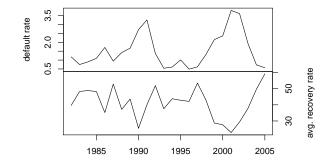
Recovery Rates, Default Probabilities and the Credit Cycle

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CEMFI

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Motivation



The research questions & method

The questions:

- Can you exploit the joint time-series behaviour of default rates and recovery rates to characterize and forecast credit risk?
- How bad is it to treat recovery rates as constant (or independent of default probabilities)?

The method:

• We propose an econometric model in which both the time variation in default probabilities and recovery rate distributions is driven by an unobserved Markov chain, the "credit cycle".

Related literature

- Default probabilities or rating transitions vary over time, and are related to macro variables. (Bangia et al. (2002), Nickell et al. (2000))
- Recovery rates and default probabilities are contemporaneously negatively related.

(Altman et al. 2006, Acharya et al. 2007)

- Recovery rates and default probabilities can be modelled as functions of observed covariates. (Chava et al. 2006)
- Theory:
 - Recovery rates should be related to the state of the industry: Shleifer and Vishny (1992).
 - RBC and credit: Bernanke and Gertler (1989), Williamson (1987)

Observed covariates versus latent factor:

- The proposed model describes the data well, and does better than many models based on observed covariates.
- E.g. out-of-sample rolling RMSE for predicted recovery rates is 22.86%. (Chava et al. 2006: 24.96%)

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We can use the estimated model to look at what happens when we go from constant to time-varying recovery rate distributions. We get

- higher estimates of tail risk, (for a sample portfolio, the 99% VaR goes from 2.6% to 2.9%.)
- the same expected losses,
- bigger swings in spreads over the cycle. Average spreads over the cycle are not affected.

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Caveats?

The basic idea

The DGP works as follows:

- The state of the credit cycle is determined by a two-state Markov chain.
- The number of defaulting firms is drawn using the state-dependent default probability.
- For each defaulting firm, we draw a recovery rate from the state-dependent recovery rate distribution.

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Dependence:

- Conditional on the state, defaults are independent, recoveries between firms are independent, and the number of defaulting firms and recoveries are independent.
- As a consequence, (unconditional) dependence is driven entirely by the (unobserved) state of the credit cycle.

• Conditional on the state of the cycle, default arrival is described by discrete hazards of the form

$$\lambda_{t} = (1 + \exp\{\gamma_{0} + \gamma_{1}c_{t} + \gamma_{2}X_{t}\})^{-1}$$

(t: time, c_t : cycle, X_t : economy-wide variables)

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- Recoveries for each default event are drawn from a beta distribution.
- The parameters of this beta distribution are given by:

$$\alpha_{tis} = \exp\left\{\delta_0 + \delta_1 c_t + \dots + \delta_6 X_t\right\}$$
(1)
$$\beta_{tis} = \exp\left\{\zeta_0 + \zeta_1 c_t + \dots + \zeta_6 X_t\right\}$$
(2)

(*i*: firm, *s*: seniority)

Estimation

- The model can be easily be estimated using a version of the Hamilton filter (MLE).
- For this we need the number of defaulting firms, and non-defaulting firms in each period, and a recovery rate for each default event.

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• We augment this with GDP growth, investment growth, unemployment, the S&P 500 index, the VIX, the slope of the term structure, and an NBER recession indicator.

Macro variables versus the business cycle

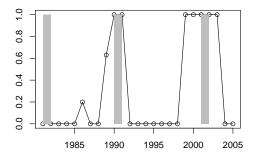
| | Model 1 | Model 2 | Model 3 | Model 4 | | |
|---|------------------------|------------------------|------------------------|------------------------|--|--|
| Explanatory variables for λ (default probability) | | | | | | |
| | constant | constant | constant | constant | | |
| | | cycle | log GDP growth | cycle | | |
| | | | | log GDP growth | | |
| Explanatory variables for α,β (recovery rates) | | | | | | |
| | constant | constant | constant | constant | | |
| | | cycle | log GDP growth | cycle | | |
| | | | | log GDP growth | | |
| | seniority ^a | seniority ^a | seniority ^a | seniority ^a | | |
| AIC | -37.73 | -405.31 | -128.96 | -412.79 | | |
| BIC | 0.0727 | -0.1549 | 0.0188 | -0.1290 | | |
| | | | | | | |

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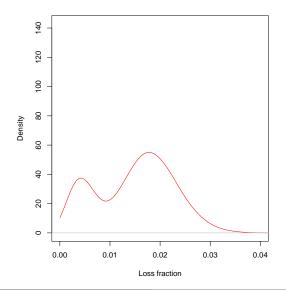
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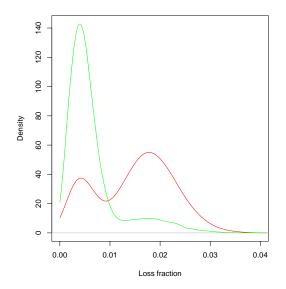
 \implies Macro variables are significant, but do not contribute much to the fit.

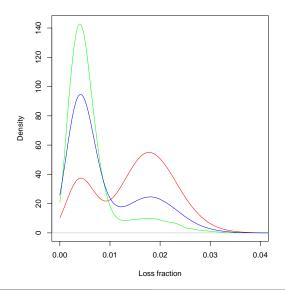
Is the business cycle = credit cycle?

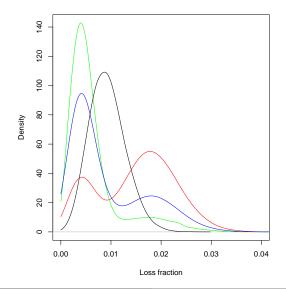


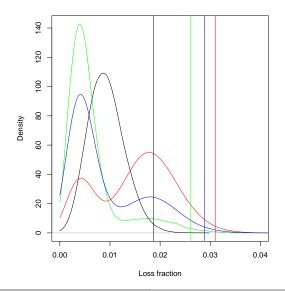
- The estimated credit downturns start earlier than NBER recessions, and end later.
- We investigate lead-lag relationships between macro variables and credit variables and find that recovery rates Granger cause log GDP growth (very significant!).

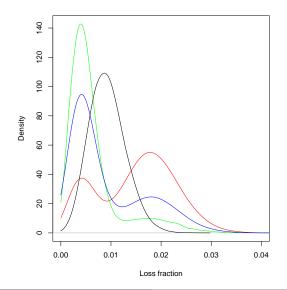


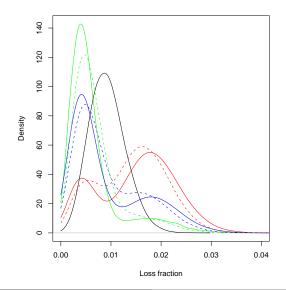


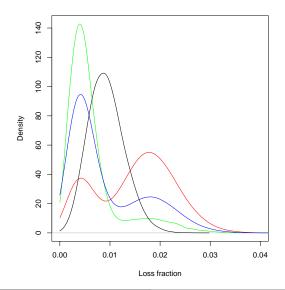


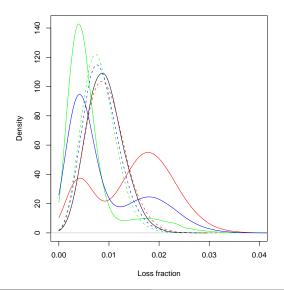












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Therefore

$$\begin{split} E[L \cdot PD] &= .5 \times 30\% \times 0.02 + .5 \times 70\% \times 0.1 = 3.8\% \\ E[L] \cdot E[PD] &= 3\% \end{split}$$

$$\implies E[L \cdot PD] - E[L] \cdot E[PD] = 80bp$$

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- But $E[L \cdot PD] E[L]E[PD] = Cov(L, PD)$.
- In our data, Cov(avg. L, dfr) = 5bp.

Some conclusions

- We propose an econometric model in which default rates and recovery rates are driven by an unobserved Markov chain.
- This describes the data well, and does better than many models based on observed covariates.

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