

Partial Sovereign Default

Cristina Arellano Xavier Mateos-Planas Jose-Víctor Ríos-Rull

Federal Reserve Bank of Minneapolis
Queen Mary University of London
University of Pennsylvania

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Motivation

Emerging markets (and others) face frequent debt crises

- ▶ Sovereign default theory
(Eaton-Gersovitz 1983, Aguiar-Gopinath 2006, Arellano 2008, Chatterjee-Eyigungor 2012)
 - ▶ Sovereign default more likely when fundamentals are weak and debt is large
 - ▶ Successful in replicating default events (Argentina 2001, Greece 2012)
 - ▶ Generates volatile and countercyclical interest rates spreads as in data
 - ▶ Volatile consumption: default risk limits risk sharing
- ▶ Existing sovereign default theory – [Default leads to new start](#)
 - ▶ Default leads to reduction in debt and during episodes no borrowing or repayment

Motivation: Sovereign Defaults in Data

In data sovereign default episodes have rich dynamics – Default leads to more default

- ▶ Defaults are partial, countries spend much time in default
 - ▶ Partial default on average 38%, 1/3 the time positive
- ▶ During default episodes:
 - ▶ Debt and partial default dynamics hump-shaped
 - ▶ Repayment and borrowing continue
 - ▶ On average 9 years long, but with many short default episodes
 - ▶ Debt not reduced but sizable haircuts

Today will focus on our more complete framework of sovereign partial default:

- ▶ Prior to the default, similar to existing theory
- ▶ **New theory:** adds partial default and dynamics during the default episode

Model Elements

- ▶ Sovereign chooses to which extent to pay debt due
- ▶ Partially defaulted debt not automatically written off, nor new borrowing ruled out
- ▶ Partial default is alternative to borrowing to inter-temporally transfer resources

Partial default as portfolio choice

- ▶ Partial default amplifies debt crises
 - ▶ Defaulted payments accumulate and increase future indebtedness
 - ▶ Associated with resource costs and higher spreads on new borrowing

Default leads to more default

- ▶ Default episodes end after sufficient output recovery and deleveraging
 - ▶ Tight bond prices gives incentive for deleveraging

Main Findings

This theory is capable of rationalizing patterns in data

- ▶ Properties of partial default: frequency, mean, and co-movements
 - ▶ Large partial defaults → high spreads, high debt, deep recessions, and longer
- ▶ Default episodes that resemble data
 - ▶ Long episodes on average, with many short
 - ▶ Deliver hump-shaped patterns for debt and partial default
 - ▶ Not resulting in a net reduction of debt but with sizable haircuts

Debt resolutions mechanisms

- ▶ Debt relief and bond covenants less useful than in standard theory

Empirical Properties of Sovereign Defaults

- ▶ Develop accounting framework to analyze data
- ▶ Use panel data for 37 emerging countries 50 years
 - ▶ World Bank data (WDI, International Debt Statistics, Debtor Reporting System): public debt in arrears, debt service, debt levels, GDP
 - ▶ Global Financial Indicators on EMBI+ yield spreads
- ▶ Document properties of partial default and default episodes

Accounting: Flows and Levels

- ▶ Each period sovereign owes lenders a_t - sum of coupons from past issuances
- ▶ Flexible partial default policy: sovereign pays $(1 - d_t)a_t$ and does not pay $d_t a_t$

$$\text{Debt service}_t = (1 - d_t)a_t$$

$$\text{Defaulted coupons}_t = d_t a_t$$

$$\text{Debt due}_t = \text{Debt service}_t + \text{Defaulted coupons}_t = a_t$$

$$\text{Partial default}_t = \text{Defaulted coupons} / \text{Debt due} = d_t$$

- ▶ Debt level is present value of future coupon promises

$$\text{Debt}_t = \sum_{j=0}^{\infty} \frac{a_t^{t+j}}{R^j}$$

Accounting: Long-term Bonds and Partial Default Accumulation

- ▶ Map to tractable structure of long-term perpetuity bonds with decay δ (Hatchondo-Martinez 09)
 - ▶ Borrowing contract gives sovereign $q_t b_t$ with promises to repay $\delta^{j-1} b_t$ in future $t + j$
- ▶ Defaulted coupons $d_t a_t$ result in future obligations with PV $\kappa d_t a_t$

Factor κ captures that sovereign accumulates debt in arrears and restructures

- ▶ A sovereign with debt due a_t , that borrows b_t , and partially defaults on $d_t a_t$ has

$$a_{t+1} = \delta a_t + (R - \delta) \kappa d_t a_t + b_t.$$

- ▶ Evolution of debt due incorporates all these
- ▶ Debt level is the present value of contractual payments due $\frac{a_{t+1}}{R - \delta}$

Accounting: Default episodes and haircuts

- ▶ Default episode: Sequence of periods with consecutive positive partial default
Episode of **length** $N + 1$ has $d_{t+j} > 0$ for $j = \{0, 1, \dots, N\}$
- ▶ Defaulted coupons $d_t a_t$ during episode accumulated with factor κ result in new obligations n_t

$$n_{t+j+1} = \begin{cases} (R - \delta)\kappa d_{t+j} a_{t+j} + \delta n_{t+j} & \text{for } j = \{0, 1, \dots, N\} \\ \delta^{j-N-1} n_{t+j} & \text{for } j = \{N+1, \dots, \infty\} \end{cases}$$

- ▶ Restructured debt is the present value of new obligations n_t

$$\text{Restructured debt}_t = \sum_{j=1}^N \frac{(1 - d_{t+j})n_{t+j}}{R^j} + n_{t+N+1} \sum_{j=0}^{\infty} \frac{\delta^j}{R^{N+j+1}}$$

- ▶ Defaulted debt is the present value of the defaulted coupons

$$\text{Defaulted debt}_t = \sum_{j=0}^N \frac{d_{t+j} a_{t+j}}{R^j}$$

Accounting: Default episodes and haircuts

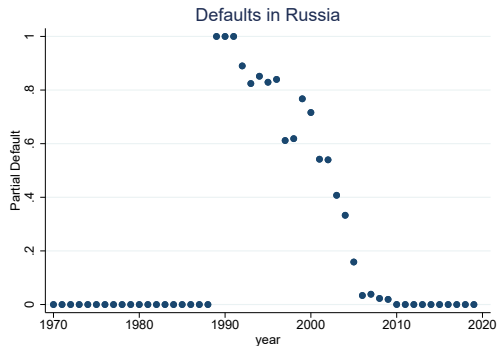
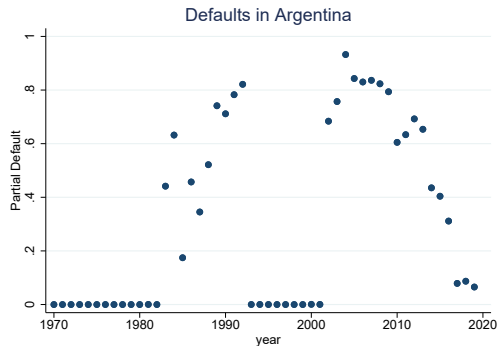
- ▶ Haircuts depend on value of the defaulted debt and the restructured debt (Cruces-Trebesch 13)

$$\text{Haircut}_t = 1 - \frac{\text{Restructured debt}_t}{\text{Defaulted debt}_t}$$

- ▶ In default episode sovereign carries its legacy debt due, restructured coupons, and borrowing
- ▶ Partial default and debt during the episode: sequences $\{d_{t+j}, \text{Debt}_{t+j}\}$ for $1 \leq j \leq N$

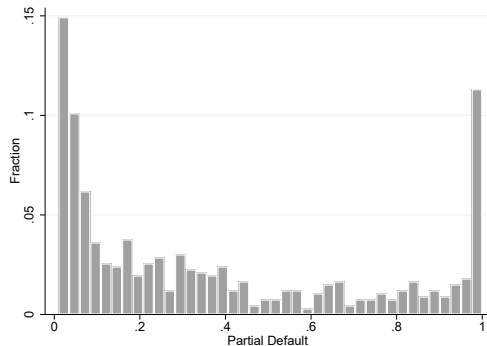
Use accounting framework to map data into our variables of interest

Partial Default and Episodes Examples

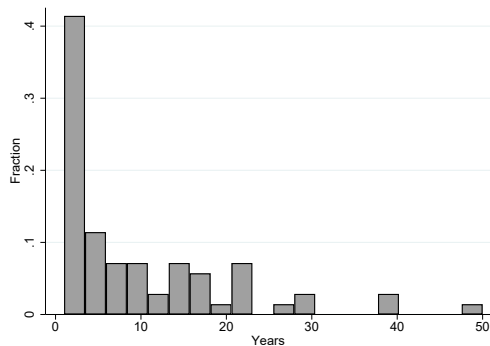


- ▶ Partial default frequent, varies in intensity
- ▶ Argentina experienced two episodes with lengths equal to 10 and 18 years
- ▶ Russia experienced one 20 year episode

Distribution of Partial Default and Episode Length



(a) Partial Default



(b) Default Episode Length

- ▶ Wide dispersion of partial default across countries and time
- ▶ Many short default episodes and a few countries always have positive default

Partial Default and Episodes across Countries

<i>Partial Default</i>			
Frequency			36
Mean partial default >0			38
Standard deviation partial default >0			22
<i>Default Episodes</i>			
Episode length (years)			9
Fraction of short episodes (≤ 2 years)			36
Haircut (%)			36
Maturity extension (years)			6
<i>Default Episodes Dynamics</i>	Partial Default	Debt	Output
Before episode	0	32	0
Beginning of episode	22	34	-2
Middle of episode	33	40	-5
After episode	0	33	-3

- ▶ Frequent partial default, about 1/3, with mean 38%
- ▶ Long default episodes on average, but lots of short
- ▶ Hump-shaped partial default and debt during default episodes; U shaped for output

Data Summary

1. Partial default: one third of time positive, on average 38%, large variance
2. With higher partial default: higher spreads and debt, more depressed output
3. Default episodes:
 - ▶ Hump-shape dynamics in partial default and debt, U shape for output
 - ▶ Do not lead to a net reduction in debt

Model: Environment

- ▶ Small open economy with stochastic endowment z_t
- ▶ Borrows internationally long-term perpetuity bonds with price q_t
- ▶ Lacks commitment and can partially default on its coupons
 - ▶ Default reduces income: cost depend on intensity d_t
 - ▶ Defaulted coupons accumulate with factor κ
 - ▶ With partial default, sovereign can continue to borrow at market higher rates
- ▶ International lenders risk neutral, bond prices compensate to default risk

Sovereign Borrower

- ▶ Preferences over consumption $E \sum_{t=0}^{\infty} \beta^t u(c_t)$
- ▶ Consumption is income y_t net of repayment of debt service and borrowing

$$c_t = y_t - a_t(1 - d_t) + q(a_{t+1}, d_t, z_t)b_t$$

- ▶ Partial default d_t expands c_t but depresses income $y_{t+1} = z_{t+1}\psi(d_t, z_{t+1}) \leq z_{t+1}$
Partial default and new borrowing is a portfolio problem
- ▶ Debt due = legacy debt δa_t + borrowing b_t + κ of new restructured $(R - \delta)\kappa d_t a_t$

$$a_{t+1} = \delta a_t + (R - \delta)\kappa d_t a_t + b_t$$

- ▶ Sovereign can always borrow, even with default but prices $q(a_{t+1}, d_t, z_t)$ respond
 d_t lowers prices because it increases a_{t+1} and lowers y_{t+1}

Recursive Problem and Bond Price

- State is (a, y, z) : a debt due; y income (due to default history); z persistent productivity

$$V(a, y, z) = \max_{b, d \in [0, 1]} \{u(c) + \beta E_z V(a', y', z')\}$$

subject to budget constraint, accumulation debt due, and income transition

- No separate problem for “default” states
- Bond price compensates for partial default loss to competitive lenders that discount at r

$$q(a', d, z) = \frac{1}{R} E \left(\underbrace{(1 - d(a', y', z'))}_{\text{partial default next}} + \left[\delta + \underbrace{(R - \delta)\kappa d(a', y', z')}_{\text{new restructured}} \right] \underbrace{q(a'', d', z')}_{\text{partial default future}} \right)$$

Trade-offs for Borrowing and Partial Default

- ▶ A portfolio-choice: Equate expected returns $R^b = R^d = u_c(c)/[\beta E u_c(c')]$

$$R^b \equiv \frac{R}{1 + q_a b/q} + \text{cov}_1 = \frac{Ez'(-\Psi_d)}{a(1 - q(R - \delta)\kappa) + q_d b} + \text{cov}_2 \equiv R^d$$

- ▶ Borrowing more attractive when q high and not too steep (R^b low)
- ▶ Partial default more attractive when a high, q low, default costs not too steep (R^d low)
- ▶ Steep bond price incentivizes exit from default episodes “induces deleveraging”

Quantitative Analysis

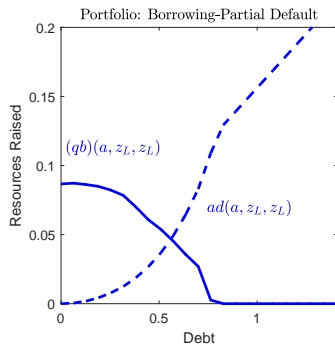
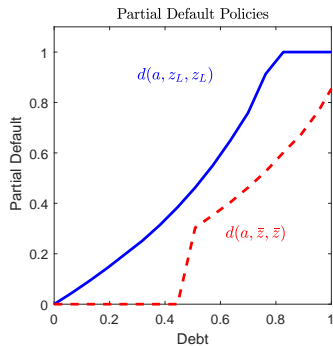
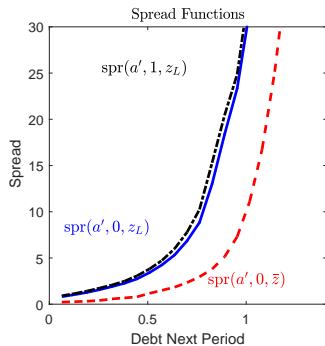
- ▶ Parameterize model to time series data of partial default and debt
 - ▶ Estimate 9 parameters (default cost parameters, discount factor, recovery factor, shock process, bond decay) to target 11 moments:
 - properties of partial default, debt to output, debt service, and spreads
 - ▶ Apply accounting to model for time series statistics, default episodes, haircuts
- ▶ Evaluate model performance for partial default co-movements and default episodes
- ▶ Perform counterfactuals: debt relief, bond covenants
- ▶ Compare with reference model

Model Fit: Moment Matching

	Data	Model
<i>Target Moments</i>		
Partial default (in %)		
frequency	36	37
mean partial default >0	38	39
st. dev. partial default >0	22	19
Debt to output (in %)		
mean	32	32
st. dev.	18	25
Debt service to output (in %)		
mean	3.6	3.5
st. dev.	2.1	2.2
Debt due to output mean	4.9	5
Spread st. dev.	4.1	3.7
Output		
persistence	0.89	0.88
st. dev. (in %)	10	12

- Good fit overall: partial default, debt service, debt to output

Mechanisms: Spreads, Partial Default, and Portfolio



- Spreads smooth, mostly depend on a' not on d directly but $a' = \delta a + da\kappa(R - \delta) + b$
- Higher debt + high spread \rightarrow larger partial default
- With low debt + low spread \rightarrow borrow
- Partial default endogenously restrict new borrowing (default piles up debt due)

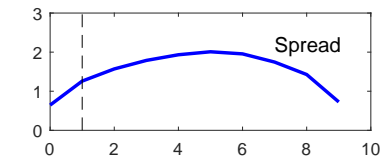
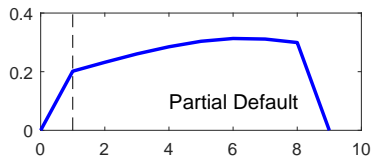
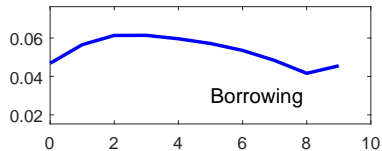
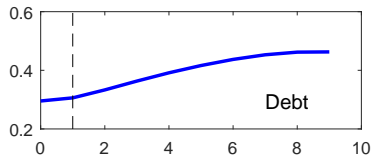
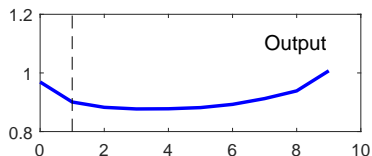
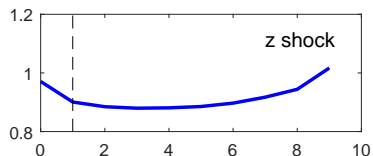
Default Episodes in Model and Data

	Data	Model
Mean episode length (years)	9	8
Percentage of short episodes (≤ 2)	36	42
Coefficient of variation for episode length	1.1	1.5
Haircut (%)	36	37
Maturity extension	6	7

Good fit for default episodes

- ▶ Model delivers long default episodes on average, with many short too
- ▶ Delivers haircuts and maturity extensions that resemble data

Default Episodes Model



- Default leads to more default, no reduction in debt
- Hump shape dynamics for partial default and debt; U shape for output

Default Episodes Dynamics in Model and Data

	Data	Model
<hr/>		
Partial Default		
Before	0	0
Beginning	22	21
Middle	33	28
End	0	0
Output		
Before	0	0
Beginning	-2	-7
Middle	-5	-9
End	-3	3
Debt		
Before	32	32
Beginning	34	35
Middle	40	44
End	33	42
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- ▶ Fits patterns in data
- ▶ Output and debt more accentuated in the model

Resolution Mechanisms Counterfactuals

PARI PASSU: NO MARKET ACCESS DURING DEFAULT

- ▶ Smaller haircuts on more recent issuances breaches pari passu (or equal treatment) clauses
- ▶ Pari passu might impede borrowing in default
- ▶ Defaulting becomes more costly, but credit is easier

DEBT RELIEF

- ▶ A permanent reduction in recovery factor κ
- ▶ Defaulting becomes less costly, but credit is harder

NO DILUTION COVENANTS

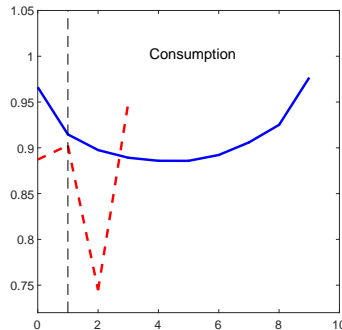
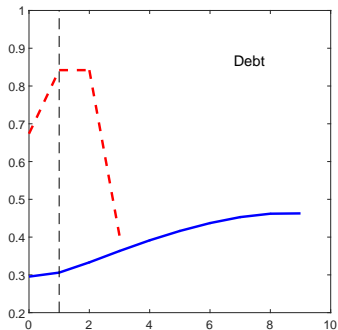
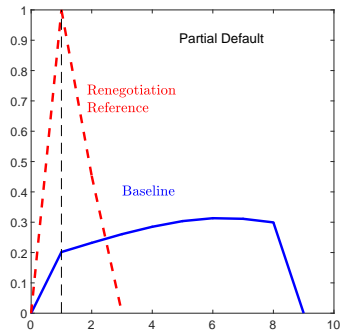
- ▶ Add no dilution covenants of Hatchondo-Martinez-SosaPadilla 2016
- ▶ Defaulting more costly, but credit easier

	Baseline	Pari Passu	Debt Relief	No-Dilution
<i>Default Episodes</i>				
Mean episode length (years)	8	2	8	6
Haircut (%)	37	32	46	36
<i>Time series in (%)</i>				
Partial default frequency	37	11	35	31
Debt to output mean	32	27	23	26
Spread st. dev.	3.7	1.1	2.3	0.9
<i>Welfare rel. baseline (% CE)</i>				
No debt, z_L	–	0.12	-0.11	0.07
Debt 64%, z_L	–	-0.07	0.05	-0.20
Overall Average	–	0.03	-0.04	-0.01

- Pari Passu: Less frequent partial default, shorter episodes, improves welfare when debt low
- Debt Relief: Larger haircuts and lower debt, improves welfare when debt high
- No Dilution: Lower debt, reduced partial default, improves welfare when debt low

Reference Model: Renegotiation with Bargaining

Model with full default + renegotiation with alternating offers between country and lenders



- ▶ Default episodes short in reference model
- ▶ Debt collapses upon default + burst borrowing and consumption upon re-entry
- ▶ Misses debt dynamics and amplification of default episodes

Conclusions

- ▶ Prior work focuses on dynamics prior to default, with fresh start after default
- ▶ Document rich dynamics during default and amplification of default
- ▶ Propose a theory with partial default: default leads to more default
 - ▶ Useful for rationalizing dynamics during default episodes, properties of partial default
- ▶ Theory potentially useful to analyze restructuring mechanisms
 - ▶ That can actually lead to a reduction in debt burden