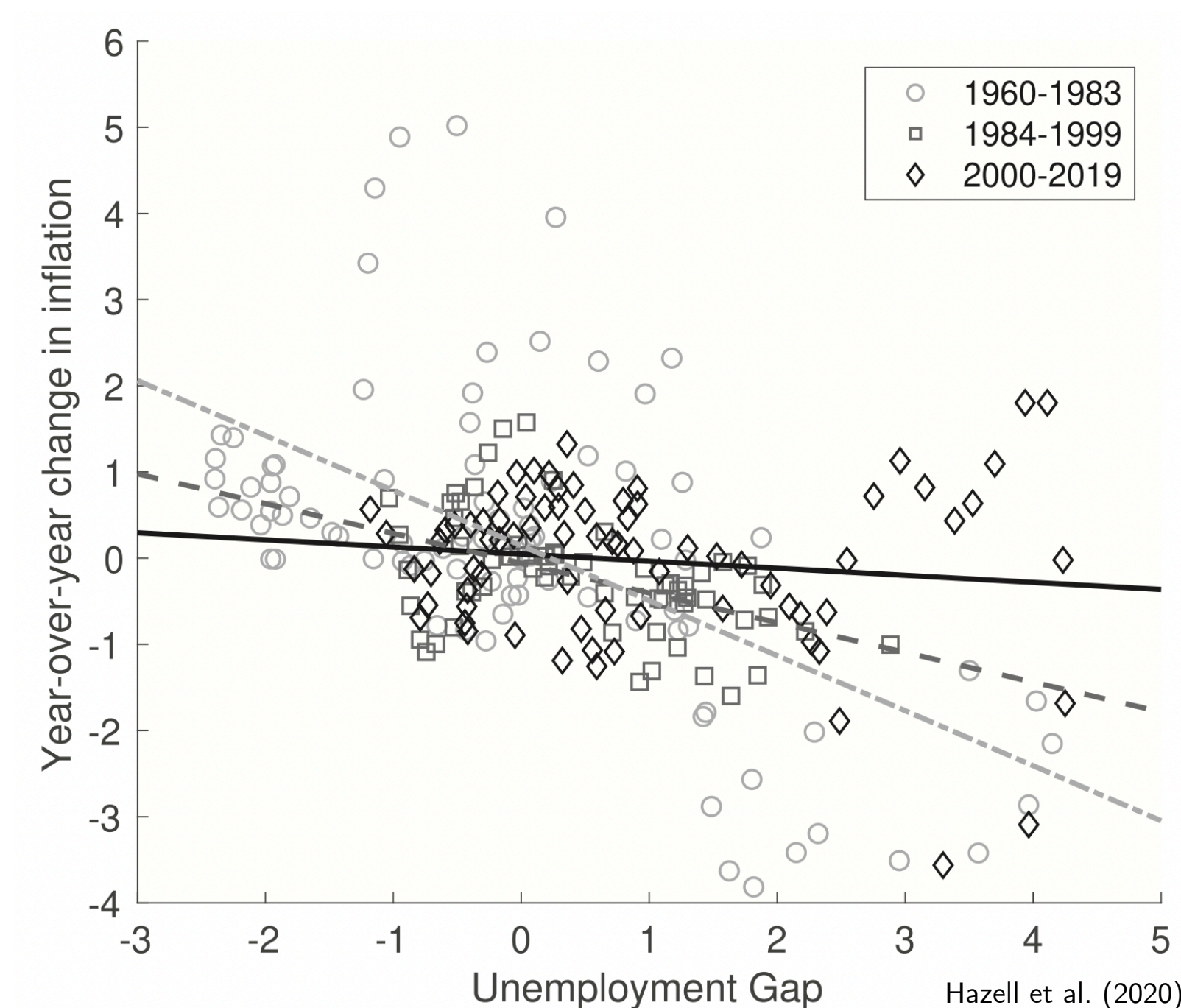
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Motivation

- **Frequency of price change:** crucial parameter in monetary economics
 - Extent of transmission of nominal shocks to the real economy
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- **Long-term decline** in the slope of the Phillips curve in the United States (US)
- One potential reason for the slope decline: fall in the frequency of price change
- Natural candidate to explain the decline: **long-term structural changes**
 - **Changes in industrial composition**

Goals

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- Impact of changes in industrial composition on the aggregate frequency of price change
 - Empirical
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 - Empirical
- Consequent impact on the slope of the Phillips curve
 - Quantitative model
- Focus: US, 1947–2019
 - Methodology general and more broadly applicable
 - Other countries/time periods/price-change statistics

Related Literature

Heterogeneity in frequency of price change across products in monetary models

Nakamura and Steinsson (2008, 2010), Carvalho (2006)

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Reasons for the decline in the slope of the Phillips curve

Del Negro et al. (2020), Mangiante (2022), Crump et al. (2019), Daly and Hobijn (2014), Moscarini and Postel-Vinay (2018), Daly and Hobijn (2014), Bernanke et al. (2010), Jørgensen and Lansing (2019), Borio and Filardo (2007), Iakova (2007), Rubbo (2020), Mangiante (2022), Kaihatsu, Katagiri, and Shiraki (2022)

This paper: simple explanation for why there has been a long-term decline in the slope from late 1940s–present

Empirical Methodology

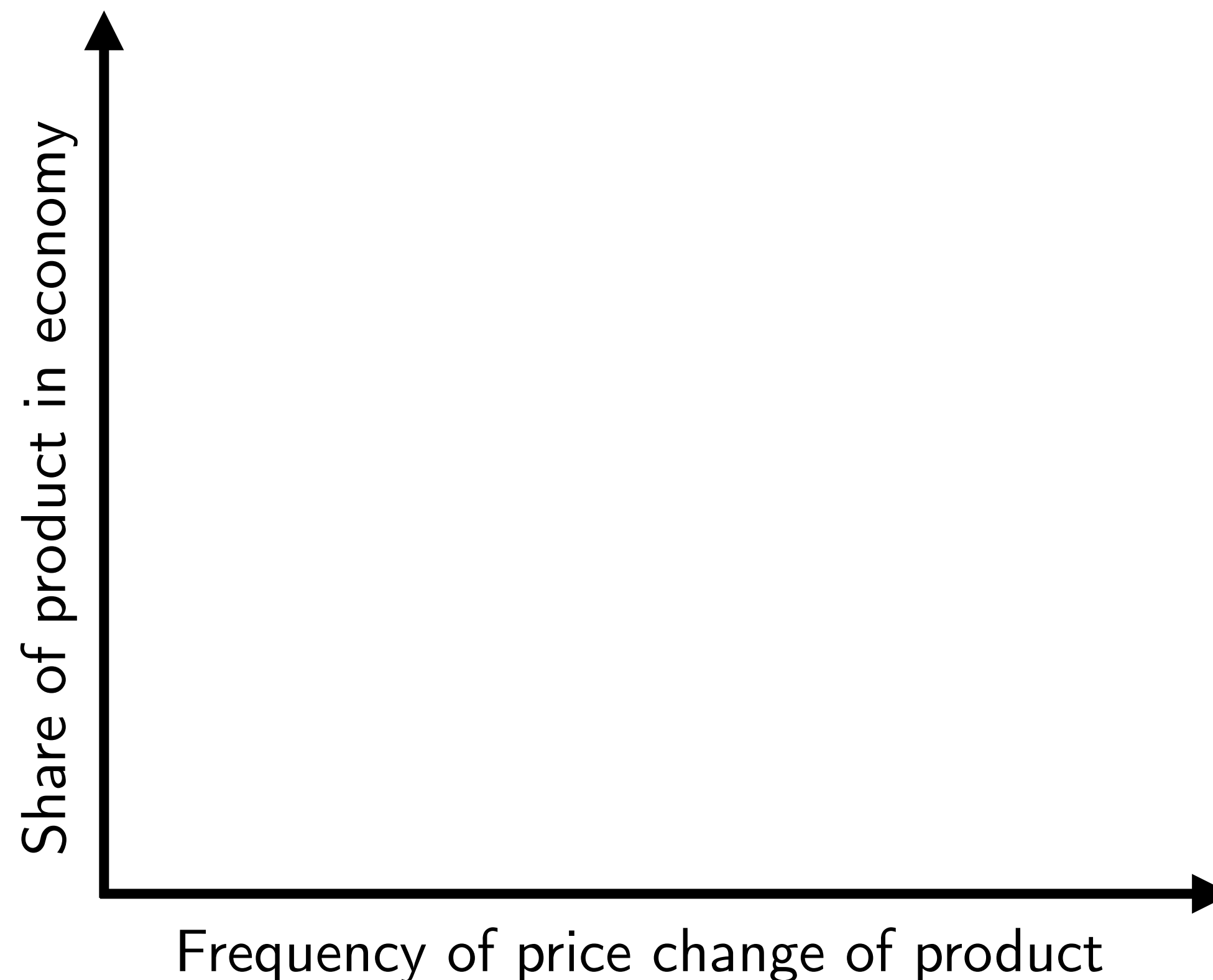
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- Distribution of frequency of $P\Delta_{it} = F(\text{Frequency of } P\Delta \text{ of product}_{it}, \text{Share of product in economy}_{it})$

Data

Distribution of frequency of $P\Delta_{it} = F$ (Frequency of $P\Delta$ of product_{*i*}, Share of product in economy_{*it*})

Data

Distribution of frequency of $P\Delta_t = F$ (Frequency of $P\Delta$ of product_{*i*}, Share of product in economy_{*it*})



- ▶ Supplementary tables of Nakamura and Steinsson (2008)
- ▶ Available for 272 CPI + 348 PPI products
- ▶ **Static** measure: 1998–2005 average

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Own algorithm based on:

- ▶ Product–Industry mapping
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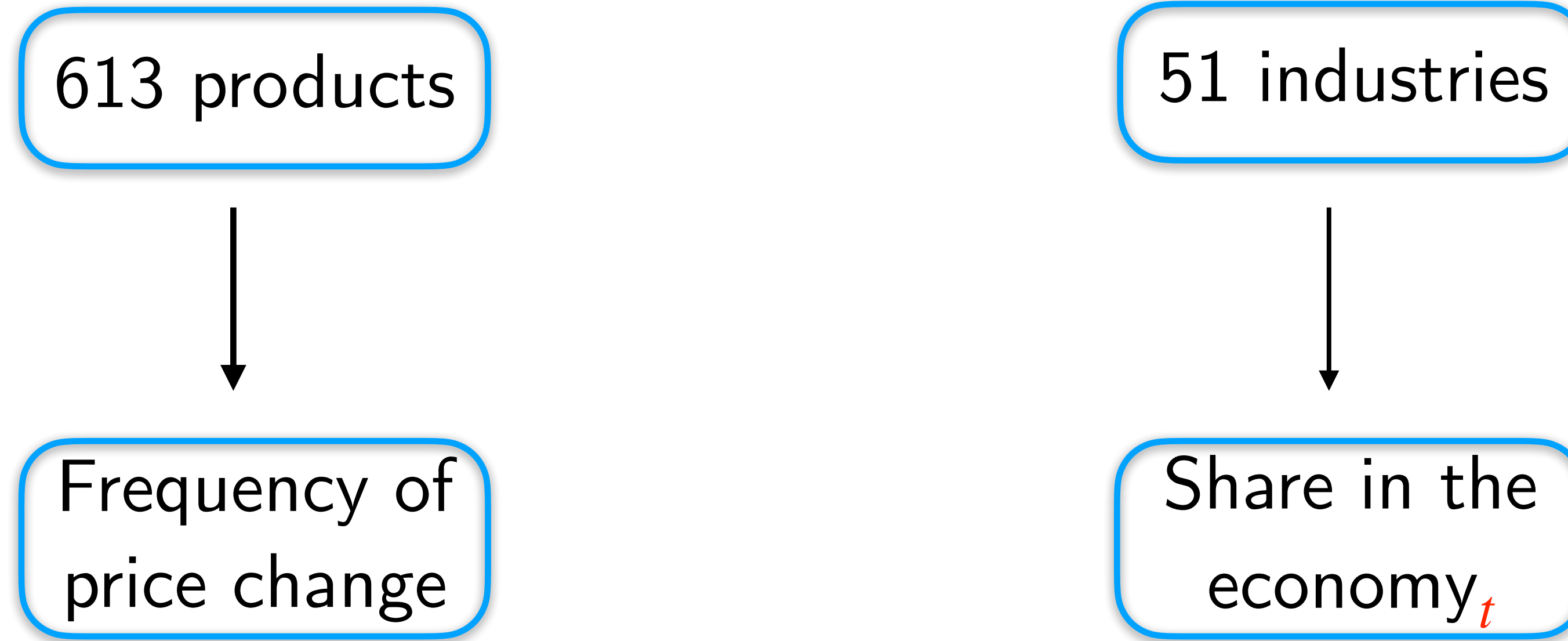
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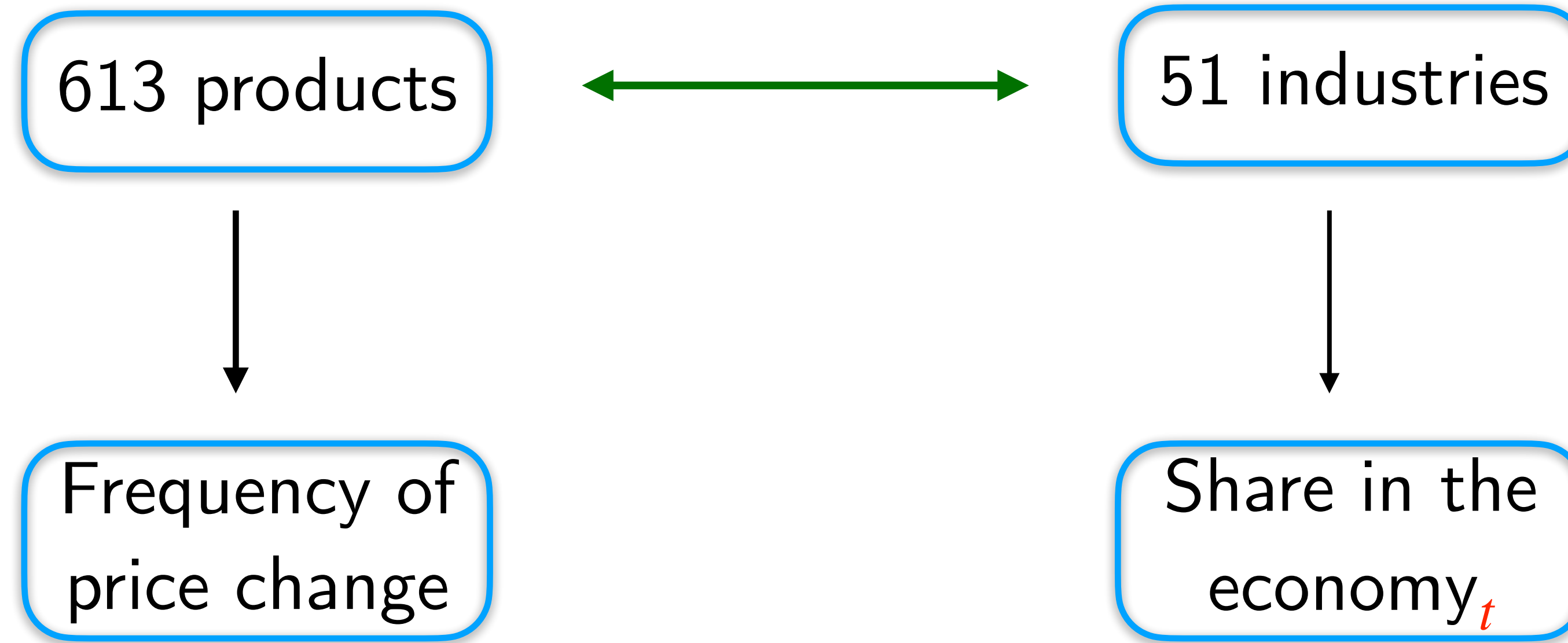
- ▶ Product–Industry mapping
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- ▶ BEA and World KLEMS Initiative
- ▶ Available for 65 industries
- ▶ **Dynamic**: 1947–2019 annual data

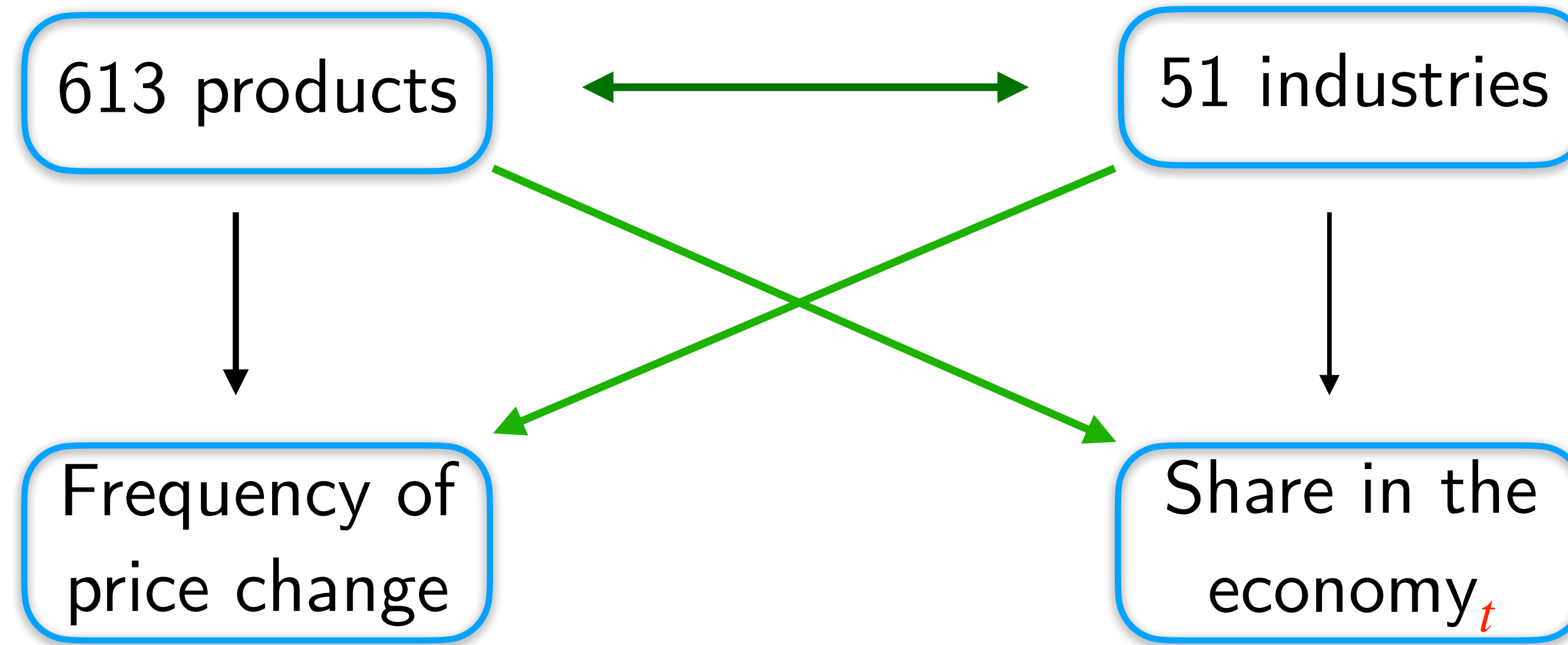
Result of the Algorithm



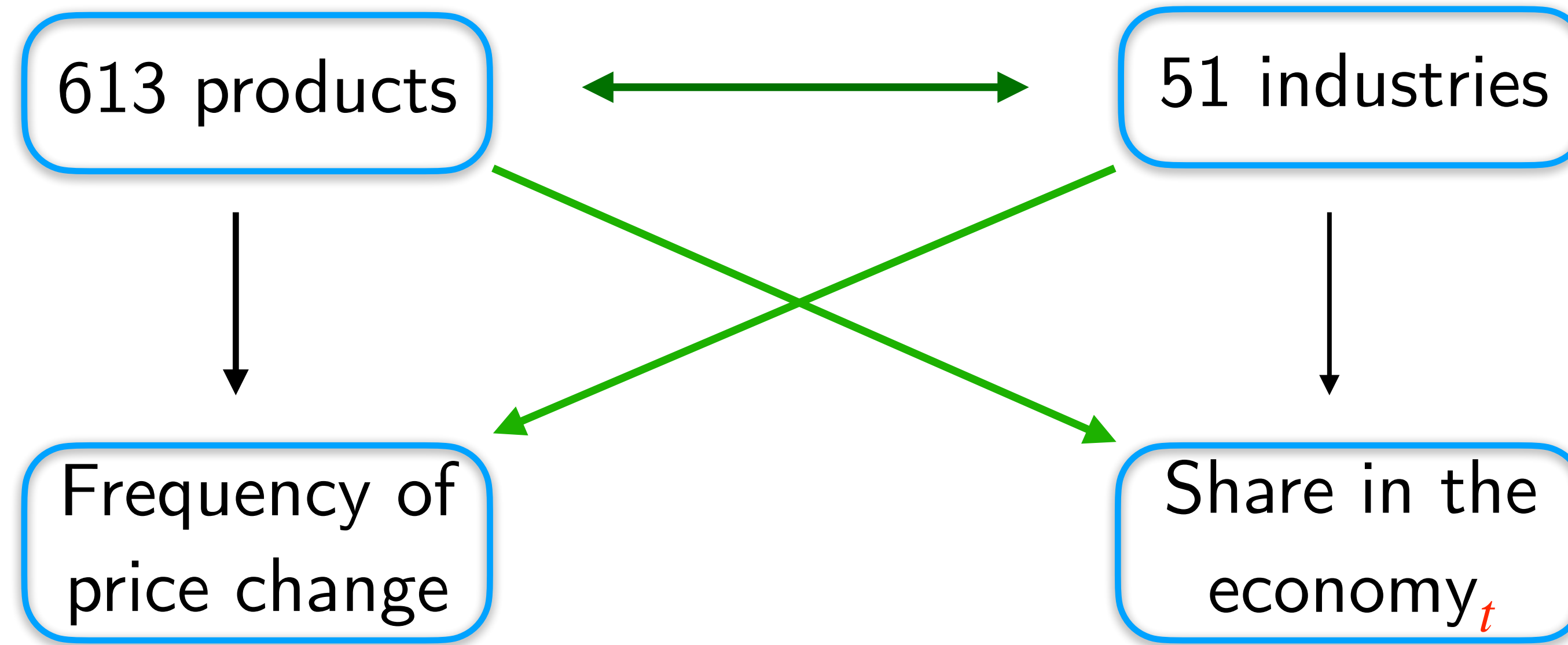
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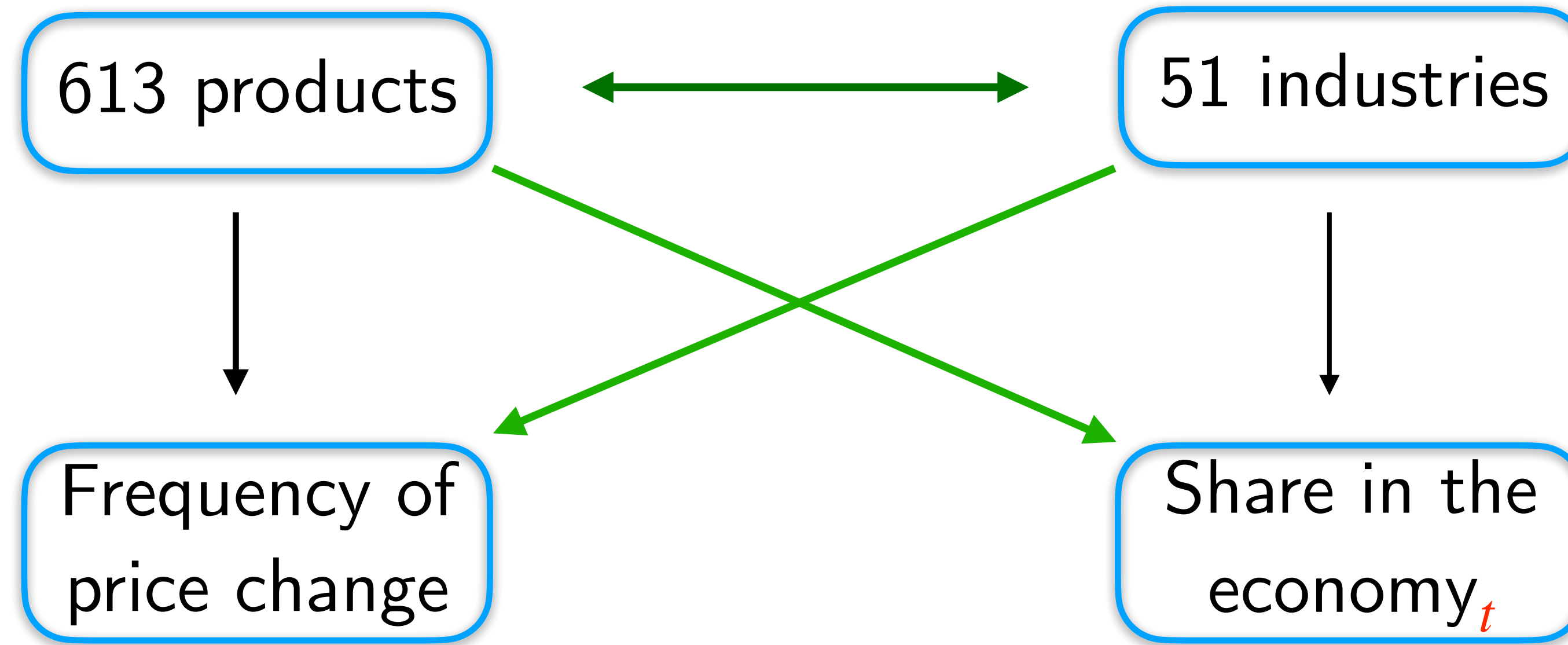


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- Once we have computed the **share of the product in the economy_{it}**
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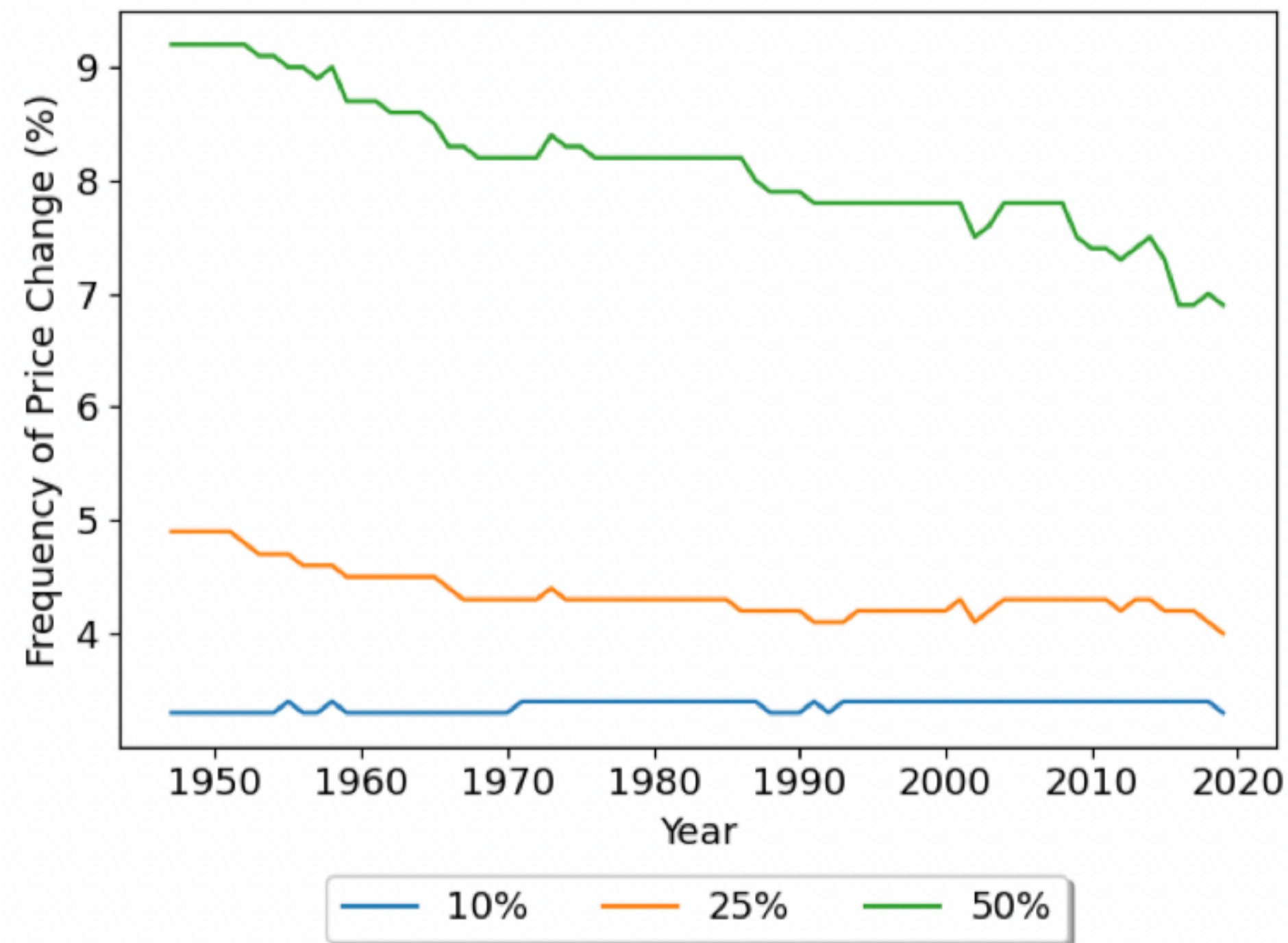


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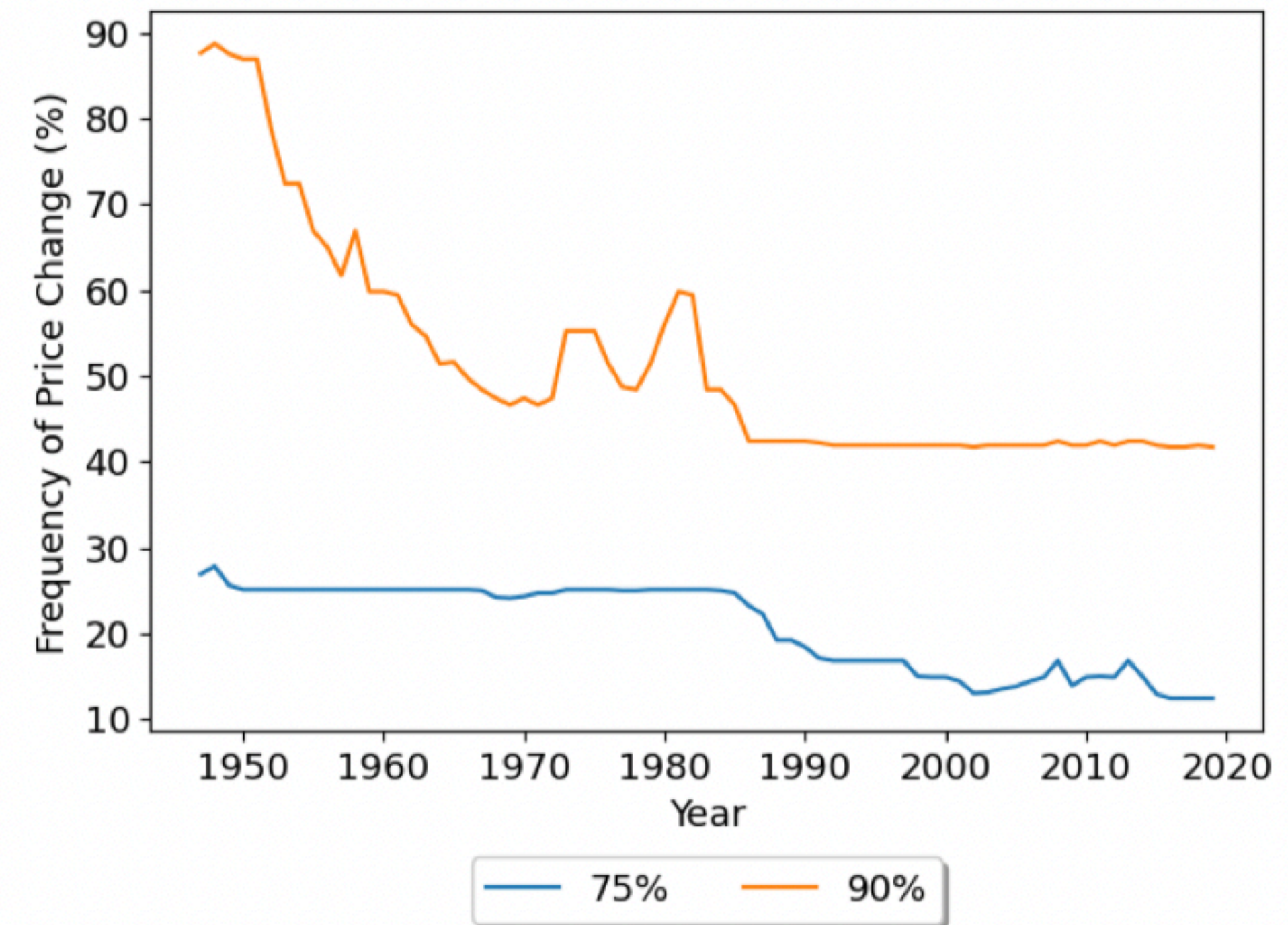
Distribution of any statistic of product_t = F (Statistic of product_i, Share of product in economy_{it})

Result 1

- Changes in industrial composition have led to **large declines across the distribution of the frequency of price change** over the 1947–2019 period



(a) For Low Percentiles



(b) For High Percentiles

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- Changes in industrial composition have led to **large declines across the distribution of the frequency of price change** over the 1947–2019 period

| Year | 10% | 25% | 50% | 75% | 90% |
|------|-----|-----|-----|------|------|
| 1947 | 3.3 | 4.9 | 9.2 | 26.9 | 87.6 |
| 1957 | 3.3 | 4.6 | 8.9 | 25.1 | 61.7 |
| 1967 | 3.3 | 4.3 | 8.3 | 25.0 | 48.4 |
| 1977 | 3.4 | 4.3 | 8.2 | 25.0 | 48.7 |
| 1987 | 3.4 | 4.2 | 8.0 | 22.2 | 42.4 |
| 1997 | 3.4 | 4.2 | 7.8 | 16.8 | 41.9 |
| 2007 | 3.4 | 4.3 | 7.8 | 14.9 | 41.9 |
| 2017 | 3.4 | 4.2 | 6.9 | 12.4 | 41.7 |
| 2019 | 3.3 | 4.0 | 6.9 | 12.4 | 41.7 |

Result 1

- Median frequency of price change has fallen from 9.2% to 6.9% over the 1947–2019 period

| Year | 10% | 25% | 50% | 75% | 90% |
|------|-----|-----|-----|------|------|
| 1947 | 3.3 | 4.9 | 9.2 | 26.9 | 87.6 |
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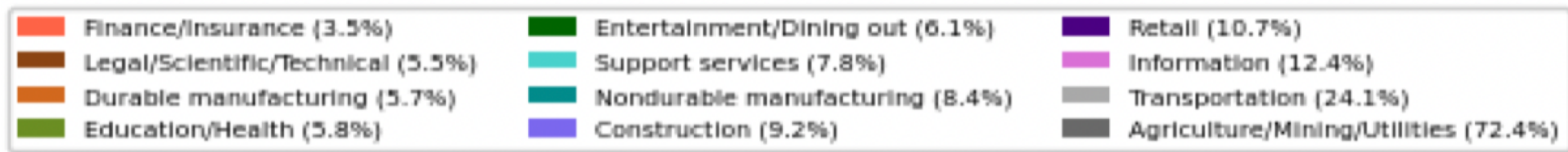
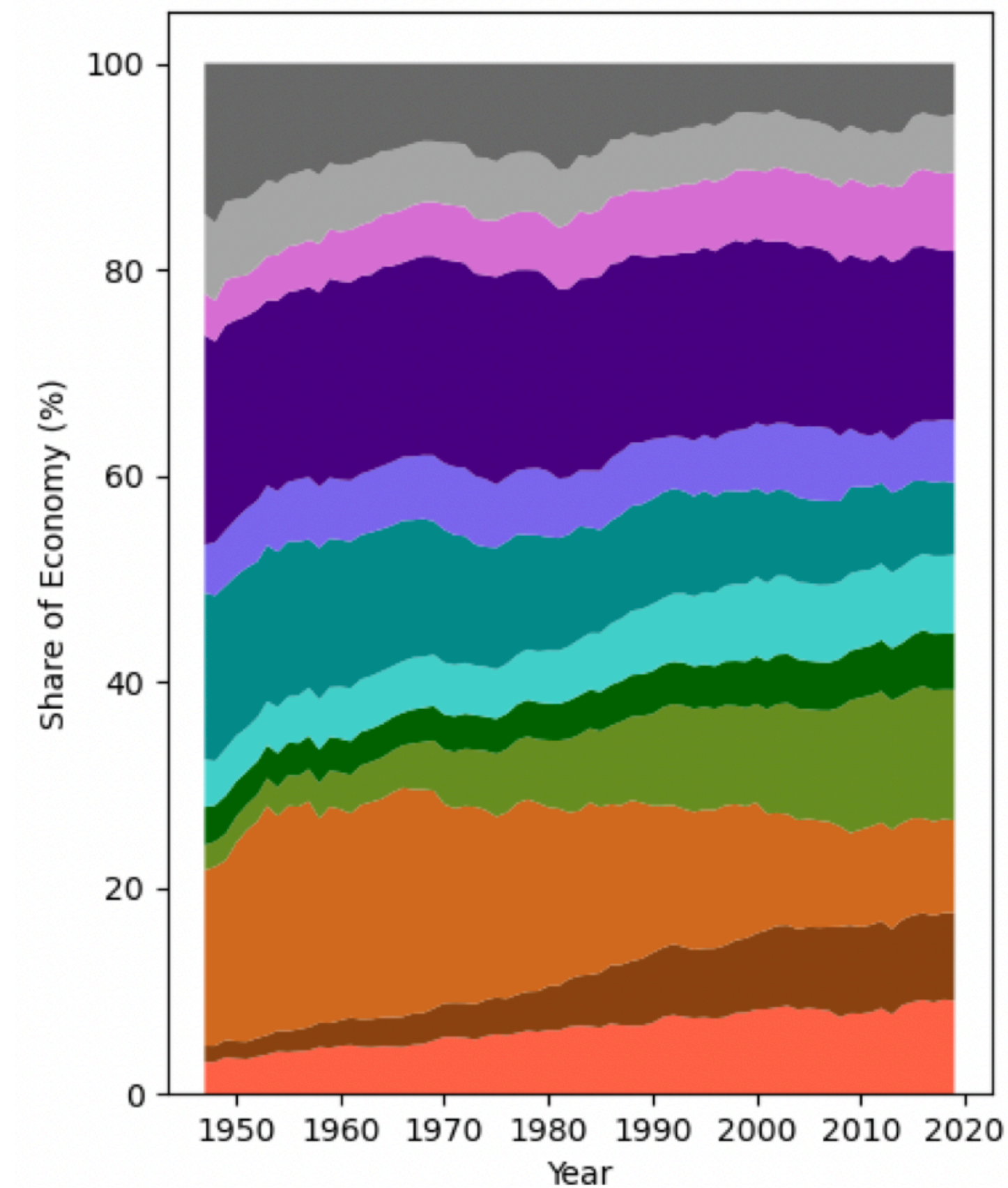
Result 1

- Similar declines for other percentiles (except 10th) of the distribution of frequency of price change over the 1947–2019 period

| Year | 10% | 25% | 50% | 75% | 90% |
|------|-----|-----|-----|------|------|
| 1947 | 3.3 | 4.9 | 9.2 | 26.9 | 87.6 |
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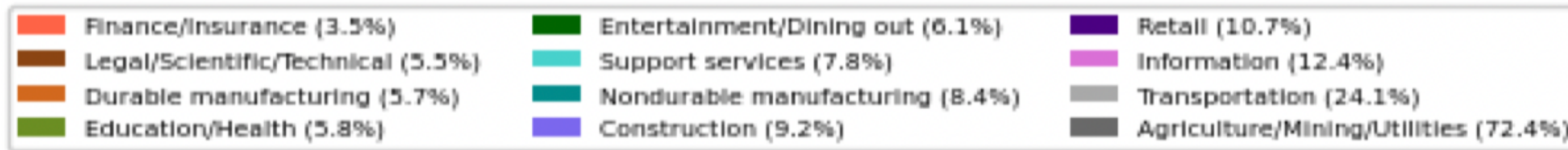
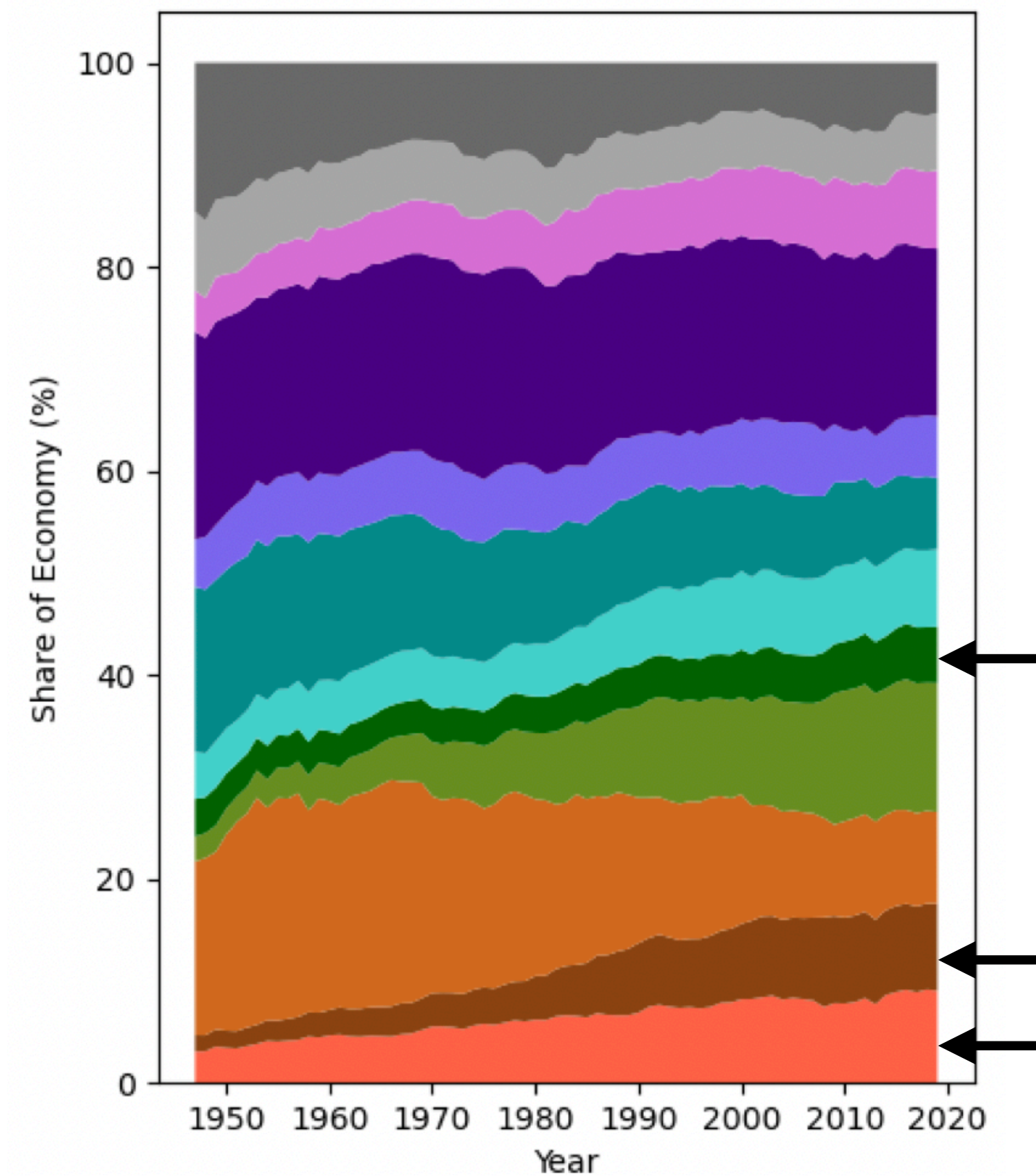
Result 2

- These declines across the distribution were driven by a **shift from primary and secondary industries to tertiary industries** over the 1947–2019 period



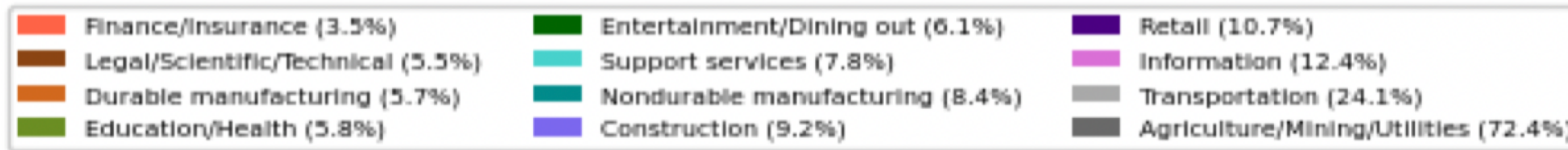
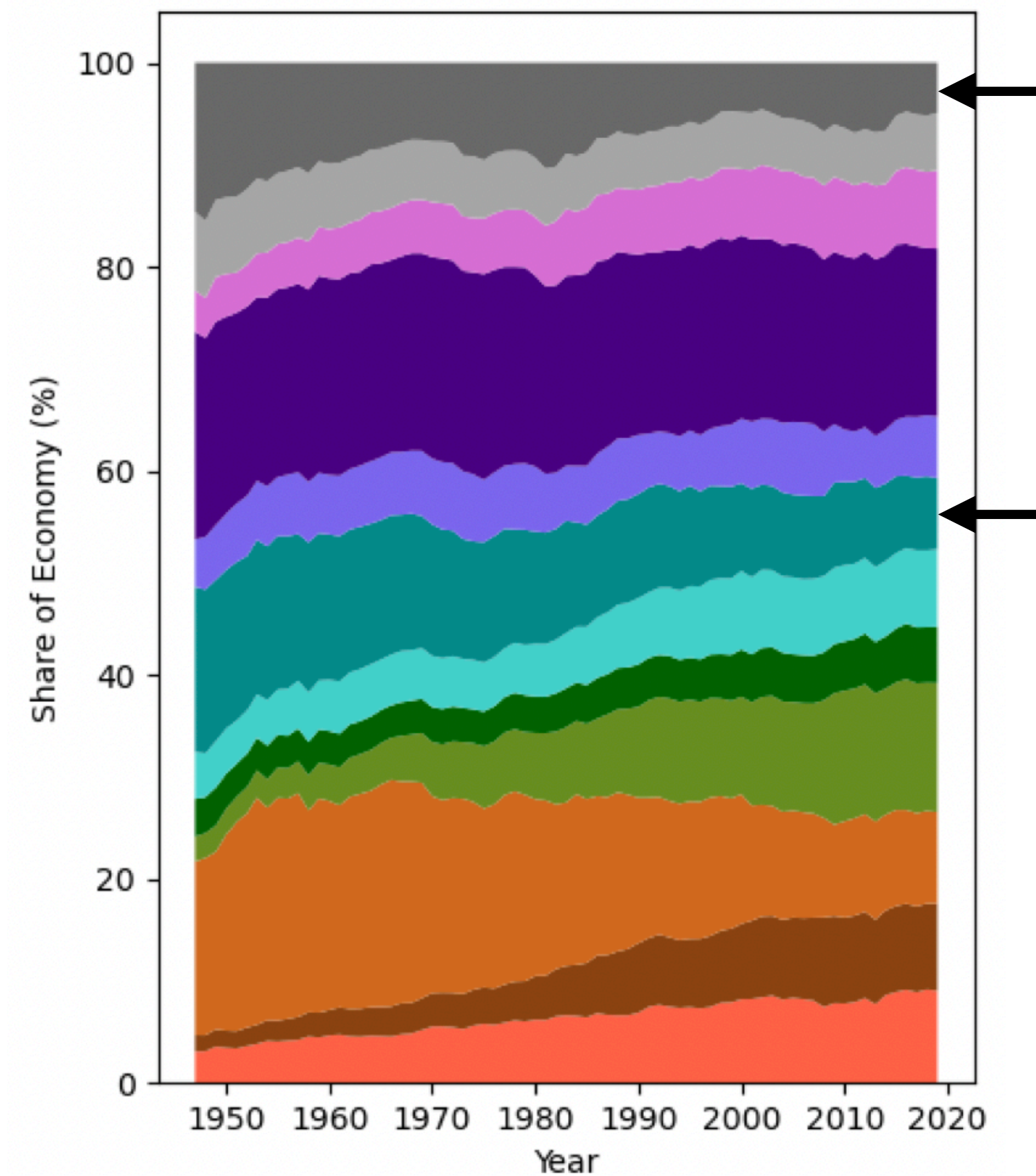
Result 2

- Finance/insurance, legal/scientific/technical, and education/health grew a lot
- All have low frequencies of price change



Result 2

- Nondurable manufacturing and agriculture/mining/utilities shrunk a lot
- Both have high frequencies of price change



Result 2

- All of the five industries that grew the most:
 - Show substantially lower frequencies of price change than industries that shrunk
 - Are tertiary (service) industries

Industries with the top 5 largest increases in share of the economy

| Industry Name | Freq. | 1947 | 1983 | 2019 |
|--|-------|------|------|------|
| Miscellaneous professional scientific and technical services | 8.2 | 1.1 | 3.5 | 6.7 |
| Ambulatory health care services | 3.4 | 1.0 | 3.0 | 5.3 |
| Hospitals Nursing and residential care facilities | 6.3 | 0.9 | 3.1 | 4.6 |
| Administrative and support services | 4.3 | 0.5 | 1.8 | 4.1 |
| Federal Reserve banks credit intermediation and related activities | 3.5 | 1.7 | 3.9 | 4.8 |

Result 2

- Three of the five industries that shrunk the most:
 - Have relatively higher frequencies of price change
 - Are primary or secondary (that extract raw materials and those that process them, respectively) industries

Industries with the top 5 largest decreases in share of the economy

| Industry Name | Freq. | 1947 | 1983 | 2019 |
|--|-------|------|------|------|
| Farms | 94.8 | 10.0 | 1.7 | 0.9 |
| Retail Trade | 10.7 | 12.2 | 9.9 | 7.9 |
| Food and beverage and tobacco products | 22.2 | 5.8 | 3.1 | 1.8 |
| Rail transportation | 24.1 | 4.0 | 0.8 | 0.3 |
| Primary metals | 34.8 | 2.8 | 1.2 | 0.4 |

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- The remaining two industries are associated with the sale and transportation of their goods

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 - Idiosyncratic productivity shocks \rightarrow sector-specific distribution with std. dev. $\sigma_{\epsilon,j}$
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- Model solved for a **given distribution of sectors** (share of sector in the economy _{jt})
- Simulate Phillips curve in response to **aggregate nominal demand shocks**

[Details](#)[Parameters](#)

Calibration

| Sector # | Target Moments: Price change | | Weight (%) |
|----------|------------------------------|-------------------|------------|
| | Frequency (%) | Absolute Size (%) | (1983) |
| 1 | 2.34 | 13.59 | 7.93 |
| 2 | 3.34 | 14.16 | 3.72 |
| 3 | 3.64 | 17.54 | 11.24 |
| 4 | 4.39 | 9.94 | 6.03 |
| 5 | 5.34 | 8.54 | 6.74 |
| 6 | 6.15 | 10.92 | 7.27 |
| 7 | 7.59 | 6.44 | 8.97 |
| 8 | 8.99 | 9.31 | 9.64 |
| 9 | 10.11 | 8.38 | 3.02 |
| 10 | 13.25 | 6.75 | 7.15 |
| 11 | 22.34 | 13.93 | 3.18 |
| 12 | 30.23 | 8.71 | 11.60 |
| 13 | 49.61 | 7.78 | 6.16 |
| 14 | 92.95 | 5.31 | 7.30 |

Calibration

Sector-specific
menu cost

| Sector # | Target Moments: Price change | | Estimated Parameters | | Weight (%) |
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| | Frequency (%) | Absolute Size (%) | χ_j | $\sigma_{\epsilon,j}$ | (1983) |
| 1 | 2.34 | 13.59 | 0.0057 | 0.0685 | 7.93 |
| 2 | 3.34 | 14.16 | 0.0074 | 0.0824 | 3.72 |
| 3 | 3.64 | 17.54 | 0.0043 | 0.0877 | 11.24 |
| 4 | 4.39 | 9.94 | 0.0013 | 0.0471 | 6.03 |
| 5 | 5.34 | 8.54 | 0.0008 | 0.0403 | 6.74 |
| 6 | 6.15 | 10.92 | 0.0011 | 0.0531 | 7.27 |
| 7 | 7.59 | 6.44 | 0.0004 | 0.0306 | 8.97 |
| 8 | 8.99 | 9.31 | 0.0005 | 0.0377 | 9.64 |
| 9 | 10.11 | 8.38 | 0.0005 | 0.0396 | 3.02 |
| 10 | 13.25 | 6.75 | 0.0001 | 0.0242 | 7.15 |
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| 12 | 30.23 | 8.71 | 0.0004 | 0.0712 | 11.60 |
| 13 | 49.61 | 7.78 | 0.0002 | 0.0857 | 6.16 |
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Sector-specific
menu cost

Sector-specific std.
dev. of idiosyncratic
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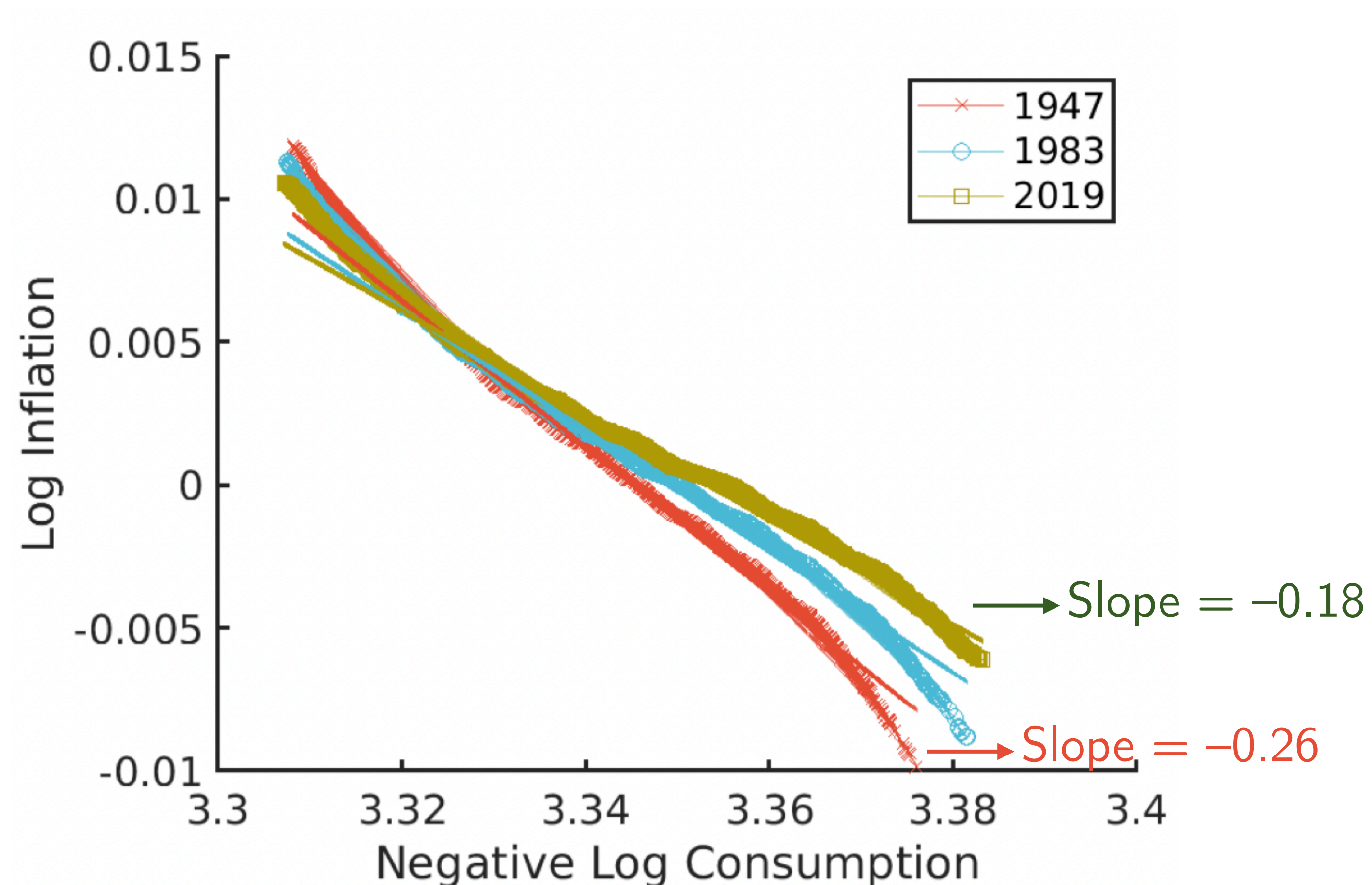
Robustness

Δ Industrial Composition \Rightarrow Δ Phillips Curve

- Hold fixed:
 - Calibrated parameters
 - Nominal demand shocks
- **Change only share of sector in the economy_{*jt*}**
 - As implied by the share of product in the economy_{*it*}
 - As implied by the industrial composition of the economy for the given year
- **Simulate the Phillips curve given the new sector distribution**
 - One for each year: 1947–2019

Result 3

- These changes in the industrial composition have led to a **30.7 percent flattening** of the slope of the Phillips curve over the 1947–2019 period



Conclusion

- We isolated the impact of changes in industrial composition during 1947–2019 on:
 - the distribution of products in the US economy
 - consequently the distribution of the frequency of price change across the products
- We found: US economy exhibits greater price stickiness in 2019 compared to 1947
 - Median frequency of price change fallen from 9.2% to 6.9%
 - Mean frequency of price change fallen from 24.2% to 15.1%

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- We found: US economy exhibits greater price stickiness in 2019 compared to 1947
 - Median frequency of price change fallen from 9.2% to 6.9%
 - Mean frequency of price change fallen from 24.2% to 15.1%
- Then we analyzed the degree to which these distributional changes affected the slope of the Phillips curve over this period
- We found: US Phillips curve 30.7% flatter
 - Cause: long-term structural forces, unlikely to revert
 - Central banks should account for the flattening in their decisions

Thank you!

Algorithm

$$\text{Share of product in economy}_{it} = \sum_j \underbrace{\text{Share of industry in economy}_{jt}}_{\substack{\text{BEA and World KLEMS Initiative} \\ \text{Available for 65 industries} \\ \text{Dynamic: 1947–2019 annual data}}} \times \underbrace{\text{Share of product in industry}_{ij}}_{\substack{\text{620 products (272 CPI + 348 PPI) mapped to one or more of 2017 6-digit NAICS industries (of which there are 65)} \\ \text{We are able to map 613 products to 51 industries}}}$$

- ▶ BEA and World KLEMS Initiative
- ▶ Available for 65 industries
- ▶ **Dynamic**: 1947–2019 annual data

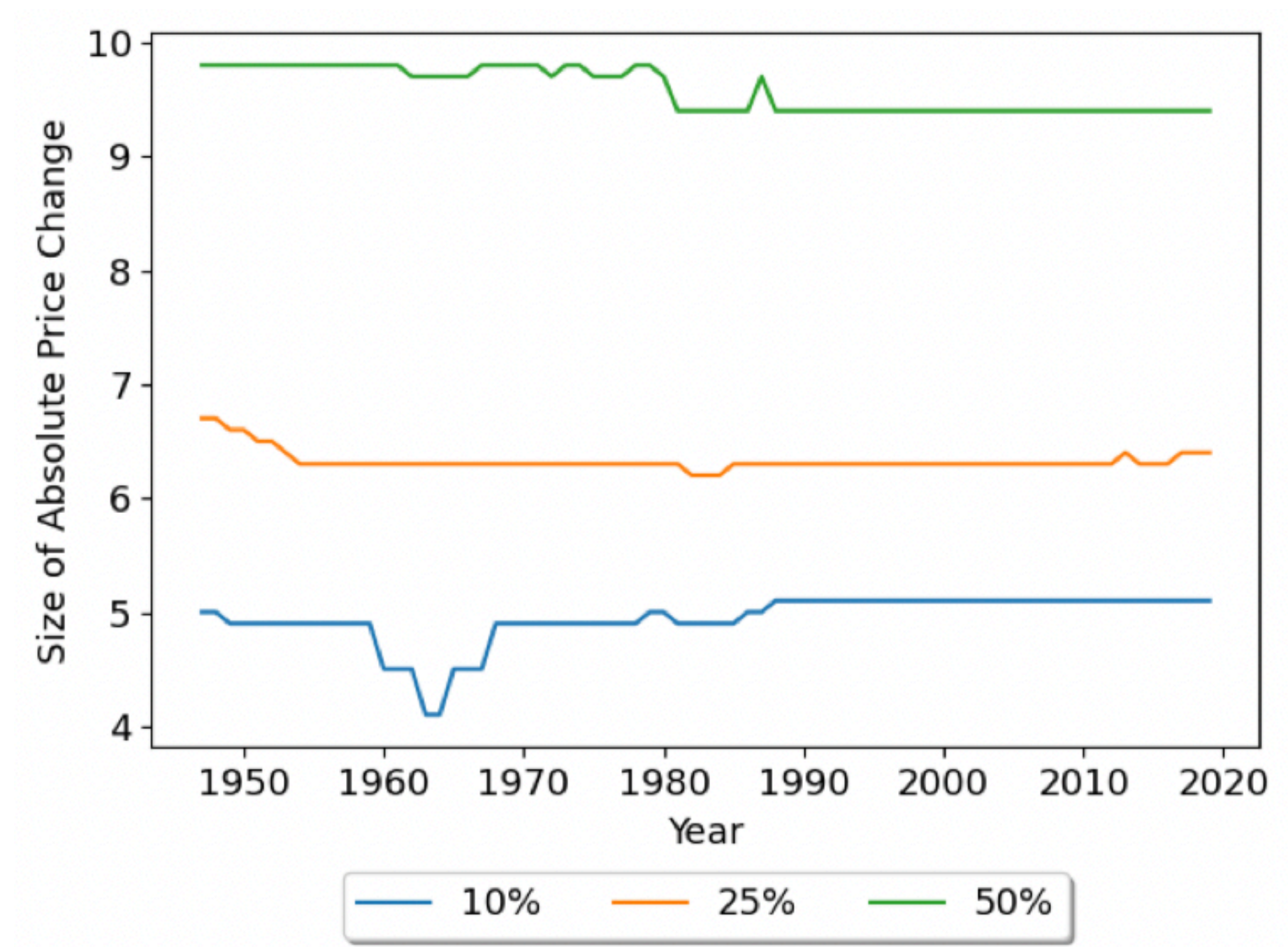
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 - ▶ We are able to map 613 products to 51 industries
2. Aggregate industries to the BEA/KLEMS World-level for which we have industry-shares data
3. Compute the *share of product in industry*_{ij} using:
 - i) set $a_{i,j} = 1$ if product i sold in industry j ; zero otherwise
 - ii) compute raw weight of product i sold in industry j : $b_{i,j} = \frac{a_{i,j}}{\sum_j a_{i,j}}$
 - iii) compute proportion of industry j sold by product i : $c_{i,j} = \frac{\omega_i b_{i,j}}{\sum_i \omega_i b_{i,j}}$, where ω_i = expenditure weight*

* expenditure weight available for CPI products; for PPI products we set it to 1 divided by the total # of PPI products

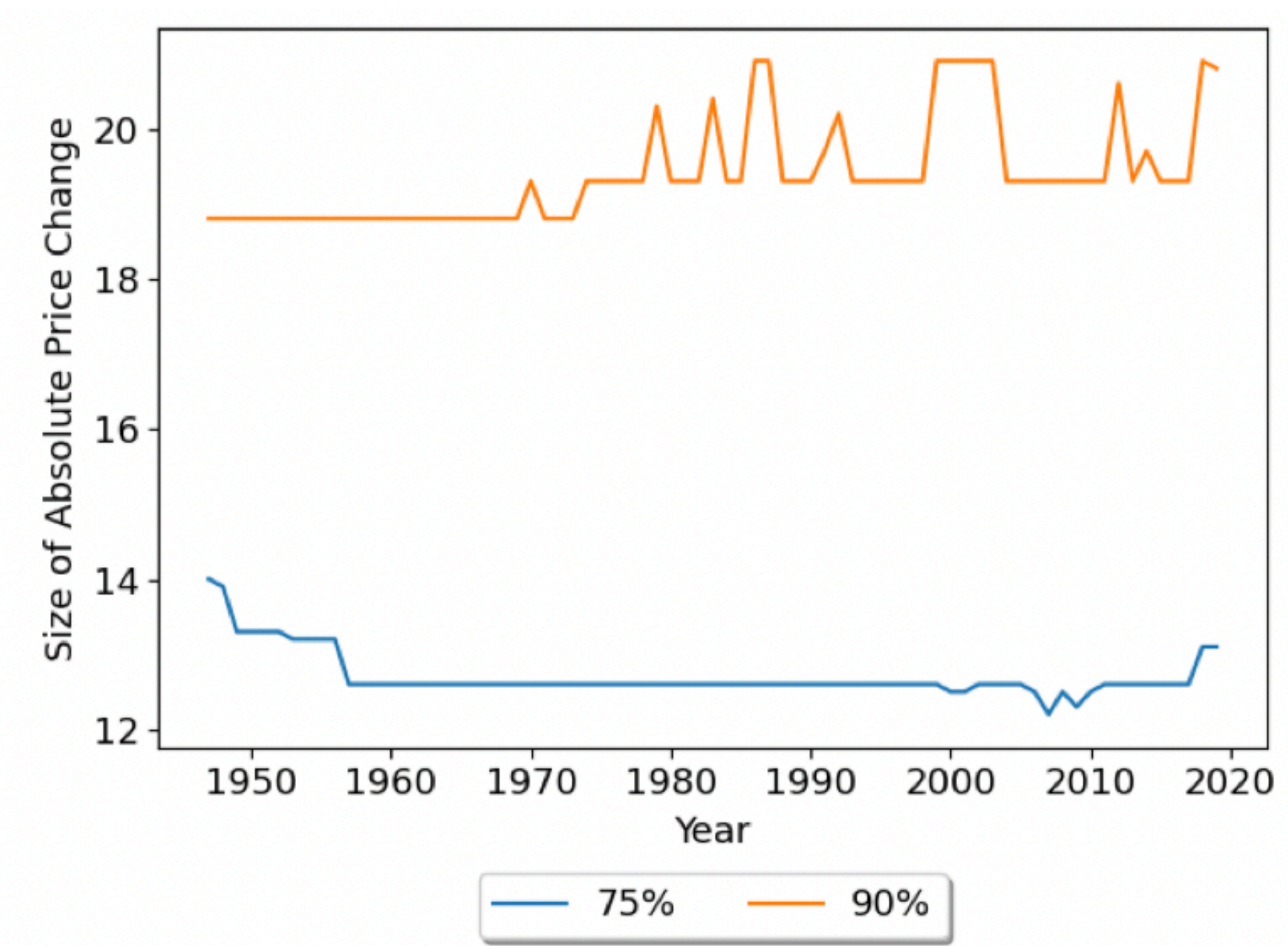
Robustness Checks

| Method | 1947 Median | 1983 Median | 2019 Median |
|--------------------------|-------------|-------------|-------------|
| A. Main | 9.2 | 8.2 | 6.9 |
| B. Any price change | 11.5 | 8.7 | 7.8 |
| C. One Klems | 9.2 | 8.2 | 6.9 |
| D. Same weight | 9.1 | 8.0 | 7.2 |
| E. No large products | 9.4 | 7.8 | 6.9 |
| F. Aggregate by Industry | 10.7 | 8.4 | 8.2 |
| G. CPI Only | 9.2 | 8.2 | 6.9 |
| H. PPI Only | 9.7 | 7.4 | 7.2 |

Distribution of absolute size of price change: 1947–2019



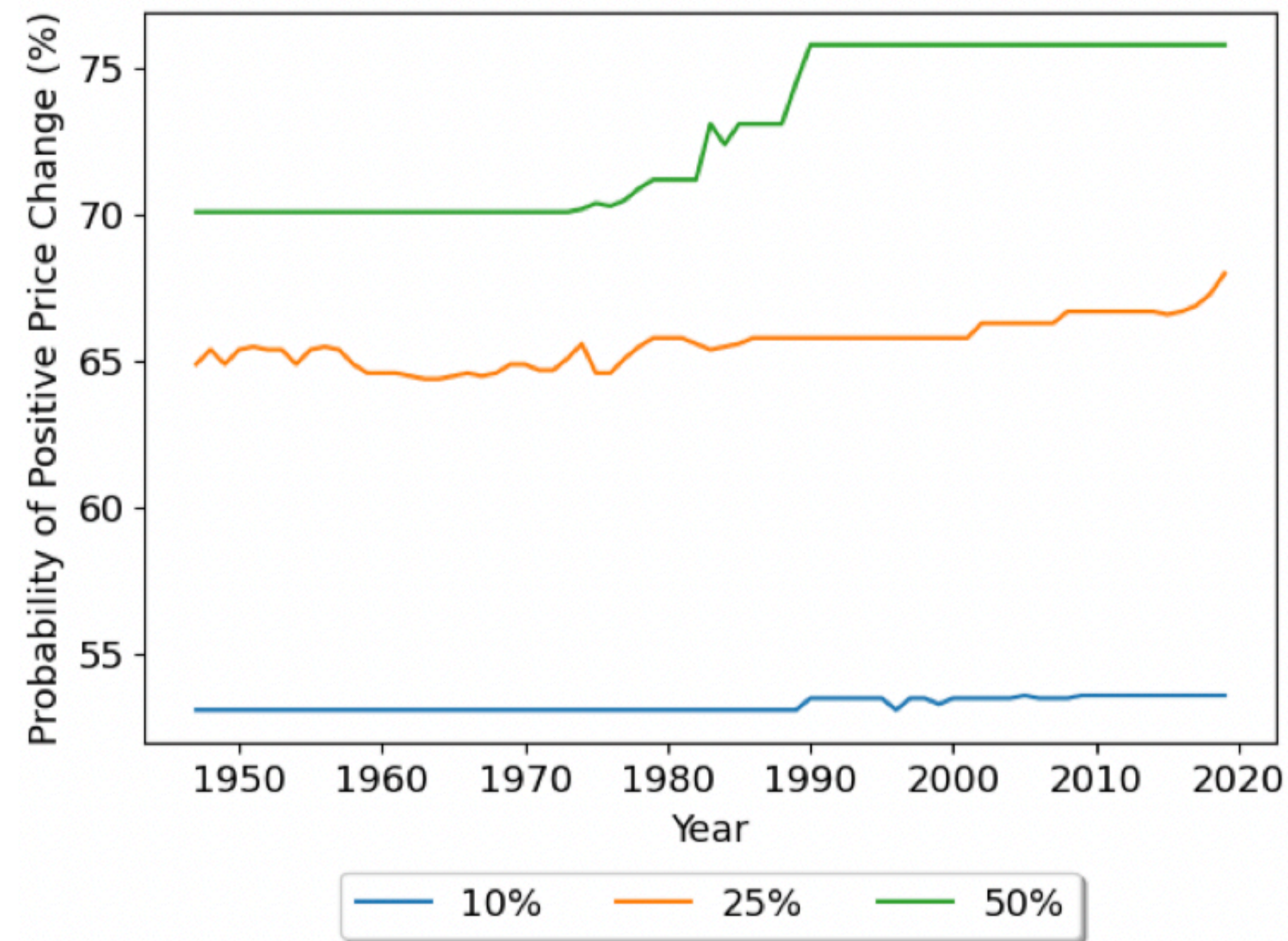
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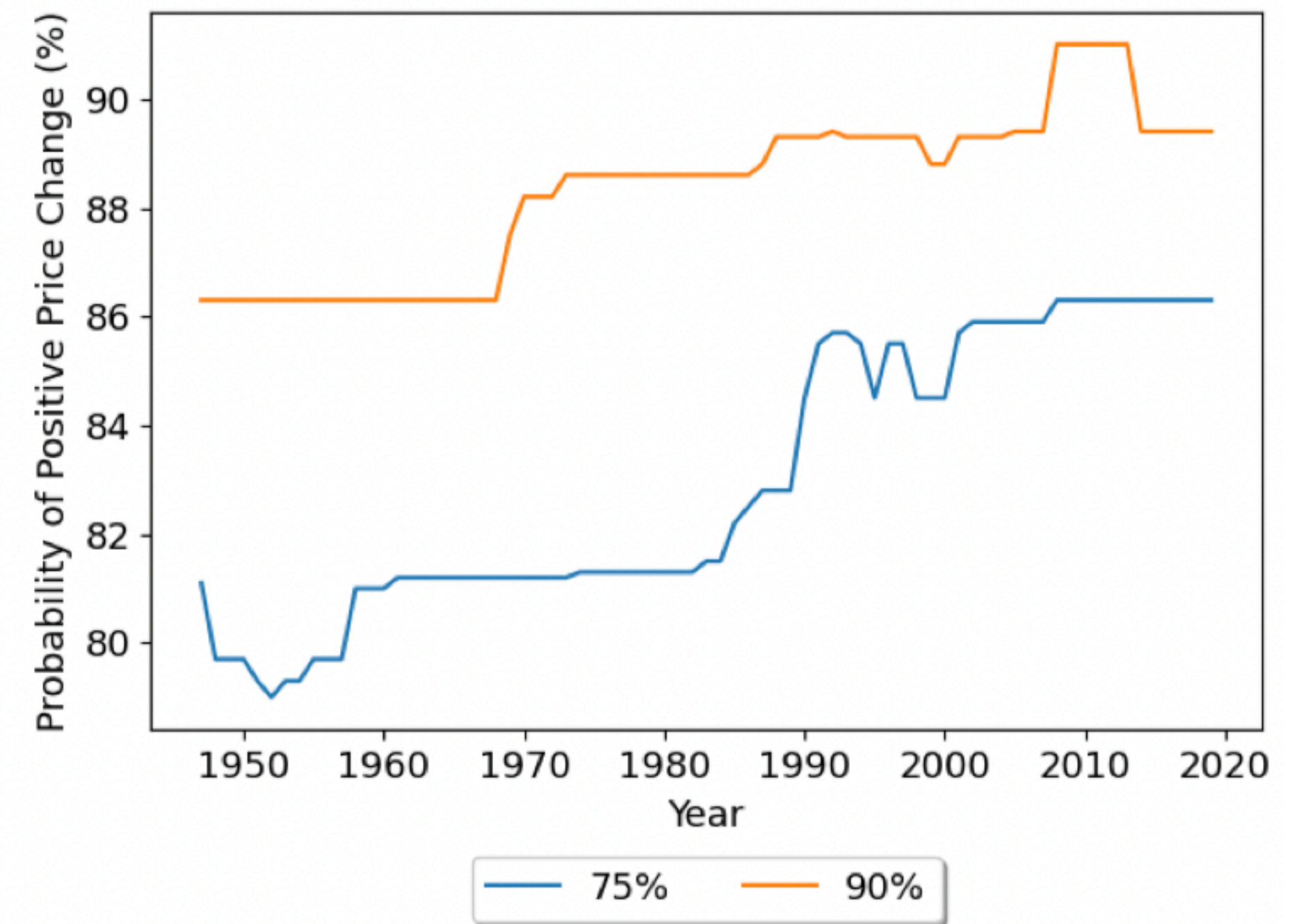
(b) For High Percentiles

- No systematic impact

Distribution of probability of positive price change: 1947–2019



(a) For Low Percentiles



(b) For High Percentiles

- Shifted up

Model Details

- 14 sectors
- Sector-specific:
 - Price stickiness in the form of menu costs χ_j
 - Standard deviation of firms' idiosyncratic productivity shocks $\sigma_{\epsilon,j}$
- Round-about production structure
 - Intermediate inputs as well as labor used in production
- Nominal target for monetary policy:
 - Nominal aggregate demand : $S_t = P_t C_t$
 - Monetary authority targets a path of S_t
- Idiosyncratic shocks to firms' productivity:

$$\log A_t(z) = \varrho \log A_{t-1}(z) + \epsilon_t(z) \text{ where } \epsilon_t \sim N(0, \sigma_{\epsilon,j}^2) \text{ are independent}$$

- Aggregate shocks to nominal demand:

$$\log S_t = \mu + \log S_{t-1} + \eta_t \text{ where } \mu \text{ represents trend inflation, } \eta_t \sim N(0, \sigma_\eta^2) \text{ are independent}$$

Model Details

- Menu cost \implies Firms' optimal price-setting decision is dynamic
- Recursive formulation:

$$V\left(A_t(z), \frac{p_{t-1}(z)}{P_t}, \frac{S_t}{P_t}\right) = \max_{p_t(z)} \left\{ \Pi_t^R(z) + \mathbb{E}_t \left[D_{t,t+1}^R V\left(A_{t+1}(z), \frac{p_t(z)}{P_{t+1}}, \frac{S_{t+1}}{P_{t+1}}\right) \right] \right\}$$

- Solution: intractable because state space of the firm's problem includes the aggregate price level P_t , which is an infinite dimensional object
- Assumption to make the model tractable: price level perceived to evolve depending on only the nominal demand deflated by the preceding period's aggregate price level:

$$\frac{P_t}{P_{t-1}} = \Gamma\left(\frac{S_t}{P_{t-1}}\right)$$

- P_{t-1} , though endogenous, is in the information's set at time t
- S_t exogenous
- General equilibrium solution computed using Value Function Iteration on a discretized state space

Calibration

| Parameter | Description | Value |
|-----------|---------------------------------------|-----------------------|
| σ | Coefficient of relative risk aversion | 1 |
| ψ | Labor disutility convexity | 0 |
| β | Discount factor | $0.96^{\frac{1}{12}}$ |
| θ | Elasticity of substitution | 4 |
| L | Steady-state labor supply | 0.33 |
| μ | Mean growth rate of nominal AD | 0.0028 |
| σ | Std. dev. of the growth of nominal AD | 0.0065 |
| s_m | Share of int. inputs in production | 0/0.7 |
| ρ | Persistence in firms' productivity | 0.7 |

Model Robustness

| Year | Frequency (%) | | Absolute Size (%) | | Prob. Positive (%) | |
|------------------------|---------------|-------|-------------------|-------|--------------------|-------|
| | Data | Model | Data | Model | Data | Model |
| Panel A. <i>Mean</i> | | | | | | |
| 1947 | 24.2 | 24.0 | 10.8 | 9.4 | 70.2 | 71.2 |
| 1983 | 18.7 | 18.6 | 10.0 | 10.1 | 71.9 | 73.0 |
| 2019 | 15.1 | 15.0 | 10.3 | 10.3 | 74.9 | 75.0 |
| Panel B. <i>Median</i> | | | | | | |
| 1947 | 9.2 | 9.2 | 9.8 | 8.6 | 70.1 | 70.5 |
| 1983 | 8.2 | 7.4 | 9.4 | 9.9 | 73.1 | 73.4 |
| 2019 | 6.9 | 7.3 | 9.4 | 9.9 | 75.8 | 73.6 |

Basic New Keynesian Phillips Curve

$$\pi_t = \kappa mc_t + \beta \mathbb{E}_t \pi_{t+1}$$

Under log utility and linear labor disutility:

$$\pi_t = \kappa y_t + \beta \mathbb{E}_t \pi_{t+1}$$

where

$$\kappa = \frac{\lambda [1 - (1 - \lambda)\beta]}{1 - \lambda}$$

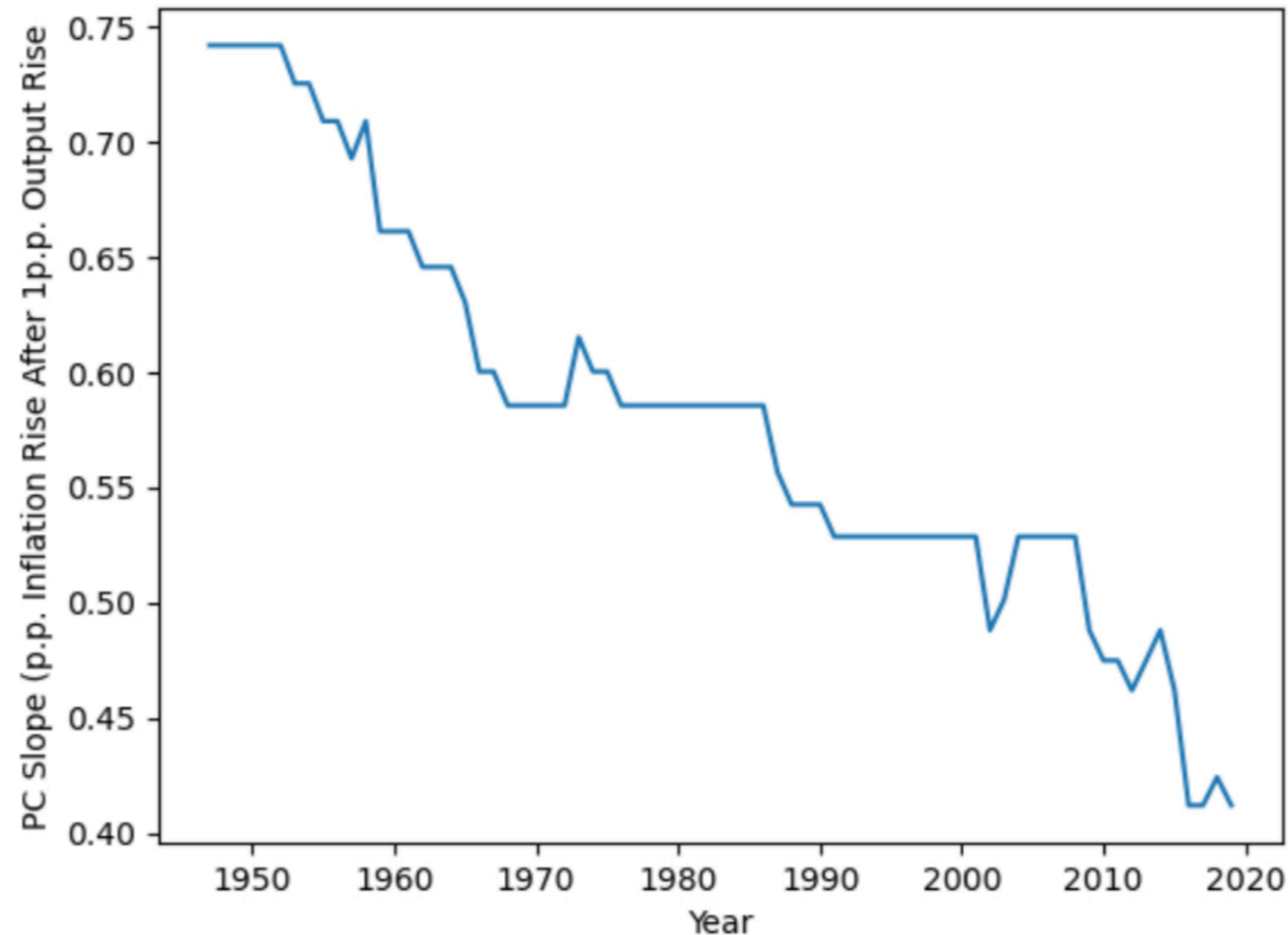
- Monthly parameters:
 - $\beta = 0.96^{\frac{1}{12}}$
 - λ = aggregate frequency of price change
 - Time-varying $\implies \kappa_t$

Basic New Keynesian Phillips Curve

$$\pi_t = \kappa_t y_t + \beta \mathbb{E}_t \pi_{t+1}$$

- $\lambda_{1947} = 9.2\% = 0.092$
- $\kappa_{1947} = 0.0096$
- Impact of known 1 p.p. rise in y_t for one year:
 - 12 months of high y_t
 - In earlier months, future inflation also rises
- Rise of 0.74 p.p. in inflation

Basic New Keynesian Phillips Curve



- Slope declines from -0.74 in 1947 to -0.59 in 1983 to -0.41 in 2019
- Amount to a 44.5% flattening from 1947 to 2019