## Money Talks: Information and Monetary Policy

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The views expressed are solely those of the authors.

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■ Deeds need to complement words!

## Research questions

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■ Why do central banks typically follow policies that lead to positive average inflation levels?

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■ The CB has info about fundamentals $\rightarrow$ how to reveal it?

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■ enable more socially efficient investment
$■ \rightarrow$ monetary policy as an optimal balance of this tradeoff

- Changes in the interest rate need not be large to be effective


## The environment

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■ Benevolent CB serves for one period and can:

- print money

■ make loans to the private sector
■ make announcements

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■ Each period: three stages 0,1 , and 2

- Three goods:
- stage 0: an investment good $k$, uncertain return $\theta^{2}$ per unit
- stage 1: good $q$
- stage 2: good $z$


## Preferences and technology

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- Stage-1 good:
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- utility of consumption: $u(q)$

■ Stage-2 good:

- linear utility of consumption (cost of production)
- $\rightarrow$ agents use Stage 2 to equalize money holdings


## Timeline

Nature chooses $\theta$, signals are sent. The CB makes an announcement or changes the interest rate $r$. Investor $i$ produces $k_{i}$ units of the investment good.

Market for good $q$ opens. Good $q$ is traded in exchange for money. Agents can borrow at the lending facility of the $C B$ at the interest rate $r \geq 0$.

Investment matures. Agents produce or consume good $z$, repay their loans (if any), and even their money holdings.

## Benchmark: Fundamentals observable

■ Planner max period- $t$ social welfare:

$$
W\left(k_{i}, \theta\right)=\frac{1}{2}\left[u(q)-q+\int \theta^{2} k_{i} d i-\int \frac{k_{i}^{2}}{2} d i\right]
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■ Decentralization using cash:

- agents can borrow from the CB at $r \geq 0$ at stage 1
- Friedman rule is optimal: $r=0$ for all states


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■ CB's tools: announcements and changes of $r$

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■ but: lower $\alpha_{a}$ increases mean investment

- No equilibrium where the CB announces its precision truthfully and the investors use the announcement $\rightarrow$ Talk is cheap!


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■ Pooling: agents use $\bar{\alpha}=\pi \alpha_{L}+(1-\pi) \alpha_{H}$ and the CB sets $r(\bar{\alpha})=0$

- If agents' expectations are far away from the truth, costly signaling is preferred to costless pooling


## Credible interest rate changes

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- For $C R R A=1$, credible info transmission achieved with $r=27$ b.p.
- For $C R R A=4$, credibility achieved with $r=54$ b.p.


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■ Extensions:

- Signaling both $y$ and $\alpha$
- Correlated signals
- Other instruments


## Thank you!

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■ Discounted lifetime utility entering Stage 2 :

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\begin{aligned}
W(k, m, l ; \theta) & =\max _{z, m_{+1}}\left\{-z+\beta E V\left(m_{+1} ; \theta\right)\right\} \\
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■ Expected discounted lifetime utility entering Stage 0:

$$
\begin{aligned}
V(m)= & \frac{1}{2} \max _{k_{i}}\left\{-\frac{k_{i}^{2}}{2}+E\left[\max _{q}-q+W\left(k_{i}, m+p q, 0, \theta\right)\right]\right\} \\
& +\frac{1}{2} E\left[\max _{q, l \text { s.t. } p q \leq m+l} u(q)+W(0, m+I-p q, I, \theta)\right]
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## Stages

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■ Stage 2: General market

- return $\theta^{2}$ per unit of $k$ realized, consumed
- good $z$ traded
- frictionless Walrasian market

