

BANK FOR INTERNATIONAL SETTLEMENTS



# BIS Working Papers No 537 Exchange rates and

# Exchange rates and monetary spillovers

by Guillaume Plantin and Hyun Song Shin

# Monetary and Economic Department

January 2016

JEL classification: F32, F33, F34

Keywords: Currency appreciation, capital flows, global games

BIS Working Papers are written by members of the Monetary and Economic Department of the Bank for International Settlements, and from time to time by other economists, and are published by the Bank. The papers are on subjects of topical interest and are technical in character. The views expressed in them are those of their authors and not necessarily the views of the BIS.

This publication is available on the BIS website (www.bis.org).

© Bank for International Settlements 2016. All rights reserved. Brief excerpts may be reproduced or translated provided the source is stated.

ISSN 1020-0959 (print) ISSN 1682-7678 (online)

# Exchange rates and monetary spillovers<sup>\*</sup>

Guillaume Plantin Sciences Po Hyun Song Shin Bank for International Settlements

January 17, 2016

#### Abstract

When does the combination of flexible exchange rates and domestic inflation-oriented monetary policy guarantee insulation from global financial conditions? We examine a dynamic global game model of international portfolio flows where, for some combination of parameters, the unique equilibrium exhibits the observed empirical feature that currency appreciation goes hand-in-hand with lower domestic interest rates and higher credit growth. When reversed, tighter monetary conditions go hand-in-hand with capital outflows and currency depreciation.

JEL codes: F32, F33, F34 Keywords: Currency appreciation, capital flows, global games

<sup>\*</sup>The views expressed here are those of the authors and not necessarily those of the Bank for International Settlements. We thank Patrick Bolton, Nicolas Coeurdacier, Doug Diamond, Andy Filardo, Itay Goldstein, Urban Jermann, Emanuel Kohlscheen, Pete Kyle, Karen Lewis, Ady Pauzner, Lasse Pedersen, Luiz Pereira, Richard Portes, Ricardo Reis, Hélène Rey, Phurichai Rungcharoenkitkul, Jeremy Stein and James Yetman for their comments. Plantin acknowledges support from a European Research Council Starting Grant (N°263673 – RIFIFI).

# 1 Introduction

Milton Friedman's essay on the case for flexible exchange rates (Friedman (1953)) is a classic statement of the role of floating exchange rates in allowing an economy to adjust to external shocks. In the same spirit, the flexible exchange rate version of the Mundell-Fleming model (Fleming (1962), Mundell (1963)) lays out the case for how flexible exchange rates allow monetary authorities to pursue domestic macroeconomic objectives in a world of free capital flows.

Post-crisis discussions of monetary spillovers have revisited these classic propositions. The BIS report on global liquidity (BIS (2011)) is a recent exposition of cross-border monetary spillovers, and it has been followed by an active literature which has examined the extent to which floating exchange rates are sufficient to insulate monetary policy from external developments (see, for instance, Agrippino and Rey (2014), Rey (2013, 2014), Bruno and Shin (2015a, 2015b)).

We shed further light on the economic mechanisms behind monetary spillovers in a regime of floating exchange rates. We explore a dynamic global game model of international investment flows where global investors interact with each other and with a central bank that pursues monetary policy aimed at domestic price developments. Our focus is on the exchange rate channel of monetary policy; we ask how currency appreciation is related to domestic interest rates and credit growth in an environment with flexible exchange rates.

Figure 1 overleaf summarises the type of empirical regularity that motivates the questions in our paper. Figure 1, taken from Hofmann, Shim and Shin (2016), depicts the returns on emerging market sovereign bonds in diversified bond mutual funds, where returns are measured both in local currency and US dollar terms. The blue scatter is the local currency return (in per-cent) against local currency yield changes (in percentage points), while the red scatter is the US dollar return plotted against the same yield change. The right-hand panel is a magnified version of the scatter chart for one of the funds.<sup>1</sup>

In all the panels in Figure 1, the red and blue scatter plots diverge, with the red line steeper than the blue line. The right-hand half of each panel is the region where yields have

<sup>&</sup>lt;sup>1</sup>See Hofmann, Shim and Shin (2016) for the full list of bond mutual funds and other details.



Figure 1: Dollar and local currency returns on emerging market sovereign bond funds. Left-hand panel shows monthly returns on twenty emerging market sovereign bond funds examined in Hofmann, Shim and Shin (2015). Blue scatter is local currency return (in per cent) against the domestic bond yield change (in percentage points). Red scatter is US dollar return against the yield change. See Hofmann, Shim and Shin (2015) for details.

risen, and so returns are negative, but dollar returns are lower than local currency returns, implying that the local currency has depreciated against the dollar. Conversely, the lefthand side of the panels corresponds to states where domestic interest rates fall. In these states, the local currency tends to *appreciate* against the dollar.<sup>2</sup> In either case, exchange rate changes are informative about shifts in monetary conditions; currency appreciation is associated with more accommodative monetary conditions.

The combination of rapid credit growth and an appreciating currency has been a good early warning indicator of booms in emerging markets that precede crises. Gourinchas and Obstfeld (2012) conduct an empirical study using data from 1973 to 2010 and find that two factors emerge consistently as the most robust and significant predictors of financial crises, namely a rapid increase in leverage and a sharp real appreciation of the currency.

We offer a parsimonious model that sheds light on a possible mechanism through which

<sup>&</sup>lt;sup>2</sup>Hofmann, Shim and Shin (2016) show in a panel investigation of emerging market economies that the relationship between exchange rates and financial conditions shown in Figure 1 holds more generally for sovereign yields, CDS spreads and as well as for forward rate adjusted spreads from the swapped return spread defined by Du and Schreger (2015).

global financial conditions exert influence on credit and asset prices in economies with flexible exchange rates. We do so in two steps. In the first step, we examine a perfect foresight model in which global investors have access to both the dollar bond market and the local currency bond market of a small open economy. Global investors form portfolios in anticipation of monetary policy pursued by the central bank, which employs a monetary policy rule that takes account of the overall domestic price developments.

We show that for reasonable parameters of the model, there are two stable steady state solutions – one associated with capital inflows and the other with capital outflows. The steady state with capital inflows is associated with low domestic interest rates, while the steady state with capital outflows is associated with high domestic interest rates.

In the second step of our analysis, we build a dynamic model based on ingredients from the steady state analysis. We introduce shocks to the dollar interest rate and use the global game technique of Burdzy, Frankel and Pauzner (2001) to refine the outcome of the model to a unique solution. We show that the state space can be partitioned into two regions – a region where all investors pile into the local currency bond, and one in which they all pile out. The transition between the two regions can be triggered by small fluctuations in the US dollar interest rate and the endogenous changes in domestic financial conditions. The unique equilibrium features dynamics that are reminiscent of boom-bust cycles in which prolonged episodes of credit growth and capital inflows, benign domestic financial conditions. Subsequent small increases in the US rate do not immediately reverse the up-phase of the cycle but will abruptly reverse when a "tantrum" boundary is reached. Hitting the "tantrum" boundary triggers a large currency depreciation, capital outflows and a crash in the domestic bond market.

# **Related literature**

The relationship between exchange rates and leverage is our point of contact with the literature on the determinants of vulnerability to financial crises. In addition to Gourinchas and Obstfeld (2012) mentioned above, Schularick and Taylor (2012) similarly highlight the role of leverage in financial vulnerability, especially that associated with the banking sector. There is a large and growing literature on the determinants of emerging market crises that emphasise the association between exchange rate appreciation and over-extension of the financial system (Kaminsky and Reinhart (1999), Borio and Disyatat (2011), among others).

Our results complement the recent work on the *risk-taking channel of currency appreciation*, introduced by Bruno and Shin (2015a, 2015b) in the context of cross-border banking, whereby currency mismatches on borrowers' balance sheets lead to credit supply effects of exchange rate fluctuations. The risk-taking channel relies on Value-at-Risk (VaR)-induced behaviour that is sensitive to tail risks of credit portfolios. Hofmann, Shim and Shin (2016) apply the risk-taking channel to domestic currency sovereign yields through shifts in the tail risk of diversified local currency sovereign bond portfolios. Whereas existing models of the risk-taking channel are static, our global game model solves for the dynamic path of the key macro variables. The trade-off is that our model is a more parsimonious model of decentralised portfolio choice.

In terms of the theoretical tools, our approach is most closely related to models of financial instability which involve coordination problems and self-fulfilling speculative episodes, such as the early currency crisis models of Obstfeld (1996). In a similar spirit, Farhi and Tirole (2012) and Schneider and Tornell (2004) offer related models of "collective moral hazard" in which the government bails out speculators if their aggregate losses are sufficiently large, thereby inducing a coordination motive among speculators. We formalise the dynamic coordination game among investors using the dynamic extension of global-game methods developed by Frankel and Pauzner (2000) and Burdzy, Frankel and Pauzner (2001) to obtain a unique equilibrium outcome. We show that these global game tools can be adapted to the situation where coordination motives coexist with congestion effects. This is important because most financial models with coordination motives also feature congestion effects. In a model of bank run, Goldstein and Pauzner (2005) adapt static global game techniques to the case in which strategic complementarities similarly fail to hold everywhere. In a model of sovereign-debt refinancing, He, Krishnamurthy and Milbradt (2015) also apply global game techniques in a context in which a large debt size comes at the benefit of smaller congestion effects but at the cost of a higher rollover risk. Most closely related to our work, He and Xiong (2012) apply the equilibrium selection techniques developed by Burdzy, Frankel and Pauzner (2001) in a dynamic financial context - the rollover of short-term debt.

Our paper is related to the literature on portfolio choice in incomplete markets. Garleanu, Panageas and Yu (2015) present a model in which investors face costs to extend their participation in markets located on a circle for diversification purposes. Our result that the profitability of investment increases in the weight of others' participation bears similarities with their finding that participation and leverage reinforce each other. In their setup, increased participation leads to an increase in the attainable Sharpe ratio, which triggers more leverage and thus higher gains from participation and diversification.

Finally, in a recent contribution, Gabaix and Maggiori (2015) introduce financial intermediaries that operate in incomplete global financial markets by intermediating gains from trade between countries. Financial constraints imply that these institutions supply liquidity inelastically, which generates risk premia on cross-currency positions. We also model global investors as financial institutions operating in incomplete markets. In our setup, however, these institutions source funds in one country and end up amplifying financial fluctuations in the destination country. Thus we reach very different conclusions regarding the relationship between limits to arbitrage and excess returns. In our setup, excess returns are self-fulfilling and hence depend on the coordination outcome. Second, whereas tighter financial constraints lead to larger excess returns in Gabaix and Maggiori (2015), the opposite holds in our setup. Less constrained traders exert greater influence; they have a freer hand at reaping higher excess returns, and thereby generate greater market amplification by doing so.

# 2 Benchmark model

Time is discrete and is indexed by  $t \in \{1, 2, \dots\}$ . There are two types of agents, households populating a small open economy and global investors. There is a single tradable good that has a fixed unit price in US dollars.

#### 2.1 Households

The households live in a small open economy. They use a domestic currency that trades at  $S_t$  dollars per unit at date t, where the exchange rate  $S_t$  will be determined in equilibrium.

At each date, a unit mass of households are born. Households live for two dates, consume when young and old, and work when old. Each household receives an initial endowment at birth with nominal value  $P_tW \ge 0$ , where  $P_t$  is the domestic price level.<sup>3</sup> The cohort that is born at date t has quasi-linear preferences over bundles of consumption and labour  $(C_t, C_{t+1}, N_{t+1})$ 

$$U(C_t, C_{t+1}, N_{t+1}) = \ln C_t + \frac{C_{t+1} - N_{t+1}^{1+\eta}}{R},$$
(1)

where  $\eta > 0$  and R is the subjective discount rate.

Domestic consumption services  $C_t$  are produced by combining the tradable good  $C_t^T$  and two nontradable goods  $C_t^{N_1}$  and  $C_t^{N_2}$  according to the technology

$$C_t = \frac{\left(C_t^T\right)^{\alpha} \left(C_t^{N_1}\right)^{\beta} \left(C_t^{N_2}\right)^{\gamma}}{\alpha^{\alpha} \beta^{\beta} \gamma^{\gamma}},\tag{2}$$

where  $\alpha$ ,  $\beta$ ,  $\gamma \in (0,1)$  and  $\alpha + \beta + \gamma = 1$ . Domestic firms set up by old households use labour input to produce. Due to quasi-linear preferences, our results do not depend on the specification of the firms' production functions. All that is needed is that both nontradable goods are produced in finite, non-zero quantities at each date. Households collect labour income and the profits from their firms when old.

An important ingredient of the model is that the prices of the nontradable goods are less flexible than that of the tradable good.<sup>4</sup> We formalise this feature as follows. First, we posit that the tradable good has a flexible price  $P_t^T$ , and that the law of one price holds ("PPP at the docks"). Second, the first nontradable good  $N_1$  also has a fully flexible price  $P_t^{N_1}$ . A linear technology enables the transformation of each date-*t* unit of  $N_1$  into *F* units of the tradable good, where F > 0. The second nontradable good  $N_2$  has a fixed price that we

<sup>&</sup>lt;sup>3</sup>If the endowment of young households is zero, then the global investors cannot have an aggregate short position in domestic bonds. A strictly positive endowment plays no other role than allowing such short positions.

<sup>&</sup>lt;sup>4</sup>This is consistent with evidence documented by Burstein, Eichenbaum and Rebelo (2005).

normalise to 1 without loss of generality. Denoting  $P_t^T$ ,  $P_t^{N_1}$  and  $P_t^{N_2}$  the respective prices of these three goods, we have:

$$P_t^T S_t = 1, (3)$$

$$P_t^{N_1} = F P_t^T, (4)$$

$$P_t^{N_2} = 1.$$
 (5)

Equation (3) is the statement of the flexible price of the tradeable good. Equation (4) states that domestic households are indifferent between purchasing the tradable good or producing it out of  $N_1$ . Finally, (5) is the statement of the rigidity of  $N_2$ 's price.

The introduction of the nontradable good with flexible price  $N_1$  allows us to decouple the openness of the economy as measured by  $1 - \beta - \gamma$  from the flexibility of the overall price index to changes in the tradeable goods price, as measured by  $1 - \gamma$ . The parameters  $\beta$  and  $\gamma$  are defined in (2). The price index is given by

$$P_t = (P_t^T)^{\alpha} (P_t^{N_1})^{\beta} (P_t^{N_2})^{\gamma}$$
$$= (P_t^T)^{1-\gamma} F^{\beta}, \qquad (6)$$

where (6) follows from (4) and (5).

Households have access to the domestic currency bond, which is a risk-free one-period bond in zero net supply that is denominated in the domestic currency. The nominal interest rate on these bonds is set by the domestic central bank according to a rule to be described below.

#### 2.2 Global investors

A unit mass of global investors have access to both the local currency bond market and to US dollar-denominated bonds. The exogenous nominal return on US dollar bonds is denoted by  $I^* > 0$ . Global investors consume outside the local economy, and their utility is increasing in the consumption of the tradable good.<sup>5</sup>

<sup>&</sup>lt;sup>5</sup>Whether they also derive utility from consuming other goods, and the curvature of their utility function, are immaterial. This is only so because the economy is deterministic, and will be relaxed in the main section with the dynamic model.

In forming their financial portfolios, global investors face limits on the size of their exposures in domestic bonds, reflecting leverage constraints or exposure caps imposed by internal risk limits. We assume that the position of any investor in domestic bonds must lie in the interval  $[P_tL^-, P_tL^+]$ , where these limits are denominated in the domestic currency and

$$L^- > -W$$

which ensures that households always consume positively.<sup>6</sup> We do not consider the microfoundations of these limits. As is well-known, they could result, for example, from agency problems within globally investing firms such as a cash-flow diversion problem.

The return to an investor to investing in the local currency bond relative to the return on dollar bonds is given by

$$\Theta_{t+1} = \frac{S_{t+1}}{S_t} \frac{I_{t+1}}{I^*}$$
(7)

We may interpret  $\Theta_{t+1}$  as the return to a carry trade position in which the investor borrows dollars at rate  $I^*$  and then invests the proceeds in the local currency bond yielding  $I_{t+1}$ . Uncovered interest parity (UIP) holds when  $\Theta_{t+1} = 0$ . Given the deterministic environment, optimal portfolio choice implies:

$$L_t \begin{cases} = L^+ & \text{if } \Theta_{t+1} > 1, \\ = L^- & \text{if } \Theta_{t+1} < 1, \\ \in (L^-, L^+) & \text{if } \Theta_{t+1} = 1. \end{cases}$$

#### 2.3 Monetary policy rule

We suppose that the domestic monetary authority sets the nominal interest rate between tand t + 1,  $I_{t+1}$ , following the interest-rate feedback rule:

$$I_{t+1} = R \left(\frac{P_t}{P_{t-1}}\right)^{1+\Phi} \tag{8}$$

where

$$\Phi > 0 \tag{9}$$

<sup>&</sup>lt;sup>6</sup>Setting lending limits in real terms simplifies the exposition but is not crucial. Nominal rigidities in trading limits would actually amplify our results.

The interest rate rule (8) follows the Taylor principle from (9) in that the nominal interest rate reacts more than one-for-one to the price level change. The Taylor principle is necessary for a determinate solution in many classes of monetary models (Taylor (1993), Woodford (2001)), and our model also shares this feature as we see below.

Given our quasi-linear preferences, the Euler equation can be written as

$$I_{t+1} = \frac{P_{t+1}}{P_t} \frac{R}{(L_t + W)}$$
(10)

# 2.4 Steady state solution

We are now equipped to solve for the perfect foresight steady states of this economy. We denote  $L_t$  the real aggregate borrowing by young households from global investors at date t, possibly negative. A steady state must be such that the domestic economy is in equilibrium and global investors form optimal portfolios at each date.

We introduce the following notation.

$$r = \ln R,$$
  

$$\delta = \ln \left(\frac{R}{I^*}\right),$$
  

$$\theta_t = \ln \Theta_t,$$
  

$$i_t = \ln I_t,$$
  

$$s_t = \ln S_t,$$
  

$$l_t = \ln(L_t + W),$$
  

$$\pi_{t+1} = \ln \left(\frac{P_{t+1}}{P_t}\right).$$

The Euler equation (10) and the interest-rate rule (8) can be gathered as follows.

$$i_{t+1} = r - l_t + \pi_{t+1} \tag{11}$$

$$i_{t+1} = r + (1 + \Phi) \pi_t \tag{12}$$

Together, they define a linear-difference equation for the path of inflation:

$$\pi_t = \frac{\pi_{t+1} - l_t}{1 + \Phi} \tag{13}$$

which has a unique non-exploding solution:

$$\pi_t = -\sum_{k\ge 0} \frac{l_{t+k}}{(1+\Phi)^{k+1}} \tag{14}$$

Equation (14) shows that current inflation consists of all the future capital inflow shocks  $(l_{t+k})_{k\geq 0}$ . The Taylor principle ensures that  $\pi_t$  is well-defined, since  $l_{t+k}$  is bounded and  $\Phi > 0$ . Our expression for  $\pi_t$  shows that our model shares the generic feature of many monetary models in that inflation reflects anticipated future "policy shocks" (see e.g. Cochrane (2011)). In our context, the "shocks" are not exogenous policy shocks, but rather are the consequence of optimal portfolio choice by investors.

Using (6) and (3), we have:

$$\pi_{t+1} = -(1-\gamma)(s_{t+1} - s_t) \tag{15}$$

Equation (15) is our exchange rate pass-through equation that expresses inflation in terms of exchange rate depreciation. As a rule of thumb, the exchange rate pass-through is normally thought of lying between 0.1 and 0.3 (Klau and Mihaljek (2008) and Gopinath (2015)), which implies a value of  $\gamma$  between 0.7 and 0.9. The magnitude of  $\gamma$  will play a key role in our analysis.

Plugging (15) and (10) in (7), we have

$$\theta_{t+1} = s_{t+1} - s_t + i_{t+1} - \ln I^*,$$
  
=  $-\frac{1}{1 - \gamma} \pi_{t+1} + \pi_{t+1} - l_t + \delta,$  (16)

$$= \frac{\gamma}{1-\gamma} \sum_{k\geq 0} \frac{l_{t+k+1}}{(1+\Phi)^{k+1}} - l_t + \delta.$$
 (17)

where (16) follows from the exchange rate pass-through equation (15) and the Euler equation, and (17) follows from the solution for for  $\pi_{t+1}$  given by (14).

We now determine the steady states in which the debt level l is constant over time. We introduce

$$\underline{l} \equiv \ln(W + L^{-}), \tag{18}$$

$$\overline{l} \equiv \ln(W + L^+). \tag{19}$$

**Proposition 1** If there is  $l^* \in (\underline{l}, \overline{l})$  such that

$$\frac{\gamma - \Phi \left(1 - \gamma\right)}{\left(1 - \gamma\right)\Phi} l^* + \delta = 0.$$

then  $l = l^*$  is a steady state in which uncovered interest parity (UIP) holds. If  $\Phi(1-\gamma) > \gamma$ , there is no other steady state solution. However, if  $\Phi(1-\gamma) < \gamma$ , there are two further steady state solutions; there is a steady state with maximum capital inflows  $(l = \overline{l})$ , and there is a steady state with maximum capital outflows  $(l = \underline{l})$ .

Proposition 1 highlights the possibility of self-fulfilling capital flow surges and outflows as steady state solutions of our model. The parameter  $\gamma$  that determines the exchange rate pass-through to domestic inflation plays a key role whether surges and sudden stops are steady state solutions.

We have noted already that rules of thumb put  $\gamma$  between 0.7 and 0.9, while Taylor (1993) considered the Taylor rule coefficient  $\Phi = 0.5$ . Thus,  $\Phi(1 - \gamma)$  takes values around 0.05 to 0.15, which is much smaller than  $\gamma$  itself. Hence, for reasonable values of  $\Phi$  and  $\gamma$ , we fall in the region where multiple steady state solutions hold, and self-fulfilling surges and outflows are sustainable as steady state solutions.

We prove Proposition 1. First, note that for l fixed, the relative return to investing in the local currency bond given by (17) can be written as

$$\theta = \frac{\gamma - \Phi \left(1 - \gamma\right)}{\left(1 - \gamma\right)\Phi} l + \delta \tag{20}$$

Let  $l^* \in (\underline{l}, \overline{l})$  be such that  $\theta = 0$ . Then investors are indifferent between investing in the local currency bond or the dollar bond. Hence,  $l^*$  is a steady state solution of our model, corresponding to the mixed strategy equilibrium of the one-shot game between investors where proportion  $(l^* - \underline{l}) / (\overline{l} - \underline{l})$  invest in the local currency bond. If  $\Phi(1 - \gamma) > \gamma$ , this is the only steady state solution, since  $\theta$  is decreasing in l.

Now consider the case where  $\gamma > \Phi(1-\gamma)$ . In this case, we have two further steady state solutions corresponding to the corner solutions  $l = \overline{l}$  and  $l = \underline{l}$ .

First, suppose that all investors choose to invest in the local currency bond. Then  $l = \overline{l}$ , so that  $\theta > 0$ , implying that investing in the local currency bond is strictly better than investing in the dollar bond. Hence, all investors invest in the local currency bond, thereby sustaining maximum inflows  $l = \overline{l}$  as a steady state solution. Conversely, suppose that all investors choose to invest in the dollar bond. Then  $l = \underline{l}$ , so that  $\theta < 0$ , implying that investing in the dollar bond is strictly better. Hence all investors invest in the dollar bond, sustaining  $l = \underline{l}$  as a steady state.

Another way to gain intuition behind Proposition 1 is to see the strategic interactions across traders at different dates. For this, see the expression for  $\theta_{t+1}$  given by equation (17). This expression shows how the excess return to engaging in the carry trade depends on current inflows  $l_t$  and the path of all future inflows  $(l_{t+k})_{k\geq 1}$ . Current inflow  $l_t$  has a negative impact on the current return on carry trade because it makes bonds expensive (term  $-l_t$  in (17)). In contrast, future inflows resulting from future carry trades are actually *beneficial* for the current return to the carry trade, since excess return  $\theta_t$  to the carry trade is *increasing* in future inflows  $(l_{t+k})_{k\geq 1}$ .

Our solution also highlights the pivotal role played by the size of exchange rate passthrough. In (16), there are two opposing effects of future inflation  $\pi_{t+1}$  on current excess returns. There is the positive effect coming from future inflows. However, there is also a dampening effect on returns that comes from lower nominal domestic interest rates that result from downward pressure on inflation due to the currency appreciation. However, provided that the exchange rate pass-through is small, the appreciation effect due to future inflows more than offsets the dampening effect of lower inflation and lower nominal interest rates. Hence, the parameter  $\gamma$  which determines the exchange rate pass-through in the model plays a pivotal role. If the pass-through is small enough, the future appreciation pressure on the domestic currency resulting from continued capital inflows more than offsets the lower nominal interest rate that comes from lower inflation.

In passing, we note an important feature of the monetary policy rule. From Proposition 1, a sufficiently aggressive interest rule ( $\Phi$  sufficiently large) would suffice to pick out the steady state in which UIP holds. Alternatively, the commitment to respond directly to the impact of capital flows would also suffice to pick out the UIP steady state. To see this, note

that replacing rule (12) with a rule of the form:

$$i_{t+1} = r_{t+1} + (1+\Phi) \pi_t \tag{21}$$

would eliminate the effect of inflows on the domestic CPI. Notice, however, that the steady states with large capital flows described in Proposition 1 could still arise under such a rule in a richer model of nominal rigidities. Suppose for example that the consumption boom due to inflows results in inflation in the price of nontradable goods. If rule (21) maintains the overall price index constant, then this inflationary pressure must be compensated with deflation in the price of the tradable good. Such a deflation, if sufficiently large, will again create room for self-fulfilling excess returns on carry trades through the associated increase in the nominal exchange rate.

#### 2.5 Properties of steady state

We now explore some key features of the steady state of our model with an eye on the empirical implications on the co-movement between the nominal interest rate, the exchange rate and credit driven by capital flows.

Consider first the solution for the nominal interest rate in our model. From the expression for  $i_{t+1}$  given by (12) and (14), we have

$$i_{t+1} = r + (1 + \Phi) \pi_t$$
  
=  $r - l_t - \sum_{k>1} \frac{l_{t+k}}{(1 + \Phi)^k}$  (22)

The nominal interest rate  $i_{t+1}$  is therefore decreasing in future credit financed by capital inflows. Meanwhile, our solution for exchange rate appreciation can be obtained from the pass-through equation (15) and equation (14). We have

$$s_{t+1} - s_t = -\frac{1}{1 - \gamma} \pi_{t+1} = \frac{1}{1 - \gamma} \sum_{k \ge 1} \frac{l_{t+k}}{(1 + \Phi)^k}$$
(23)

In other words, future credit financed by capital inflows is associated with an appreciation of the domestic currency. The pass-through parameter  $1 - \gamma$  determines the size of the appreciation. The lower is the exchange rate pass-through, the sharper is the currency appreciation.

By putting together (22) and (23) we can at last address the empirical regularity depicted in Figure 1 between currency appreciation and domestic interest rates, mentioned at the outset of our paper. Recall that in Figure 1, we pointed to the empirical regularity between the returns on emerging market bonds and currency appreciation in which domestic currency appreciation against the dollar is associated with more permissive financial conditions in the form of lower domestic interest rates. Conversely, currency depreciation against the dollar is associated with tighter financial conditions in the form of *higher* domestic interest rates. The two steady states where  $(l_t)_{t\geq 1}$  take the corner solutions of  $l_t = \overline{l}$  and  $l_t = \underline{l}$  are associated with the extremes of the correlations. We summarise this finding in terms of the following proposition.

**Proposition 2** In the steady state with maximum capital inflows, the domestic currency appreciates and nominal interest rates are low. Uncovered interest parity fails, and dollar returns are lower than domestic currency returns. In the steady state with maximum capital outflows, the domestic currency depreciates and domestic nominal interest rates are high. Uncovered interest parity fails and dollar returns are higher than domestic currency returns.

Proposition 2 summarises the relationship between exchange rates and financial conditions depicted in the scatter charts in Figure 1. Uncovered interest parity fails in a strong sense. Not only does UIP fail to hold, the portfolio position of global investors is given by corner solutions - either the maximum capital inflows or maximum capital outflows.

So far, we have addressed the steady states only. The shortcoming of a steady state analysis is that it cannot address the switch from one steady state to another, nor the transition between steady states in response to shocks and other forces buffeting the economy. We therefore turn to a stochastic version of our benchmark model and employ global game techniques to tie down a unique dynamic solution. The goal of the analysis is to provide the theoretical foundations of the dynamics of an open economy in which surges of capital inflows can be explained alongside the sudden reversals that happen in practice.

# 3 Stochastic model

We proceed to develop a dynamic version of our model, and solve for the uniquely determined time paths by using perturbation methods due to Burdzy, Frankel and Pauzner (2001) that resemble global game methods, but which are better suited for dynamic contexts such as ours.

Begin by assuming that time is continuous. The fixed integer dates of the previous section are replaced by the arrival times of a Poisson process with intensity 1. Namely, at each arrival time  $T_n$ , a new cohort of households are born, and die at the next arrival time  $T_{n+1}$ . They value consumption and leisure only at these two dates, with preferences that are analogous to those in our benchmark setup:

$$\ln C_{T_n} + \frac{1}{R} E_{T_n} \left[ C_{T_{n+1}} - N_{T_{n+1}}^{1+\eta} \right].$$

At each arrival date  $T_n$ , the central bank sets a nominal rate  $I_{T_{n+1}}$  between  $T_n$  and  $T_{n+1}$  according to the rule:

$$I_{T_{n+1}} = R \left(\frac{P_{T_n}}{P_{T_{n-1}}}\right)^{1+\Phi}$$
(24)

Replacing integer dates with dates that arrive at a constant rate is not essential, and our setup is designed for tractability. It is designed to ensure that the global investors' portfolio choice problem is time homogeneous.

One departure in the dynamic model is to be more explicit about global investors' preferences in order to characterise their portfolio choice decision. We follow Gabaix and Maggiori (2015) in this respect. Global investors are a unit-mass continuum of financial institutions that can form zero-cost portfolios in bonds denominated in either currency at each date  $T_n$ with size within  $[P_{T_n}L^-, P_{T_n}L^+]$  (in units of the domestic currency). The date- $T_n$  trade is unwound at the next date  $T_{n+1}$  and the realised profit or loss is paid to the old households at this date. Each firm maximises the expected value of future consumption paid to all future households discounted at the households' subjective discount rate R.<sup>7</sup>

 $<sup>^{7}\</sup>mathrm{In}$  particular, the global investors' objective increases in the consumption of the tradable good as was assumed in Section 2.

The following two modifications to the benchmark model are key to generate equilibrium uniqueness.

First, we assume that the interest rate at which global investors borrow in US dollars between two arrival dates  $T_n$  and  $T_{n+1}$  is given by

$$I_{T_{n+1}}^* = R \left( 1 - w_{T_n} \right), \tag{25}$$

where  $w_t$  is a Wiener process with volatility  $\sigma$  and no drift. In this way, we introduce an exogenous stochastic component in the interest rate differential.

Second, we assume that the capital supplied by global investors is slow-moving in the following sense. Each global investor can revise its trading strategy only at switching dates that are generated by a Poisson process with intensity  $\lambda$ . These switching dates are independent across global investors. In between two switching dates, each global investor commits to a trading strategy and thus to lending a fixed real amount  $L_t \in [L^-, L^+]$  to each new cohort of households at each arrival date  $T_n$  (if any).

This model of slow-moving capital has a key property that will yield equilibrium uniqueness: Every global investor knows that some other global investors will revise their trading strategy almost surely between his current switching date and the next one.

Remark. (Arbitrage versus good deal and trading limits) It is important to stress that the exogenous trading limits  $[P_{T_n}L^-, P_{T_n}L^+]$  fulfill a very different role from that played in Section 2. In the previous section, it was necessary to impose such limits regardless of global investors' preferences because cross-currency positions were (possibly) textbook arbitrage opportunities given the deterministic environment. As is well-known, any agent with increasing utility over consumption has an infinite demand for an arbitrage opportunity absent any financial constraint. In the stochastic environment, we will see that carry trade portfolios generate losses with a non-zero probability in equilibrium. Thus, any risk-averse agent would form finite portfolios. Trading limits here only play the role of a very tractable substitute for risk aversion that is commonplace in models in which agents' attitude towards risk is not the main focus.<sup>8</sup>

<sup>&</sup>lt;sup>8</sup>In recent work, Albagli, Hellwig and Tsyvinski (2015) use a similar assumption to generate a high tractability and thus new insights in a standard noisy REE asset-pricing model. The binary portfolio choice of risk-neutral carry traders is particularly suited to our iterated-dominance solution.

Local risk-neutrality implies that global investors choose corner portfolios. We deem "long" a global investor who committed to maximum lending  $L^+$  at his last switching date, and "short" one who committed to the minimum lending  $L^-$ . Suppose that a global investor has a chance to revise his position at a date t such that

$$T_{n-1} < t < T_n. \tag{26}$$

Denoting  $T_{\lambda}$  his next switching date, its expected unit return from holding local currency bonds — the expected value from committing to lend one additional real unit to each future cohort until  $T_{\lambda}$  — is

$$\Theta_t = E_t \left[ \sum_{m \ge 0} \frac{1_{\{T_\lambda > T_{n+m}\}}}{R^m} \frac{P_{T_{n+m}} S_{T_{n+m}}}{P_{T_{n+m+1}} S_{T_{n+m+1}}} \left( \frac{S_{T_{n+m+1}} I_{T_{n+m+1}}}{S_{T_{n+m}} R} - 1 + w_{T_{n+m}} \right) \right]$$
(27)

Expression (27) states that the global investor earns the local currency bond return associated with each arrival date until he gets a chance to revise his position.<sup>9</sup>

We let  $x_t$  denote the fraction of global investors who are long at date t. Note that the paths of the process  $(x_t)_{t \in \mathbb{R}}$  must be Lipschitz continuous, with a Lipschitz constant smaller than  $\lambda$ . The aggregate real lending  $L_{T_n}$  taking place at an arrival date  $T_n$  is then equal to

$$L_{T_n} = x_{T_n} L^+ + (1 - x_{T_n}) L^-.$$
(28)

The evolution of the economy is fully described by two state variables – the exogenous state variable  $w_t$  and the endogenous state variable  $x_t$  which is a function of  $w_t$ . The exogenous state variable affects only the expected return on carry trade  $\Theta_t$  while the endogenous one affects both the carry trade return and the equilibrium variables  $(L_{T_n}, I_{T_n}, P_{T_n}, S_{T_n})$  of the domestic economy. We are now equipped to define an equilibrium.

**Definition.** An *equilibrium* is a process  $x_t$  that is adapted to the filtration of  $w_t$  and has Lipschitz-continuous paths such that:

<sup>&</sup>lt;sup>9</sup>To arrive at (27), note that investing one real unit at arrival date  $T_j$  costs USD  $P_{T_j}S_{T_j}$ . The net rate of return  $(S_{T_{j+1}}/S_{T_j})I_{T_{j+1}} - I_{T_{j+1}}^*$  applies to this dollar amount. The resulting consumption for old households at date  $T_{j+1}$  is then this USD profit divided by  $P_{T_{j+1}}S_{T_{j+1}}$ . Re-arranging and discounting these terms yields (27).

$$L_{T_n} = x_{T_n} L^+ + (1 - x_{T_n}) L^-, (29)$$

$$I_{T_{n+1}} = R \left(\frac{P_{T_n}}{P_{T_{n-1}}}\right)^{1+\Phi},$$
(30)

$$P_{T_n} = \left(P_{T_n}^T\right)^{1-\gamma} F^{\beta},\tag{31}$$

$$P_{T_n}^T S_{T_n} = 1, (32)$$

$$E_{T_n}\left[\frac{I_{T_{n+1}}P_{T_n}}{P_{T_{n+1}}}\right] = \frac{R}{L_{T_n} + W},$$
(33)

$$\frac{dx_t}{dt} = \begin{cases} -\lambda x_t & \text{if } \Theta_t < 0, \\ \lambda(1 - x_t) & \text{if } \Theta_t > 0. \end{cases}$$
(34)

Equations (30) to (33) state that the domestic economy is in equilibrium given the paths of  $x_t$ . Equation (34) states that global investors make optimal individual decisions. They take long positions at switching dates at which the expected return on the investment is positive (or remain long if this was their previous position), and take short positions if this is negative.

Notice that relations (30) to (32) are identical to their counterparts in the perfect foresight case except for the re-labelling of dates. They are in particular log-linear. Conversely, the Euler equation (33) now features an expectation over the inverse of inflation given the stochastic environment. We will assume for the remainder of the paper that  $W + L^-$  and  $W + L^+$  are sufficiently close to 1 that  $\underline{l}$  and  $\overline{l}$  defined in (18) and (19) are sufficiently close to 0, so that we can use the approximation:

$$\ln E_t \left[ \frac{P_{T_n}}{P_{T_{n+1}}} \right] \simeq -E_t \left[ \ln \frac{P_{T_{n+1}}}{P_{T_n}} \right].$$
(35)

This implies of course that we restrict the analysis to the impact of relatively small capital inflows. Up to this log-linearization, we have

**Proposition 3** Suppose that

$$\gamma > \Phi \left( 1 - \gamma \right). \tag{36}$$



Figure 2: Equilibrium dynamics. The frontier f divides (w, x)-space into two regions. In the unique equilibrium, lending increases in the right-hand region and declines in the left.

For  $\lambda$  sufficiently small, there exists a unique equilibrium defined by a decreasing Lipschitz function f such that

$$\frac{dx_t}{dt} = \begin{cases} -\lambda x_t & \text{if } w_t < f(x_t), \\ \lambda(1-x_t) & \text{if } w_t > f(x_t). \end{cases}$$
(37)

The frontier f divides the (w, x)-space into two regions. Proposition 3 states that in the unique equilibrium, any trader takes on a long position when the system is to the right of the frontier f at his switching date, and a short position when it is on the left of the frontier. Thus, lending positions (and therefore the exchange rate) will tend to rise in the right-hand region, and tend to fall in the left-hand region, as indicated by the arrows in Figure 2.

The expected return on the carry trade at date t is zero if and only if  $w_t = f(x_t)$ . It is positive if  $(w_t, x_t)$  is on the right of the frontier f in the (w, x)-space and negative if it is on the left of f.

The dynamics of  $x_t$  implied by the unique equilibrium follow:

$$dx_t = \lambda \left( \mathbf{1}_{\{w_t > f(x_t)\}} - x_t \right) dt, \tag{38}$$

where  $1_{\{.\}}$  denotes the indicator function that takes the value 1 when the condition inside

the curly brackets is satisfied. These processes are known as *stochastic bifurcations*, and are studied in Bass and Burdzy (1999) and Burdzy, Frankel and Pauzner (1998). These mathematics papers establish in particular that for almost every sample path of  $w_t$ , there exists a unique Lipschitz solution  $x_t$  to the differential equation (38) defining the price dynamics for f Lipschitz decreasing.

The main features of these dynamics can be seen from Figure 2. Starting on the frontier, a positive shock on w will pull the system on the right of it. Unless the path of  $w_t$  is such that a larger negative shock brings it back on the frontier immediately, a more likely scenario is that lending grows for a while so that  $x_t$  becomes close to 1, in which case  $\frac{dx_t}{dt}$  becomes close to 0. If cumulative negative shocks on w eventually lead the system back to the left of the frontier, then there are large outflows

$$\frac{dx_t}{dt} \simeq -\lambda$$

Condition (36) is the same as the one that generates multiple steady-states in the perfectforesight case. It is worthwhile commenting on the additional condition that capital move sufficiently slowly ( $\lambda$  sufficiently small). This condition guarantees that the frontier f is decreasing, and thus that the portfolio choice decision generates a coordination motive between investors.

To better grasp the role of the coordination motive, notice that if a global investor expects other global investors to take long positions in the future, then he expects the exchange rate to appreciate. This implies that on one hand, the currency will be expensive when he purchases it to lend. On the other hand, it will keep appreciating over the duration of the loan, thereby generating a positive return. The former effect is akin to a congestion effect. Other traders make the trade more expensive and thus less desirable. Conversely, the latter effect is destabilising as future long positions make taking on a long position more appealing. That  $\lambda$  be sufficiently small ensures that this latter effect offsets the former congestion effect because aggregate lending does not converge too quickly to its maximum value. Thus a global investor with a current switching date is more likely to have a chance to lend before the currency becomes too expensive, and its upside potential too small. This congestion effect is the salient difference between our setup and that studied by Burdzy, Frankel and Pauzner.

Note that even if the frontier is increasing, it is still the case that small shocks  $w_t$  can have a large impact on total investment positions provided it is sufficiently steep in the (w, x)plane. We focus on the case of a decreasing frontier

## 3.1 **Proof of proposition**

The proof of Proposition 3 essentially extends to this stochastic environment the logic leading to the perfect foresight results in Proposition 1. In a first step, we derive an expression of the expected return on carry trades (27) as a function of the future flows  $(l_{t+s})_{s\geq 0}$  and of the interest-rate differential  $w_t$  that is the stochastic counterpart of equation (17). Second, we use this expression to solve for a Lipschitz process that satisfies (34). This latter step is the equivalent of the one that consisted in solving for feasible steady states given the expected return for global investors (17) under perfect foresight.

More precisely, the first step consists in using relations (30) to (33) to express the nominal exchange rate and interest rate as functions of the expected future paths of capital inflows  $L_t$ . This yields in turn a relatively simple expression for the expected return on the carry trade  $\Theta_t$  as a function of these expected capital inflows:

Lemma 4 At first-order, the expected return on the carry trade is

$$\Theta(w_t, x_t) = \int_0^{+\infty} \left( \left( \frac{\chi \omega}{\omega - \rho - \lambda} - 1 \right) e^{-(\lambda + \rho)v} - \frac{\chi \omega}{\omega - \rho - \lambda} e^{-\omega v} \right) E_t \left[ l_{t+v} \right] dv + \frac{w_t}{\lambda + \rho},$$
(39)

$$l_t = \ln(L_t + W) \simeq x_t \overline{l} + (1 - x_t) \underline{l}, \tag{40}$$

$$\rho = 1 - \frac{1}{R},\tag{41}$$

$$\omega = \frac{\Phi}{1 + \Phi},\tag{42}$$

$$\chi = \frac{7}{(1-\gamma)\Phi}.\tag{43}$$

The proof of Lemma 4 is given in the Appendix.

The factor that discounts future capital inflows in (39):

$$\left(\frac{\chi\omega}{\omega-\rho-\lambda}-1\right)e^{-(\lambda+\rho)v}-\frac{\chi\omega}{\omega-\rho-\lambda}e^{-\omega v},\tag{44}$$

is first negative, then positive as v spans  $[0, +\infty)$ .<sup>10</sup> This formalizes the above comment that future long traders create a congestion effect for the current trader. The earliest inflows have a negative impact on  $\Theta$  because they make the domestic currency expensive. The more remote inflows are desirable as the current trader is more likely to have lent before they occur. The following lemma establishes conditions under which the congestion effect is not too important.

**Lemma 5** Suppose that  $\chi > 1$ . There exists  $\overline{\lambda}$  such that for all  $\lambda \leq \overline{\lambda}$ , the following is true. Suppose that two processes  $x_t^1$  and  $x_t^2$  satisfy

$$0 < x_0^1 \le x_0^2 < 1,$$
  
For  $i = 1, 2, \ dx_t^i = \lambda \left( \mathbb{1}_{\left\{ w_t > f^i(x_t^i) \right\}} - x_t^i \right) dt,$ 

where  $f^i$  is decreasing Lipschitz and  $f^2 \leq f^1$ . Then

$$\Theta(w_t, x_0^2) \ge \Theta(w_t, x_0^1). \tag{45}$$

The inequality is strict if  $f^1 \neq f^2$  and/or  $x_0^1 \neq x_0^2$ .

The proof of Lemma 5 is in the Appendix.

Lemma 5 states that if (36) holds and  $\lambda$  is sufficiently small, then future inflows make current carry trades more attractive because the reinforcing effect overcomes the congestion effect. In the balance of the paper, we suppose that the conditions in Lemma 5 are satisfied. We now show that there is in this case a unique Lipschitz process  $x_t$  that satisfies the equilibrium conditions.

First, the proof of Lemma 5 also shows that the case in which  $x_t$  obeys  $\frac{dx_t}{dt} = -\lambda x_t$  for all  $u \ge 0$  corresponds to a lower bound on the expected carry-trade return. When  $x_t$  obeys such dynamics, there exists a frontier  $f_0$  such that

$$w_t = f_0(x_t) \implies \Theta(x_t, w_t) = 0 \tag{46}$$

<sup>&</sup>lt;sup>10</sup>Notice that this is so regardless of the sign of  $\omega - \rho - \lambda$ .

The frontier  $f_0$  is decreasing from Lemma 5 (with  $f^1 = f^2 = +\infty$ ) and is clearly affine and thus Lipschitz.<sup>11</sup> Thus an admissible equilibrium process must be such that investors who have a chance to switch when the system is on the right of  $f_0$  go long.

Define now  $f_1$  such that

$$w_t = f_1(x_t) \implies \Theta(x_t, w_t) = 0 \tag{47}$$

if for all  $u \ge 0$ ,

$$\frac{dx_{t+u}}{du} = \begin{cases} -\lambda x_{t+u} & \text{if } w_{t+u} < f_0(x_{t+u}), \\ \lambda(1-x_{t+u}) & \text{if } w_{t+u} > f_0(x_{t+u}), \end{cases}$$
(48)

That is,  $f_1$  is such that a global investor is indifferent between going long and going short when the system is on  $f_1$  at his switching date if he believes that other traders go long if and only if they are on the right of  $f_0$ . This function  $f_1$  must be decreasing. Suppose otherwise that two points (w, x) and (w', x') on  $f_1$  satisfy

$$x' > x,$$
$$w' \ge w.$$

Then applying Lemma 5 with  $f^2 = f_0$ ,  $f^1 = f_0 + w' - w$  contradicts that both points generate the same expected carry trade return. We also show in the Appendix that  $f_1$  is Lipschitz, with a Lipschitz constant smaller than that of  $f_0$ .

By iterating this process, we obtain a limit  $f_{\infty}$  of the sequence of frontiers  $(f_n)_{n\geq 0}$  that is decreasing Lipschitz as a limit of decreasing Lipschitz functions with decreasing Lipschitz constants. The process

$$\frac{dx_t}{dt} = \begin{cases} -\lambda x_t & \text{if } w_t < f_{\infty}(x_t), \\ \lambda(1-x_t) & \text{if } w_t > f_{\infty}(x_t), \end{cases}$$
(49)

is an admissible equilibrium since, by construction, if all traders switch to going short to the left of  $f_{\infty}$  and to going long to the right, the indifference point for a trader also lies on  $f_{\infty}$ . We now show that this is the only equilibrium process.

<sup>&</sup>lt;sup>11</sup>The frontier simply obtains from writing  $E_t [l_{t+v}] = \underline{l} + (\overline{l} - \underline{l}) x_t e^{-\lambda v}$  in (39).



Figure 3: Uniqueness of the limiting boundary. This figure illustrates the argument for the uniqueness of the equilibrium boundary separating the two regions. The boundary  $f'_{\infty}$  coincides with  $f_{\infty}$ .

Consider a translation to the left of the graph of  $f_{\infty}$  in (w, x) so that the whole of the curve lies in a region where  $w_t$  is sufficiently small that going short is dominant regardless of the dynamics of  $x_t$ . Call this translation  $f'_0$ . To the left of  $f'_0$ , being short is dominant. Then construct  $f'_1$  as the rightmost translation of  $f'_0$  such that a trader must choose a short position to the left of  $f'_1$  if he believes that other traders will play according to  $f'_0$ . By iterating this process, we obtain a sequence of translations to the right of  $f'_0$ . Denote by  $f'_{\infty}$  the limit of the sequence. Refer to Figure 3.

The boundary  $f'_{\infty}$  does not necessarily define an equilibrium strategy, since it was merely constructed as a translation of  $f'_0$ . However, we know that if all others were to play according to the boundary  $f'_{\infty}$ , then there is at least one point A on  $f'_{\infty}$  where the trader is indifferent. If there were no such point as A, this would imply that  $f'_{\infty}$  is not the rightmost translation, as required in the definition.

We claim that  $f'_{\infty}$  and  $f_{\infty}$  coincide exactly. The argument is by contradiction. Suppose that we have a gap between  $f'_{\infty}$  and  $f_{\infty}$ . Then, choose point B on  $f_{\infty}$  such that A and B have the same height - i.e. correspond to the same x. But then, since the shape of the boundaries of  $f'_{\infty}$  and  $f_{\infty}$  and the values of x are identical, the paths starting from A must have the same distribution as the paths starting from B up to the constant difference in the initial values of w. This contradicts the hypothesis that a trader is indifferent between the two actions both at A and at B. If he were indifferent at A, he would strictly prefer maximum lending at B, and if he is indifferent at B, he would strictly prefer minimum lending when in A. But we constructed A and B so that traders are indifferent in both A and B. Thus, there is only one way to make everything consistent, namely to conclude that A = B. Thus, there is no "gap", and we must have  $f'_{\infty} = f_{\infty}$ .

Proposition 3 shows that adding exogenous shocks  $w_t$  to the carry return eliminates the indeterminacy of the perfect foresight case. More precisely, equilibrium uniqueness stems from the interplay of these shocks with the fact that each global investor, when he receives a switching opportunity, needs to form beliefs about the decisions of the global investors that will have an opportunity to switch between now and his next switching date.

Suppose that  $(w_t, x_t)$  is close to a dominance region in which global investors would prefer a course of action for sure, but just outside it. If  $w_t$  was fixed, it may be possible to construct an equilibrium for both actions, but when  $w_t$  moves around stochastically, it will wander into the dominance region between now and the next opportunity that the trader gets to switch with some probability. This gives the trader some reason to hedge his bets and take one course of action for sure. But then, this shifts out the dominance region, and a new round of reasoning takes place given the new boundary, and so on.

**Remark 1. (Bounded shocks to the world rate)** We model the interest-rate differential as a Brownian motion for expositional simplicity. It is easy to see that we could write it as  $d(w_t)$ , where  $w_t$  is a standard Brownian motion, and d a Lipschitz increasing function, possibly bounded as long as there are still dominant actions for  $w_t$  sufficiently large or small.

**Remark 2.** (Transitory shocks to the world rate) While a strong persistence in shocks to the policy rates is undoubtedly realistic, extensions of this framework can also accommodate for various forms of mean-reversion (Burdzy, Frankel and Pauzner (2001), or Frankel and Burdzy (2005)).

**Remark 3.** (Illiquidity and slow-moving capital) The condition that  $\lambda$  be sufficiently

small seems particularly relevant for the carry trades that involved many retail investors, such as those targeting New Zealand dollar or Icelandic krona. The glacier bonds denominated in Icelandic krona or the uridashi bonds used by Japanese investors to invest in New Zealand had a typical maturity of 1 to 5 years, and were principally purchased by retail investors. More generally, Bacchetta and van Wincoop (2009) claim an average two-year rebalancing frequency to be plausible in FX markets in general, and assume it in order to quantitatively explain the forward discount bias. Also, well-documented price pressure and illiquidity in currency markets, especially for small currencies, may force professional FX speculators to build up or unwind large positions more gradually than they would like to.

#### The case of small shocks

The limiting case in which the volatility  $\sigma$  of the interest-rate differential tends to zero yields useful insights. It is possible to characterize the shape of the frontier f in this case.

In this section we denote the frontier  $f_{\sigma}$  to emphasize its dependence on  $\sigma$ . Suppose the economy is in the state  $(f_{\sigma}(x_t), x_t)$  at date t. That is, it is on the equilibrium frontier. For some arbitrarily small  $\varepsilon > 0$ , introduce the stopping times

$$T_{1} = \inf_{u \ge 0} \left\{ x_{t+u} \notin (\varepsilon, 1-\varepsilon) \right\},$$
  
$$T_{0} = \sup_{0 \le u \le T_{1}} \left\{ w_{t+u} \ne f_{\sigma} (x_{t+u}) \right\}.$$

In words,  $T_1$  is the first date at which  $x_t$  gets close to 0 or 1, and  $T_0$  is the last date at which  $x_t$  crosses the frontier before  $T_1$ . If  $T_0$  is small in distribution, it means that the economy is prone to bifurcations. That is, it never stays around the frontier for long. Upon hitting it, it quickly heads towards extreme values of x. The next proposition shows that this is actually the most likely scenario when  $\sigma$  is small. This, in turn, yields a simple explicit determination of the frontier.

#### **Proposition 6**

1. As  $\sigma \to 0$ ,  $T_0$  converges to 0 in distribution, and the probability that  $\frac{dx_t}{dt} > 0$  (respectively  $\frac{dx_t}{dt} < 0$ ) over  $[T_0, T_1]$  converges to  $1 - x_t$  ( $x_t$  respectively).

2. As  $\sigma \to 0$ , the frontier  $f_{\sigma}$  tends to an affine function. For  $\lambda$  sufficiently small, the slope of this function is increasing in  $\Phi$  and decreasing in  $\gamma$ .

The proof of Proposition 6 is in the Appendix.

First, Proposition 6 clears the concern that in equilibrium, x would only exhibit small fluctuations around a fixed value because Brownian paths cross the frontier too often. As  $\sigma$ becomes smaller, the system exhibits more frequent bifurcations towards extremal values of x. When the system reaches the frontier, it is all the more likely to bifurcate towards capital outflows when cumulative inflows have been large (x large). Thus the model does generate "destabilizing carry trades," whereby global investors generate durable self-justified excess returns on the carry trade followed by large reversals.

The second point in Proposition 6 relates the slope of the frontier  $f_{\sigma}$  to the monetary parameters of the model  $\Phi$  and  $\gamma$  in this case of small shocks. The slope of the frontier affects the dynamics of capital inflows and in turn the exchange-rate dynamics. If the graph of the frontier is closer to being horizontal in the (w, x) plane, then the system should cross the frontier less often, and thus do so only for more extreme values of x. Carry-trade returns should in this case exhibit more serial correlation and fatter tails. Point 2 states that, at least for  $\lambda$  sufficiently small, the frontier is flatter when  $\Phi$  is smaller, and  $\gamma$  larger. In other words, if the central bank fails to respond to inflows by sufficiently reducing its official rate, then carry trade returns should exhibit more skewness.

# 4 Further analytical results

Our model generates a rich set of qualitative features, of which many have empirical predictions. Our approach may shed light on several well-documented empirical findings on carry trade returns.

# Profitability of FX momentum strategies

Proposition 6 shows that as  $\sigma \to 0$ , the system often bifurcates in one direction. This implies that, at least at a sufficiently short horizon, returns are positively autocorrelated, so that momentum strategies in FX markets should generate a positive excess return. It is important to stress that the profitability of momentum strategies is not a mechanical consequence of the assumption of slow-moving capital ( $\lambda$  sufficiently small). Returns on the carry trade are still positively auto-correlated if the system bifurcates quickly towards extreme values of activity x. The key economic force behind this profitability of momentum strategies is that once global investors coordinate on a course of action, they stick to it until a sufficiently large reversal of the interest-rate differential leads them to switch to a different strategy. Such a rationalization of momentum returns with coordination motives is novel to our knowledge.

### Profitability of FX carry trades

Lemma 5 implies that the equilibrium expected return on the carry trade  $\Theta(w, x)$  increases with respect to x. It also implies that  $\Theta(w, x)$  increases with respect to w, because an increase in w is equivalent to a leftward translation of the frontier f in the graph (w, x). On the other hand, the interest-rate differential increases in w and decreases in x. We have indeed:

**Lemma 7** At first-order, the interest-rate differential at a given arrival date  $T_n$  is given by  $R\left(w_{T_n} - l_{T_n} - \frac{1}{1+\Phi} \int_0^{+\infty} e^{-\omega s} E_{T_n}\left[l_{T_n+s}\right] ds\right).$ (50)

The proof of Lemma 7 is in the Appendix.

The interest-rate differential increases w.r.t. w but decreases w.r.t. l (and thus x) because the current domestic real rate is lower and future deflation more likely when l is large. Thus the expected return on the carry trade is not unambiguously increasing in the interest-rate differential. For  $\underline{l}$ ,  $\overline{l}$  sufficiently small, however, most of the interest-rate differential is due to the exogenous component w rather than to the endogenous actions of the global investors l. In this case, when the interest-rate differential is sufficiently large in absolute terms, it must be that the system is on the right (left) of the frontier when the differential is positive (negative). In other words, we have the following interesting prediction:

A positive (negative) interest-rate differential predicts a positive (negative) return on the carry trade only for sufficiently large absolute differentials. The exchange rate must be more volatile when the interest-rate differential is small. When w is small, so is the interest-rate differential, and the differential may correspond to values of (w, x) that are either on the left or on the right of the frontier. The expected return on the carry trade is thus unclear. Since the system is closer to the frontier in this case, future crossings of the frontier are more likely and thus the exchange rate should be more volatile. This is because close to the frontier, for a finite  $\sigma$ , it takes more time for global investors to coordinate on a given course of action and bifurcate in one direction. This nonlinear impact of the interest-rate differential on the carry-trade return has not been tested to our knowledge.

#### Peso problem

A large literature argues that the return on the carry trade partly reflects a risk premium for rare and extreme events that may not show in finite samples (see, e.g., Farhi and Gabaix (2015), Jurek (2014), or Lewis (2007), and the references herein.) We closely connect to this literature as follows. Fix  $\epsilon > 0$  small. The expected return on the carry trade is 0 starting both from  $(f(\epsilon), \epsilon)$  and  $(f(1 - \epsilon), 1 - \epsilon)$  in the (w, x) plane. Yet from Proposition 6, as  $\sigma$ becomes small, most paths starting from  $(f(\epsilon), \epsilon)$  will exhibit long periods of appreciation of the domestic currency ended with rare (and large) depreciations, while paths starting from  $(f(1-\epsilon), 1-\epsilon)$  will feature a symmetric prolonged depreciation. The interest-rate differential is positive in the former case and negative in the latter. Thus, finite samples should yield that a positive interest-rate differential predicts a positive excess return on the carry trade even when the true expected return is zero.

# Leverage and currency appreciation predict financial crises

Gourinchas and Obstfeld (2012) find that credit expansion and appreciation of the domestic currency predict financial crises. The build-up of leverage and currency appreciation correspond to paths in which x increases for a long time in our model. Such paths are the ones in which sharp deleveraging and important capital outflows are most likely to occur soon, other things being equal.

# Monetary policy and carry-trade returns

In addition to relating to the above existing empirical findings, the model also generates a new range of predictions on the relationship between the stance of monetary policy and the distribution of the returns on momentum and carry trade strategies. Proposition 6 suggests that the frontier is flatter when  $\Phi$  is smaller and  $\gamma$  larger. In other words, the frontier is flatter when the central bank is more reluctant to respond to a surge in investment positions with a large reduction in the official rate. This is in turn more likely to be the case when the prices of nontradables are very sticky. Otherwise stated, if an economy is such that the CPI is not too sensitive to the exchange rate, and/or the central bank not too aggressive, then this economy should be more prone to large fluctuations in total investment because it will experience more prolonged bifurcations. Thus the returns on carry-trade and momentum strategies should have fatter tails. These predictions are novel, to our knowledge.

# **Concluding remarks**

The independence of monetary policy under liberalised capital flows and floating exchange rates has been a benchmark principle in international finance. In our paper, we have explored a parsimonious model of global investors facing each other in a dynamic global game and have found that for reasonable parameters of the model, the model generates boom-bust cycles associated with coordinated capital inflows and outflows. In such a setting, monetary conditions depend on the coordination outcome of investors who have access to the domestic bond market, as well as the economic fundamentals. In this sense, we can reject the strict version of the claim that a floating exchange rate guarantees monetary autonomy.

Nevertheless, the rejection of the strict version of the monetary autonomy proposition does not mean that we can derive normative prescriptions that imply the undesirability of floating exchange rates. It is entirely possible that floating exchange rates would emerge as the optimal exchange rate arrangement even when monetary spillovers through exchange rate movements were present. Much will depend on the trade-offs in the second-best problem. We leave the larger policy questions for a more sophisticated model that can do justice to the trade-offs involved. Nevertheless, we see our paper as having established a useful benchmark in the debate. We have shown in our dynamic global game model of international investment flows that, for a reasonable combination of parameters, the unique equilibrium exhibits the observed empirical feature that currency appreciation goes hand-in-hand with looser domestic financial conditions in the form of lower domestic interest rates and higher credit growth fuelled by capital inflows.

When reversed, tighter monetary conditions go hand-in-hand with capital outflows and currency depreciation. We offer these findings as the first steps in a more complete analysis. They come at a time when they may be of some use in making sense of recent macro developments in emerging economies.

# A Appendix

# A.1 Proof of Lemma 4

Using the first-order approximation (35) in (33), relations (30) and (33) yield domestic inflation as a function of future expected inflows as in the perfect foresight case:

$$E_{T_n}\left[\ln\frac{S_{T_{n+1}}I_{T_{n+1}}}{RS_{T_n}}\right] = \frac{\gamma}{1-\gamma}\sum_{k\geq 0}\frac{E_{T_n}\left[l_{T_{n+k+1}}\right]}{(1+\Phi)^{k+1}} - l_{T_n}$$

One can write (27) as

$$\Theta_t = E_t \left[ \sum_{m \ge 0} \frac{1_{\{T_\lambda > T_{n+m}\}}}{R^m} E_{T_{n+m}} \left[ \frac{P_{T_{n+m}} S_{T_{n+m}}}{P_{T_{n+m+1}} S_{T_{n+m+1}}} \left( \frac{S_{T_{n+m+1}} I_{T_{n+m+1}}}{RS_{T_{n+m}}} - 1 + w_{T_{n+m}} \right) \right] \right].$$
(51)

At first-order w.r.t.  $l_t$ ,

$$E_{T_{n+m}}\left[\frac{P_{T_{n+m}}S_{T_{n+m}}}{P_{T_{n+m+1}}S_{T_{n+m+1}}}\left(\frac{S_{T_{n+m+1}}I_{T_{n+m+1}}}{RS_{T_{n+m}}}-1\right)\right] = E_{T_{n+m}}\left[\ln\frac{S_{T_{n+m+1}}I_{T_{n+m+1}}}{RS_{T_{n+m}}}\right]$$
(52)

$$= \frac{\gamma}{1-\gamma} \sum_{k\geq 0} \frac{E_{T_{n+m}} \left[ l_{T_{n+m+k+1}} \right]}{(1+\Phi)^{k+1}} - l_{T_{n+m}}.$$
(53)

Simplifying,

$$\Theta_t = E_t \left[ \int_0^{+\infty} e^{-(\lambda+\rho)s} \left( \int_0^{+\infty} \chi \omega e^{-\omega u} l_{t+s+u} du - l_{t+s} + w_t \right) ds \right]$$
(54)

$$= \int_{0}^{+\infty} e^{-(\lambda+\rho)v} \left( \chi \omega \int_{0}^{v} e^{-(\omega-\lambda-\rho)u} du - 1 \right) E_t \left[ l_{t+v} \right] dv + \frac{w_t}{\lambda+\rho}$$
(55)

Integrating then yields the result.

# A.2 Proof of Lemma 5

Suppose  $\chi > 1$ . Consider two processes  $x_t^1$  and  $x_t^2$  that satisfy the conditions stated in Lemma 5 with  $x_0^1 < x_0^2$ . Lemma 2 in Burdzy, Frankel and Pauzner (1998) states that almost surely,

$$x_t^2 \ge x_t^1 \text{ for all } t \ge 0.$$
(56)

This implies in particular that whenever traders switch to going long along a sample path of  $(w_t, x_t^1)$ , they do so also along the sample path of  $(w_t, x_t^2)$  that corresponds to the same sample path of  $w_t$ . This is because it must be that  $(w_t, x_t^2)$  is on the right of the frontier  $f^2$ whenever  $(w_t, x_t^1)$  is on the right of the frontier  $f^1$ . Thus, the process

$$y_t = x_t^2 - x_t^1 (57)$$

satisfies

$$0 < y_0 < 1,$$
 (58)

$$\frac{dy_t}{dt} = \lambda(\epsilon_t - y_t),\tag{59}$$

In order to prove the lemma, we only need to find  $\overline{\lambda}$  such that for all  $\lambda \leq \overline{\lambda}$ ,

$$\Delta = \int_0^{+\infty} \left( \left( \frac{\chi \omega}{\omega - \rho - \lambda} - 1 \right) e^{-(\lambda + \rho)v} - \frac{\chi \omega}{\omega - \rho - \lambda} e^{-\omega v} \right) y_v dv \ge 0.$$
(60)

for all deterministic process  $y_t$  that obeys (58) and (59). The result then obtains from taking expectations over all paths of  $w_t$ .

To prove (60), we introduce the function  $\zeta$  that satisfies

$$\begin{cases} \frac{d\zeta_{\ell}v}{dv} = -\left(\left(\frac{\chi\omega}{\omega-\rho-\lambda} - 1\right)e^{-(\lambda+\rho)v} - \frac{\chi\omega}{\omega-\rho-\lambda}e^{-\omega v}\right),\\ \lim_{+\infty}\zeta = 0. \end{cases}$$

Integrating by parts, we have

$$\Delta = \zeta(0)y_0 + \int_0^{+\infty} \zeta(v) \frac{dy_v}{dv} dv, \tag{61}$$

$$=\zeta(0)y_0 + \lambda \int_0^{+\infty} \zeta(v)(\epsilon_v - y_v)dv.$$
(62)

$$y_v = y_0 e^{-\lambda v} + \lambda \int_0^v e^{-\lambda(v-u)} \epsilon_u du, \tag{63}$$

$$\Delta = y_0 \left( \zeta(0) - \lambda \int_0^{+\infty} \zeta(v) e^{-\lambda v} dv \right)$$
(64)

$$+\lambda \left[ \int_{0}^{+\infty} \epsilon_{v} \left( \zeta(v) - \lambda \int_{v}^{+\infty} \zeta(u) e^{-\lambda(u-v)} du \right) \right].$$
(65)

We have

$$\lim_{\lambda \to 0} \zeta(0) = \frac{\chi - 1}{\rho} > 0, \tag{66}$$

 $\zeta$  is increasing then decreasing beyond a value that stays bounded as  $\lambda$  tends to zero, and  $\int_0^{+\infty} \zeta$  converges. Thus for  $\lambda$  sufficiently small,

$$\zeta(v) - \lambda \int_{v}^{+\infty} \zeta(u) e^{-\lambda(u-v)} du$$
(67)

is positive for all  $v \ge 0$ , which yields that  $\Delta$  is positive, and concludes the proof.

#### A.3 Complement to the proof of Proposition 3

We prove here that  $f_1$  is Lipschitz with a constant that is smaller than that of  $f_0$ , that we denote  $K_0$ . Suppose by contradiction that two points  $(w_t, x_t)$  and  $(w'_t, x'_t)$  on  $f_1$  satisfy

$$x' > x, \tag{68}$$

$$\frac{x'_t - x_t}{w_t - w'_t} < \frac{1}{K_0}.$$
(69)

We compare the paths  $x'_{t+u}$  and  $x_{t+u}$  corresponding to pairs of paths of  $w'_{t+u}$  and  $w_{t+u}$  that satisfy for all  $u \ge 0$ 

$$w_{t+u} - w'_{t+u} = w_t - w'_t. ag{70}$$

It must be that for such pairs of paths:

$$x'_{t+u} - x_{t+u} \le (x'_t - x_t)e^{-\lambda u}.$$
(71)

Otherwise it would have to be the case that (w', x') can be on the right of  $f_0$  when (w, x) is not. Let T denote the first time at which this occurs. It must be that

$$K_0 e^{-\lambda T} (x'_t - x_t) \ge w_{t+T} - w'_{t+T} = w_t - w'_t, \tag{72}$$

a contradiction with (69). Thus along such paths of  $w'_{t+u} - w_{t+u}$ ,  $x'_{t+u} - x_{t+u}$  shrinks at least as fast as when traders switch to going short all the time. Together with (69), this implies that the expected return on the carry trade cannot be the same in  $(w_t, x_t)$  and  $(w'_t, x'_t)$ , a contradiction.

# A.4 Proof of Proposition 6

The first point is a particular case of Theorem 2 in Burdzy, Frankel and Pauzner (1998). To prove the second point, notice that as  $\sigma \to 0$ , starting from a point on the frontier,

$$E_t [x_{t+\nu}] \simeq (1 - x_t) \left( 1 - (1 - x_t)e^{-\lambda \nu} \right) + x_t^2 e^{-\lambda \nu}$$
(73)

because the system bifurcates upwards with probability  $1 - x_t$  and downwards with probability  $x_t$  in the limit. Plugging this in (39) and writing that the expected return is zero yields a slope of the frontier equal to

$$-(\bar{l}-\underline{l})(\chi-1)$$

as  $\lambda \to 0$ . This means that the absolute value of the slope of the frontier varies as  $\chi$  w.r.t.  $\gamma$ ,  $\Phi$  for  $\sigma$ ,  $\lambda$  sufficiently small. This proves the proposition.

# A.5 Proof of Lemma 7

We have

$$I_{T_n+1} - R(1 - w_{T_n}) = R\left(\left(\frac{P_{T_n}}{P_{T_{n-1}}}\right)^{1+\Phi} - 1 + w_{T_n}\right),\tag{74}$$

$$\simeq R\left(w_{T_n} - E_{T_n}\left[\sum_{k\geq 0} \frac{l_{T_n+k}}{(1+\Phi)^k}\right]\right),\tag{75}$$

$$= R\left(w_{T_n} - l_{T_n} - \int_0^{+\infty} \sum_{k \ge 1} \frac{s^{k-1} e^{-s}}{(k-1)!(1+\Phi)^k} E_{T_n}\left[l_{T_n+s}\right] ds\right), \quad (76)$$

$$= R\left(w_{T_n} - l_{T_n} - \frac{1}{1+\Phi} \int_0^{+\infty} e^{-\omega s} E_{T_n}\left[l_{T_n+s}\right] ds\right).$$
(77)

This proves the lemma.

# References

Adrian, Tobias and Hyun Song Shin (2010) "Liquidity and Leverage," *Journal of Financial Intermediation*, 19, 418-437

Adrian, Tobias and Hyun Song Shin (2014) "Procyclical leverage and Value-at-Risk" *Review* of Financial Studies, 27 (2), 373-403

Agrippino, Silvia Miranda and Helene Rey (2014) "World Asset Markets and the Global Liquidity," working paper

Albagli, Elias, Christian Hellwig and Aleh Tsyvinski (2015) "A Theory of Asset Prices based on Heterogeneous Information," working paper

Bacchetta, Philippe and Eric van Wincoop (2010) "Infrequent Portfolio Decisions: A Solution to the Forward Discount Puzzle," *American Economic Review*, 100(3), 870-904

Bank for International Settlements (2010) "Funding patterns and liquidity management of internationally long banks" CGFS Papers 39, Committee on the Global Financial System, http://www.bis.org/publ/cgfs39.pdf

Bank for International Settlements (2011) "Global liquidity – concept, measurement and policy implications" CGFS Papers 45, Committee on the Global Financial System http://www.bis.org/publ/cgfs45.pdf

Bass, Richard and Krzysztof Burdzy (1999) "Stochastic bifurcation models," Annals of Probability, 27, 50-108

Borio, Claudio (2014) "The International Monetary and Financial System: Its Achilles Heel and What To Do About It" BIS Working Paper 456 http://www.bis.org/publ/work456.pdf

Borio, Claudio and Piti Disyatat (2011) "Global imbalances and the financial crisis: Link or no link?" BIS Working Paper 346 http://www.bis.org/publ/work346.pdf

Borio, Claudio, Harold James and Hyun Song Shin (2014) "The International Monetary and Financial System: A Capital Account Historical Perspective" BIS Working Paper 457 http://www.bis.org/publ/work457.pdf

Bruno, Valentina and Hyun Song Shin (2015a), "Cross-Border Banking and Global Liquidity," *Review of Economic Studies*, 82 (2), 535-564

Bruno, Valentina and Hyun Song Shin (2015b), "Capital flows and the risk-taking channel of monetary policy" *Journal of Monetary Economics*, 71, 119-32.

Burdzy, Krzysztof, David Frankel and Ady Pauzner (2001) "Fast Equilibrium Selection by Rational Players Living in a Changing World," *Econometrica*, 68, 163-190

Burdzy, Krzysztof, David Frankel and Ady Pauzner (1998) "On the Time and Direction of Stochastic Bifurcation," In B. Szyszkowicz, ed. Asymptotic Methods in Probability and Statistics: A Volume in Honour of Miklos Csorgo. Holland: Elsevier

Burstein, Ariel, Martin Eichenbaum and Sergio Rebelo (2005) "Large Devaluations and the Real Exchange Rate," *Journal of Political Economy*, Vol. 113, No. 4, 742-784

Cochrane, John, (2011) "Determinacy and Identification with Taylor Rules," *Journal of Political Economy*, Vol. 119, No. 3 (June 2011), pp. 565-615.

Du, Wenxin and Jesse Schreger (2015) "Local currency sovereign risk" forthcoming in the *Journal of Finance* 

Engel, Charles (2015) "Exchange Rates and Interest Parity," Handbook of International Economics, 4, 453-522

Farhi, Emmanuel and Xavier Gabaix (2015) "Rare Disasters and Exchange Rates", working paper

Farhi, Emmanuel and Jean Tirole (2012) "Collective Moral Hazard, Maturity Mismatch and Systemic Bailouts," *American Economic Review*, vol. 102, 60-93

Fleming, J. Marcus (1962): "Domestic financial policies under fixed and floating exchange rates" *IMF Staff Papers* 9, 369–379.

Forbes, Kristin J. and Francis E. Warnock (2012) "Capital Flow Waves: Surges, Stops, Flight and Retrenchment" Journal of International Economics, 88(2): 235-251

Frankel, David and Krzysztof Burdzy, (2005) "Shocks and Business Cycles," Advances in Theoretical Economics, v. 5 iss. 1 paper no. 2

Frankel, David and Ady Pauzner (2000) "Resolving Indeterminacy in Dynamic Settings: The Role of Shocks," *Quarterly Journal of Economics*, Vol. 115, 283-304

Friedman, Milton (1953) "The case for flexible exchange rates" in *Essays in Positive Economics*, University of Chicago Press

Gabaix, Xavier and Matteo Maggiori (2015) "International Liquidity and Exchange Rate Dynamics," *Quarterly Journal of Economics*, forthcoming

Garleanu, Nicolae, Stavros Panageas and Jianfeng Yu (2015) "Financial Entanglement: A Theory of Incomplete Integration, Leverage, Crashes, and Contagion," *American Economic Review*, forthcoming

Goldstein, Itay and Ady Pauzner (2005) "Demand Deposit Contracts and the Probability of Bank Runs," *Journal of Finance*, 60(3), 1293-1328.

Gopinath, Gita (2015) "The international price system" paper presented at 2015 Jackson Hole conference http://scholar.harvard.edu/files/gopinath/files/paper\_083115.pdf

Gourinchas, Pierre-Olivier and Maurice Obstfeld (2012) "Stories of the Twentieth Century for the Twenty-First," *American Economic Journal: Macroeconomics*, 4, 226-65

He, Zhiguo, Arvind Krishnamurthy and Konstantin Milbradt (2015) "A model of the reserve asset", working paper.

He, Zhiguo and Wei Xiong (2012), "Dynamic Debt Runs," *Review of Financial Studies*, 25, 1799-1843

Hofmann, Boris, Ilhyock Shim and Hyun Song Shin (2016) "Sovereign yields and the risk-taking channel of currency appreciation" *BIS Working Paper* No. 538, January.

Jurek, Jakub (2014) "Crash-Neutral Currency Carry Trades," Journal of Financial Economics, forthcoming

Kaminsky, G. L., Reinhart, C. M., (1999) "The twin crises: the causes of banking and balance-of-payments problems" *American Economic Review* 89, 473-500.

Klau, Marc and Dubravko Mihaljek (2008) "Exchange rate pass-through in emerging market economies: what has changed and why?" BIS Papers No 35, Bank for International Settlements

Lewis, Karen (2007) "Peso Problem," The New Palgrave Dictionary of Money and Finance

Mundell, Robert A. (1963): "Capital mobility and stabilisation policy under fixed and flexible exchange rates" *Canadian Journal of Economic and Political Science* 29(4), 475–485.

Obstfeld, Maurice (1996) "Models of currency crises with self-fulfilling features," *European Economic Review*, vol. 40(3-5), 1037-1047

Rey, Hélène (2013) "Dilemma not trilemma: the global financial cycle and monetary policy independence" proceedings of the Federal Reserve Bank of Kansas City Economic Symposium at Jackson Hole.

Rey, Hélène (2014) "International channels of transmission of monetary policy and the Mundellian trilemma" Mundell-Fleming lecture. IMF Annual Research Conference

Rose, Andrew and Mark Spiegel (2009). "Cross-Country Causes and Consequences of the 2008 Crisis: International Linkages and American Exposure." NBER Working Paper #15358.

Schneider, Martin and Aaron Tornell (2004), "Balance Sheet Effects, Bailout Guarantees and Financial Crises," *Review of Economic Studies*, 71, 883-913

Schularick, Moritz and Alan M. Taylor (2012) "Credit Booms Gone Bust: Monetary Policy, Leverage Cycles, and Financial Crises, 1870-2008." *American Economic Review* 102, 1029–61

Shek, Jimmy, Ilhyock Shim and Hyun Song Shin (2015) "Investor redemptions and fund manager sales of emerging market bonds: how are they related?" BIS Working Paper 509

Shin, Hyun Song (2012) "Global Banking Glut and Loan Risk Premium" Mundell-Fleming Lecture, IMF Economic Review 60 (2), 155-192.

Taylor, John B. (1993) "Discretion Versus Policy Rules in Practice," *Carnegie-Rochester Conference Series on Public Policy* 39, 195-214.

Woodford, Michael (2001) "The Taylor Rule and Optimal Monetary Policy" American Economic Review, 91 (2), 232-237.

# Previous volumes in this series

No	Title	Author
536 January 2016	Is macroprudential policy instrument blunt?	Katsurako Sonoda and Nao Sudo
535 January 2016	Interbank networks in the national banking era: their purpose and their role in the panic of 1893	Charles W Calomiris and Mark Carlson
534 December 2015	Labour reallocation and productivity dynamics: financial causes, real consequences	Claudio Borio, Enisse Kharroubi, Christian Upper and Fabrizio Zampolli
533 December 2015	Managing price and financial stability objectives – what can we learn from the Asia- Pacific region?	Soyoung Kim and Aaron Mehrotra
532 December 2015	Mortgage risk and the yield curve	Aytek Malkhozov, Philippe Mueller, Andrea Vedolin and Gyuri Venter
531 December 2015	The supply side of household finance	Gabriele Foà, Leonardo Gambacorta, Luigi Guiso and Paolo Emilio Mistrulli
530 November 2015	Commercial Bank Failures During The Great Recession: The Real (Estate) Story	Adonis Antoniades
529 November 2015	A search-based model of the interbank money market and monetary policy implementation	Morten Bech and Cyril Monnet
528 November 2015	External shocks, banks and optimal monetary policy in an open economy	Yasin Mimir and Enes Sunel
527 November 2015	Expectations and Risk Premia at 8:30AM: Macroeconomic Announcements and the Yield Curve	Peter Hördahl, Eli M Remolona and Giorgio Valente
526 November 2015	Modelling the Time-Variation in Euro Area Lending Spread	Boris Blagov, Michael Funke and Richhild Moessner
525 October 2015	Capital flows and the current account: Taking financing (more) seriously	Claudio Borio and Piti Disyatat
524 October 2015	Breaking free of the triple coincidence in international finance	Stefan Avdjiev, Robert N McCauley and Hyun Song Shin
523 October 2015	The evolution of inflation expectations in Canada and the US	James Yetman
522 October 2015	Do banks extract informational rents through collateral?	Bing Xu, Honglin Wang and Adrian van Rixtel
521 October 2015	Does variance risk have two prices? Evidence from the equity and option markets	Laurent Barras and Aytek Malkhozov
520 October 2015	Optimal Inflation with Corporate Taxation and Financial Constraints	Daria Finocchiaro, Giovanni Lombardo, Caterina Mendicino and Philippe Weil

All volumes are available on our website www.bis.org.