

# Financial Institution Dynamics and Capital Regulations

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- During the financial crisis, regulatory discussions included
  - insufficient capitalization of banks;
  - bank dividend payouts (Acharya, Gujral, Kulkarni and Shin 2011);
  - executive compensation (FSF 2009).
- Basel III
  - Capital conservation buffer (2.5%) + min. capital requirement (4.5%).
  - Distribution of earnings will be restricted if the buffer is drawn down.

# Objective & Issues with Existing Macro-Banking Models

- Our goal: Analysis of macroeconomic implications of minimum capital requirement and conservation buffer in Basel III.
- To do so, we need model environment whereby over-payment of dividends and executive bonuses naturally arise.
- There is no off-the-shelf macro-banking models....
  - Manager's incentive perfectly aligned with shareholders' interests.
  - No equity issuance.

- Main ingredients of our dynamic macro-banking model:
  - ① Outside equity
  - ② An impatient manager controls the bank
  - ③ Moral hazard through limited liability
- These elements allow us to analyze capitalization and risk taking of banks simultaneously.

- Under-capitalization due to time-inconsistency problem. Time inconsistency problems exist because of:
  - Reoptimization of dividend payment;
  - Dilution of existing equities.
- Excessive leverage by banks due to moral hazard.
- Need for both capital conservation buffer and minimum capital requirement.

# The Model: Bank without Uncertainty

- An impatient manager runs the bank ( $\chi < \beta$ ).
- Budget constraint:  $c + z + y = n + \alpha m$ .
- New equity issuance:  $m = e\beta\Omega(n')$ .
- Market valuation of bank equity in equilibrium:

$$\Omega(n) = z(n) + \beta[1 - e(n)]\Omega(n'(n)).$$

- Concave loan returns as a function of  $y$ :  $n' = f(y)$ .

# Time Inconsistency Problem and Incentive Alignment

The manager today wants to set  $z = 0$  and  $e = 1$ . We assume that existing shareholders impose the following restrictions:

- Manager's bonus is tightly linked to dividends:

$$c \leq \psi z.$$

- Anti-dilution protection determines the fraction of new claims by an accounting rule:

$$e \leq \frac{m}{(n - \gamma c - z) + m}.$$

# Banker without Commitment (Markov Perfect Equilibrium)

$$V(n) = \max_{\{c,z,y,e,m\}} \{u(c) + \chi V(f(y))\}$$

subject to

$$c + z + y = n + \alpha m$$

$$m = e\beta\Omega(f(y))$$

$$c \leq \psi z$$

$$e = \frac{m}{(n - \gamma c - z) + m}.$$

- MPE is time-consistent but not history-dependent.
- Tomorrow's manager will *not* take into account that tomorrow's dividend policy affects today's equity issuance. Manager knows this.



## Generalized Euler Equation:

$$u_c = \frac{\chi(1-\alpha)f_y}{1 + \alpha\beta\gamma\psi f_y z'_n - \alpha\beta f_y} u'_c.$$

- $z'_n \equiv \frac{\partial z'}{\partial n'}$  captures preemptive action of the banker.
- This collapses to a usual Euler equation when  $\alpha = 0$ :  $u_c = \chi f_y u'_c$ .
- $z'_n > 0$  reduces  $y$  as there is an extra cost of increasing  $y$  through

$$\Omega(f(y)) = -\psi\gamma z(f(y)) + f(y).$$

More  $y$  partially erodes  $\Omega'$  as unproductive  $c$  will increase.

# Steady State Comparison

- Markov Perfect Equilibrium:

$$f_y^{ME} = \frac{1}{\chi(1-\alpha) + \alpha\beta(-\gamma\psi z'_n + 1)}$$

- Commitment Equilibrium:

$$f_y^{CM} = \frac{1}{\chi(1-\alpha) + \alpha\beta}$$

- Social Planner

$$f_y^{SP} = \frac{1}{\beta}$$

- Insufficient capitalization if  $z'_n > 0$ .

$$y^{SP} > y^{CM} > y^{ME}.$$

# Numerical Results (Steady State)

- Functional forms:  $u(c) = \log(c)$ ,  $f(y) = y^\nu$ .
- Parameter values:

$\alpha$	$\beta$	$\gamma$	$\chi$	$\psi$	$\nu$
0.98	0.99	0.5	0.9	1.0	0.9

- Results:  $z'_n = 0.036 > 0$ . Thus,  $y^{CM} > y^{ME}$ .

## Commitment Equilibrium vs Markov Perfect Equilibrium

	$y$	$z$	$\Omega$	$z/\Omega$	$m/\Omega$
Commitment	0.31	0.035	0.33	0.10	0.09
Markov Perfect	0.26	0.034	0.28	0.12	0.11

# Introducing Loans under Uncertainty

- Loans are funded by deposit and capital:  $\ell = y + d$ .
- Net loan return function generating  $n'$  exhibits DRS:

$$n' = F(\ell, y, \eta') = R\ell^{1-\gamma}\eta' - \left[ R_d + \underbrace{h(\ell - y)}_{=d} \right] \underbrace{(\ell - y)}_{=d},$$

where  $h(d)$  is the internal cost of deposit.

- The bank defaults when the shock,  $\eta'$ , is small.
- We want to show

$$\text{leverage}^{ME} > \text{leverage}^{CM} > \text{leverage}^{SP},$$

$$y^{ME} < y^{CM} < y^{SP}.$$

# The Model with Loans under Uncertainty

$$V(n; \Omega) = \max_{\{c, z, y, l, e, m\}} \left\{ u(c) + \chi \int_{\eta'_*(l, y)} V(F(l, y, \eta'); \Omega) dG(\eta') \right. \\ \left. + \chi V(\underline{n}) [1 - G(\eta'_*(l, y))] \right\}$$

subject to

$$c + z + y = n + \alpha m \\ m = \beta e \int_{\eta'_*(l, y)} \Omega(F(l, y, \eta')) dG(\eta') \\ c \leq \psi z \\ e = \frac{m}{m + n - \gamma c - z}.$$

## Two State Example (Long-Surviving Bankers)

- $\eta' \in \{0, 1\}$  and  $p_1 = \Pr(\eta' = 1)$ . Default when  $\eta' = 0$ .
- Assume  $h = \kappa \cdot (\ell - y)$ .
- The marginal condition w.r.t.  $\ell$  determines  $\ell(y)$ .

$$F_{\ell}^{\text{Banker}} = (1 - \gamma) R \ell^{-\gamma} - [R_d + 2\kappa(\ell - y)] = 0.$$

- Due to DRS,  $d\ell(y) / dy < 1$ , implying leverage is decreasing in  $y$ .
- As before,  $y^{\text{ME}} < y^{\text{CM}}$  due to time inconsistency. Hence,

$$\text{leverage}^{\text{ME}} > \text{leverage}^{\text{CM}}.$$

## Two State Example (Comparison with Social Planner)

- Marginal conditions w.r.t.  $\ell$  and  $y$  imply  $d^{CM} > d^{SP}$  and  $\ell^{CM} < \ell^{SP}$ :

$$d^{CM} = \frac{p_1^{-1} [\chi(1-\alpha) + \alpha\beta]^{-1} - R_d}{2\kappa} > \frac{\beta^{-1} - R_d}{2\kappa} = d^{SP},$$

$$\ell^{CM} = [[\chi(1-\alpha) + \alpha\beta] p_1 (1-\gamma) R]^{1/\gamma} < [\beta p_1 (1-\gamma) R]^{1/\gamma} = \ell^{SP}$$

- Moral hazard and impatience induce higher leverage for bankers.

$$\text{leverage}^{CM} > \text{leverage}^{SP},$$

$$y^{CM} < y^{SP}.$$

- Markov perfect equilibrium exhibits insufficient capital accumulation and excessive leverage.
- Minimum capital requirement places a cap on banks' leverage.
  - This addresses over-borrowing but not necessarily under-capitalization.
- Basel III complements this by restricting dividend payouts and manager compensation of banks with low capital.
  - May be an effective policy to address issues arising from *both* time inconsistency and moral hazard.



# Conclusion

- Time inconsistency problem regarding outside equity issuance leads bankers to pay excessive dividends and accumulate insufficient capital.
- Moral hazard problem leads to too much borrowing and thus excessive leverage of banks.
- Minimum capital requirement may not be adequate to promote capital accumulation. Capital conservation buffer may be an effective policy instrument.
- What's next?
  - Global solution (non-steady-state analysis).
  - Quantitative analysis of capital regulations.
  - Markovian evolution of banking industry.
  - Aggregate shocks.
  - General equilibrium.